

1 **A coarse-grained NADH redox model enables inference of subcellular** 2 **metabolic fluxes from fluorescence lifetime imaging**

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9

10 **Abstract**

11
12 Mitochondrial metabolism is of central importance to diverse aspects of cell and developmental
13 biology. Defects in mitochondria are associated with many diseases, including cancer,
14 neuropathology, and infertility. Our understanding of mitochondrial metabolism *in situ* and
15 dysfunction in diseases are limited by the lack of techniques to measure mitochondrial metabolic
16 fluxes with sufficient spatiotemporal resolution. Herein, we developed a new method to infer
17 mitochondrial metabolic fluxes in living cells with subcellular resolution from fluorescence
18 lifetime imaging of NADH. This result is based on the use of a generic coarse-grained NADH
19 redox model. We tested the model in mouse oocytes and human tissue culture cells subject to a
20 wide variety of perturbations by comparing predicted fluxes through the electron transport chain
21 (ETC) to direct measurements of oxygen consumption rate. Interpreting the FLIM measurements
22 of NADH using this model, we discovered a homeostasis of ETC flux in mouse oocytes:
23 perturbations of nutrient supply and energy demand of the cell do not change ETC flux despite
24 significantly impacting NADH metabolic state. Furthermore, we observed a subcellular spatial
25 gradient of ETC flux in mouse oocytes and found that this gradient is primarily a result of a
26 spatially heterogeneous mitochondrial proton leak. We concluded from these observations that
27 ETC flux in mouse oocytes is not controlled by energy demand or supply, but by the intrinsic
28 rates of mitochondrial respiration.
29

30 **Introduction**

31
32 Cells transduce energy from the environment to power cellular processes. Decades of extensive
33 research have produced a remarkable body of detailed information about the biochemistry of
34 mitochondrial energy metabolism (Salway, 2017). In brief, metabolites, such as pyruvate, are
35 transported into mitochondria, where they are broken down and their products enter the
36 tricarboxylic acid cycle (TCA). The TCA is composed of a number of chemical reactions, which
37 ultimately reduces NAD⁺ to NADH. NADH and oxygen are then utilized by the electron
38 transport chain (ETC) to pump hydrogen ions across the mitochondrial membrane. ATP synthase
39 uses this proton gradient to power the synthesis of ATP from ADP (Mitchell, 1961). The
40 activities of mitochondrial energy metabolism are characterized by the fluxes through these
41 pathways: i.e. the number of molecules turned over per unit time (Stephanopoulos, 1999).
42 However, despite the wealth of knowledge concerning mitochondrial biochemistry, the
43 spatiotemporal dynamics of cellular energy usage remains elusive and it is still unclear how cells
44 partition energy across different cellular processes (Dumollard et al., 2007; Blerkom, 2011;
45 Yellen 2018, Yang 2021) and how energy metabolism is misregulated in diseases (Brand and

46 Nicholls, 2011; Lin and Flint Beal, 2006; Wallace, 2012; Bratic and Larsson, 2013; Lowell and
47 Shulman, 2005; Mick et al., 2020). Metabolic heterogeneities, between and within individual
48 cells, are believed to be widespread, but remain poorly characterized (Takhaveev and Heinemann
49 2018; Aryaman et al., 2019). Mitochondria have been observed to associate with the
50 cytoskeleton (Lawrence et al., 2016), spindle (Wang et al., 2020), and endoplasmic reticulum
51 (Dumollard et al., 2004) and display subcellular heterogeneities in mtDNA sequence (Morris et
52 al., 2017) and mitochondrial membrane potential (Smiley et al., 1991). These observations
53 suggest the potential existence of subcellular patterning of mitochondrial metabolic fluxes that
54 could be critical in processes such as oocyte maturation (Yu et al., 2010) and embryo
55 development (Sanchez et al., 2019). The limitations of current techniques for measuring
56 mitochondrial metabolic fluxes with sufficient spatiotemporal resolution presents a major
57 challenge. In particular, there is a lack of techniques to measure mitochondrial metabolic fluxes
58 with single cell and subcellular resolution.

59
60 Bulk biochemical techniques for measuring metabolic fluxes, such as oxygen consumption and
61 nutrient uptake rates (Ferrick et al., 2008; Houghton et al., 1996; Lopes et al., 2005), and isotope
62 tracing by mass spectrometry (Wiechert, 2001), require averaging over large populations of cells.
63 Such techniques cannot resolve cellular, or subcellular, metabolic heterogeneity (Takhaveev and
64 Heinemann, 2018; Aryaman et al., 2019). Biochemical approaches for measuring mitochondrial
65 metabolic fluxes, such as mass spectrometry, are also often destructive (Wiechert, 2001; Saks, et
66 al 1998), and thus cannot be used to observe continual changes in fluxes over time. Fluorescence
67 microscopy provides a powerful means to measure cellular and subcellular metabolic
68 heterogeneity continuously and non-destructively, with high spatiotemporal resolution. However,
69 while fluorescent probes can be used to measure mitochondrial membrane potential (Perry et al.,
70 2011) and the concentration of key metabolites (Imamura et al., 2009; Berg et al., 2009; Díaz-
71 García et al., 2017; Martin et al., 2014), it is not clear how to relate those observables to
72 mitochondrial metabolic fluxes.

73
74 NADH is an important cofactor that is involved in many metabolic pathways, including the TCA
75 and ETC in mitochondria. NADH binds with enzymes and acts as an electron carrier that
76 facilitates redox reactions. In the ETC, for example, NADH binds to complex I and donates its
77 electron to ubiquinone and ultimately to oxygen, becoming oxidized to NAD^+ . Endogenous
78 NADH has long been used to non-invasively probe cellular metabolism because NADH is
79 autofluorescent, while NAD^+ is not (Heikal, 2010). Fluorescence lifetime imaging microscopy
80 (FLIM) of NADH autofluorescence allows quantitative measurements of the concentration of
81 NADH, the fluorescence lifetimes of NADH, and the fraction of NADH molecules bound to
82 enzymes (Becker, 2012; Becker, 2019; Bird et al., 2005; Skala et al., 2007; Heikal, 2010; Sharick
83 et al., 2018; Sanchez et al., 2018; Sanchez et al., 2019; Ma et al., 2019). It has been observed that
84 the fraction of enzyme-bound NADH and NADH fluorescence lifetimes are correlated with the
85 activity of oxidative phosphorylation, indicating that there is a connection between NADH
86 enzyme-binding and mitochondrial metabolic fluxes (Bird et al., 2005; Skala et al., 2007). The
87 mechanistic basis of this empirical correlation has been unclear.

88
89 Here, we developed a generic coarse-grained NADH redox model that enables the inference of
90 ETC flux with subcellular resolution from FLIM measurements. We validated this model in
91 mouse oocytes and human tissue culture cells subject to a wide range of perturbations by

92 comparing predicted ETC fluxes from FLIM to direct measurements of oxygen consumption
93 rate, and by a self-consistency criterion. Using this method, we discovered that perturbing
94 nutrient supply and energy demand significantly impacts NADH metabolic state but does not
95 change ETC flux. We also discovered a subcellular spatial gradient of ETC flux in mouse
96 oocytes and found that this flux gradient is primarily due to a spatially heterogeneous
97 mitochondrial proton leak. We concluded from these observations that ETC flux in mouse
98 oocytes is not controlled by energy demand or supply, but by the intrinsic rates of mitochondrial
99 respiration. Thus, FLIM of NADH can be used to non-invasively and continuously measure
100 mitochondrial ETC fluxes with subcellular resolution and provides novel insights into
101 spatiotemporal regulation of metabolic fluxes in cells.
102

103 **Results**

104

105 **Quantifying response of mitochondrial metabolism to changing oxygen levels and** 106 **metabolic inhibitors using FLIM of NADH**

107

108 We used meiosis II arrested mouse oocytes as a model system. MII oocytes are in a metabolic
109 steady state, which eases interpretations of metabolic perturbations. ATP synthesis in mouse
110 oocytes occurs primarily through oxidative phosphorylation using pyruvate, without an
111 appreciable contribution from glycolysis (Houghton et al., 1996), providing an excellent system
112 to study mitochondrial metabolism. Mouse oocytes can be cultured *in vitro* using chemically
113 well-defined media (Biggers and Racowsky, 2002). In our work, we used AKSOM as the
114 culturing media (Summers, 2013). The oocytes can directly take up pyruvate supplied to them or
115 derive it from lactate through the activity of lactate dehydrogenase (LDH) (Lane and Gardner,
116 2000), and they can remain in a steady state for hours with constant metabolic fluxes. While
117 NADH and NADPH are difficult to distinguish with fluorescence measurements due to their
118 overlapping fluorescence spectrum, the concentration of NADH in mouse oocytes is 40 times
119 greater than the concentration of NADPH for the whole cell (Bustamante et al., 2017) and
120 potentially even greater in mitochondria (Zhao et al, 2011), so the autofluorescence signal from
121 these cells (particularly from mitochondria) can be safely assumed to result from NADH.
122

122

123 To investigate how FLIM measurements vary with mitochondrial activities, we performed
124 quantitative metabolic perturbations. We first continually varied the concentration of oxygen in
125 the media, from $50 \pm 2 \mu\text{M}$ to $0.26 \pm 0.04 \mu\text{M}$, over a course of 30 minutes while imaging NADH
126 autofluorescence of oocytes with FLIM (Figure 1a, top, black curve; Video 1). NADH is present
127 in both mitochondria and cytoplasm where it is involved in different metabolic pathways. To
128 specifically study the response of NADH in mitochondria, we used a machine-learning based
129 algorithm to segment mitochondria from the NADH intensity images (Berg et al., 2019)
130 (Appendix 1, Figure 1b and Figure 1-figure supplement 1). We verified the accuracy of the
131 segmentation with a mitochondrial labeling dye, MitoTracker Red FM, which showed a $80.6 \pm$
132 1.0% (SEM) accuracy of the segmentation (Appendix 1).
133

133

134 Using the segmentation mask, we obtained the intensity of NADH, I , in mitochondria by
135 averaging the photon count over all mitochondrial pixels. The intensity increased with
136 decreasing oxygen concentration (Figure 1a, top, red), as is readily seen from the raw images
137 (Figure 1a, middle). Restoring oxygen to its original level caused a recovery of NADH intensity,

138 indicating that the observed changes are reversible (Figure 1a; Video 1). These observations are
 139 consistent with the expectation that NADH concentration will increase at low oxygen levels due
 140 to oxygen's role as the electron acceptor in the ETC. In addition to intensity, FLIM can be used
 141 to determine the enzyme engagement of NADH by measuring the photon arrival time, from
 142 which fluorescence lifetimes can be fitted. Enzyme-bound NADH has a much longer
 143 fluorescence lifetime than free NADH (Sharick et al., 2018), allowing bound and free NADH to
 144 be separately resolved, but the precise fluorescence lifetimes of NADH depend on a range of
 145 factors, including viscosity, pH, and the identity of the enzyme NADH binds to (Sharick et al.,
 146 2018, Ghukasyan and Heikal, 2015). To fit NADH fluorescence lifetimes, we grouped all
 147 detected photons from mitochondria to form histograms of photon arrival times from NADH
 148 autofluorescence for each time point (Figure 1a. lower). We fitted the histograms using a model
 149 in which the NADH fluorescence decay, $F(\tau)$, is described by the sum of two exponentials,

$$151 \quad F(\tau) = f \cdot \exp\left(-\frac{\tau}{\tau_l}\right) + (1 - f) \cdot \exp\left(-\frac{\tau}{\tau_s}\right), \quad (1)$$

152
 153 where τ_l and τ_s are long and short fluorescence lifetimes, corresponding to enzyme-bound
 154 NADH and free NADH, respectively, and f is the fraction of enzyme-bound NADH (Sanchez et
 155 al., 2018; Sanchez et al., 2019) (Methods).

156
 157 We repeated the oxygen drop experiments for a total of 68 oocytes. Since the oxygen drop is
 158 much slower than the NADH redox reactions (30 minutes compared to timescale of seconds), the
 159 oxygen perturbation can be safely assumed to be quasistatic, allowing the FLIM measurements
 160 to be determined as a function of oxygen levels. We averaged data from all oocytes to obtain a
 161 total of four FLIM parameters: mitochondrial NADH intensity, I , long and short fluorescence
 162 lifetimes, τ_l and τ_s , and the fraction of enzyme-bound NADH, f . We determined how these
 163 parameters varied with oxygen level (Figure 1a and c). All parameters are insensitive to oxygen
 164 level until oxygen drops below $\sim 10 \mu\text{M}$. This observation is consistent with previous studies that
 165 showed mitochondria have a very high apparent affinity for oxygen (Chance et al., 1955,
 166 Gnaiger et al., 1998).

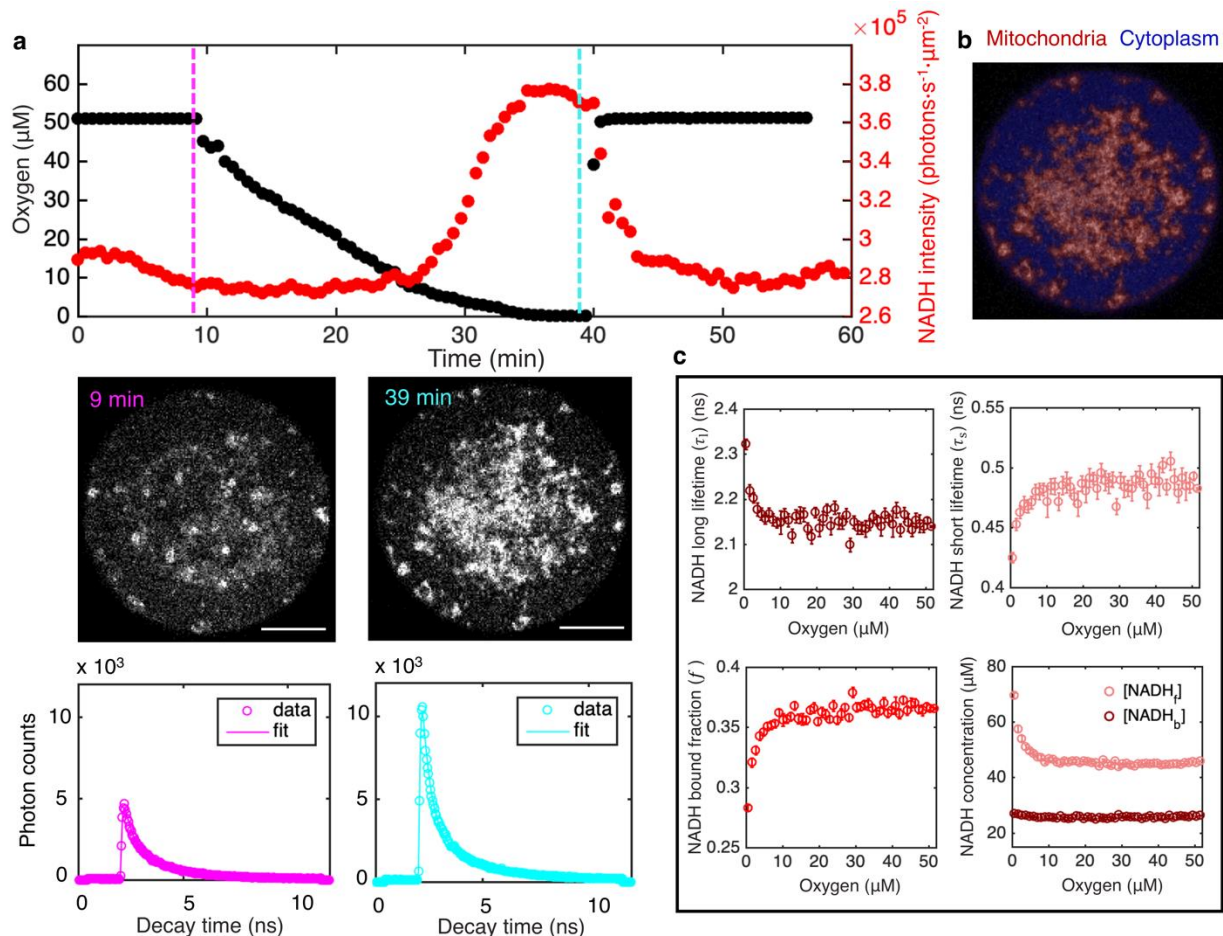
167
 168 We next explored the relationship between the measured FLIM parameters and the concentration
 169 of NADH. Since bound and free NADH have different fluorescence lifetimes, and hence
 170 different molecular brightnesses, the NADH concentration is not generally proportional to
 171 NADH intensity. Assuming molecular brightness is proportional to fluorescence lifetime
 172 (Lakowicz, 2006), we derived a relation between NADH intensity, fluorescence lifetimes, and
 173 concentrations as

$$175 \quad [\text{NADH}_f] = \frac{I(1-f)}{c_s[(\tau_l - \tau_s)f + \tau_s]}, \quad (2a)$$

$$176 \quad [\text{NADH}_b] = [\text{NADH}_f] \frac{f}{1-f}, \quad (2b)$$

177
 178 where c_s is a calibration factor that relates intensities and concentrations (see Appendix 1). We
 179 measured the calibration factor by titrating free NADH *in vitro* and acquiring FLIM data (Figure
 180 1-figure supplement 2, equation (S4)). To test the validity of this approach, we used Equations 2a
 181 and 2b to measure concentrations of free and bound NADH in solutions with different

182 concentrations of purified lactate dehydrogenase (LDH), an enzyme to which NADH can bind.
 183 The measured NADH bound concentration increases with LDH concentration while the sum of
 184 free and bound NADH concentration remains a constant and equal to the amount of NADH
 185 added to the solution. This result demonstrates that Equations 2a and 2b can be used to measure
 186 free and bound NADH concentrations from NADH intensity and lifetimes. It is well established
 187 that FLIM can be used to distinguish bound and free NADH *in vivo* based on the large change of
 188 fluorescence lifetime when NADH binds to enzymes (Skala et al., 2007; Heikal, 2010). Even
 189 though the exact amount that the lifetime changes depends on the specific enzyme NADH binds
 190 to (Sharick et al., 2018), enzyme-bound NADH always has a much longer fluorescence lifetime
 191 than free NADH. Therefore, the method to calculate free and bound concentrations of NADH
 192 from FLIM measurements is expected to hold *in vivo*. We next used this method to study NADH
 193 in mitochondria in oocytes. We applied Equations 2a and 2b to our FLIM data from oocytes and
 194 determined how the concentrations of free NADH, $[NADH_f]$, and enzyme-bound NADH,
 195 $[NADH_b]$, depended on oxygen level (Figure 1c, lower right). Interestingly, $[NADH_f]$ increased
 196 as oxygen fell below $\sim 10 \mu\text{M}$, while $[NADH_b]$ did not vary with oxygen level.
 197

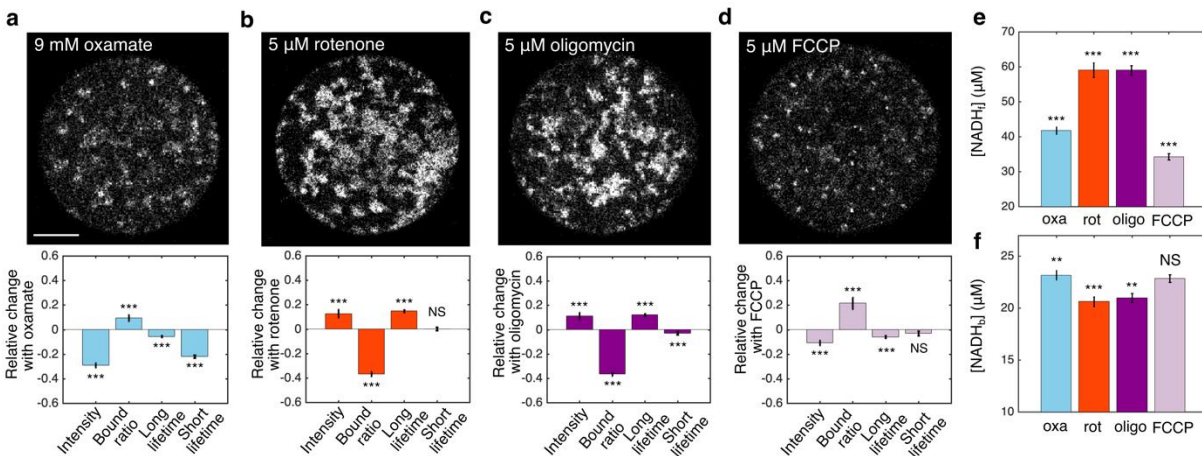


198
 199 **Figure 1 | FLIM measurements of the response of mitochondrial NADH as a function of oxygen level.** a, Top
 200 row: oxygen level (black circles) and mitochondrial NADH intensity (red circles) as a function of time. Middle row:
 201 NADH intensity images of MII mouse oocyte at high and low oxygen levels corresponding to times indicated by the
 202 vertical lines. Scale bar, $20 \mu\text{m}$. Bottom row: NADH fluorescence decay curves of the corresponding oocyte at low
 203 and high oxygen levels, with corresponding fits. b, NADH-intensity-based segmentation of mitochondria and

204 cytoplasm. c, Mitochondrial NADH long fluorescence lifetime τ_l (upper left), short fluorescence lifetime τ_s (upper
 205 right), and bound fraction f (lower left) as a function of oxygen level (n=68 oocytes). These FLIM parameters can
 206 be used in combination with intensity, I , and proper calibration, to obtain the concentration of free NADH,
 207 $[NADH_f]$, and the concentration of enzyme-bound NADH, $[NADH_b]$, in mitochondria as a function of oxygen
 208 (lower right). Error bars are standard error of the mean (s.e.m) across individual oocytes.

209 **Video 1 | NADH intensity in mouse oocyte as a function of oxygen level. Left: Imaging of NADH from**
 210 **autofluorescence of mouse oocyte. Right: Real time measurement of oxygen level in the imaging chamber.**
 211

212 We next explored the impact of metabolic inhibitors on mitochondrial NADH. We first inhibited
 213 lactate dehydrogenase (LDH) by adding 9 mM of oxamate to the AKSOM media. This led to a
 214 decrease of NADH intensity in the mitochondria (Figure 2a upper) and significant changes in all
 215 FLIM parameters (Figure 2a lower, $p < 0.001$). We next inhibited complex I of the ETC using 5
 216 μM of rotenone (in the presence of 9 mM of oxamate, to reduce cytoplasmic NADH signal for
 217 better mitochondrial segmentation). This resulted in a dramatic increase of NADH intensity in
 218 the mitochondria (Figure 2b upper) and significant changes in NADH bound ratio and long
 219 lifetime (Figure 2b lower, $p < 0.001$). Then we inhibited ATP synthase with 5 μM of oligomycin
 220 (in the presence of 9 mM of oxamate), which, similar to rotenone, resulted in an increase of
 221 mitochondrial NADH intensity (Figure 2c upper) and significant changes in all FLIM parameters
 222 (Figure 2c lower, $p < 0.001$). Finally, we subjected the oocytes to 5 μM of FCCP (in the presence
 223 of 9 mM of oxamate), which uncouples proton translocation from ATP synthesis, and observed a
 224 decrease of mitochondrial NADH intensity (Figure 2d upper) and significant changes in FLIM
 225 parameters (Figure 2d lower, $p < 0.001$). Interestingly, the direction of change of FLIM
 226 parameters under FCCP is opposite to those under rotenone and oligomycin. For each of these
 227 conditions, we used Equations 2a and 2b to calculate the concentrations of free NADH,
 228 $[NADH_f]$, (Figure 2e) and bound NADH, $[NADH_b]$, (Figure 2f) from the measured intensity and
 229 FLIM parameters. While rotenone and oligomycin significantly increased $[NADH_f]$ and
 230 decreased $[NADH_b]$, FCCP decreased $[NADH_f]$. It remains unclear how to relate these changes
 231 of the free and bound concentrations of NADH to the activities of mitochondrial respiration.
 232



233 **Figure 2 | FLIM measurements of mitochondrial NADH under the impact of metabolic inhibitors. a-d:** NADH
 234 intensity images (Scale bar, 20 μm) and the corresponding changes of FLIM parameters in response to 9 mM
 235 oxamate (a) (n=28), and with an additional 5 μM rotenone (b) (n=28), 5 μM oligomycin (c) (n=37) and 5 μM FCCP
 236 (d) (n=31) perturbations. n is the number of oocytes. 15-30 minutes have elapsed between the administration of the
 237 drugs and the measurements. e: free NADH concentrations ($[NADH_f]$). f: bound NADH concentrations ($[NADH_b]$).
 238
 239

270 Error bars represent standard error of the mean (s.e.m) across different oocytes. Student's t-test is performed
 271 between parameters before and after the perturbation. *p<0.05, **p<0.01, ***p<0.001.

272

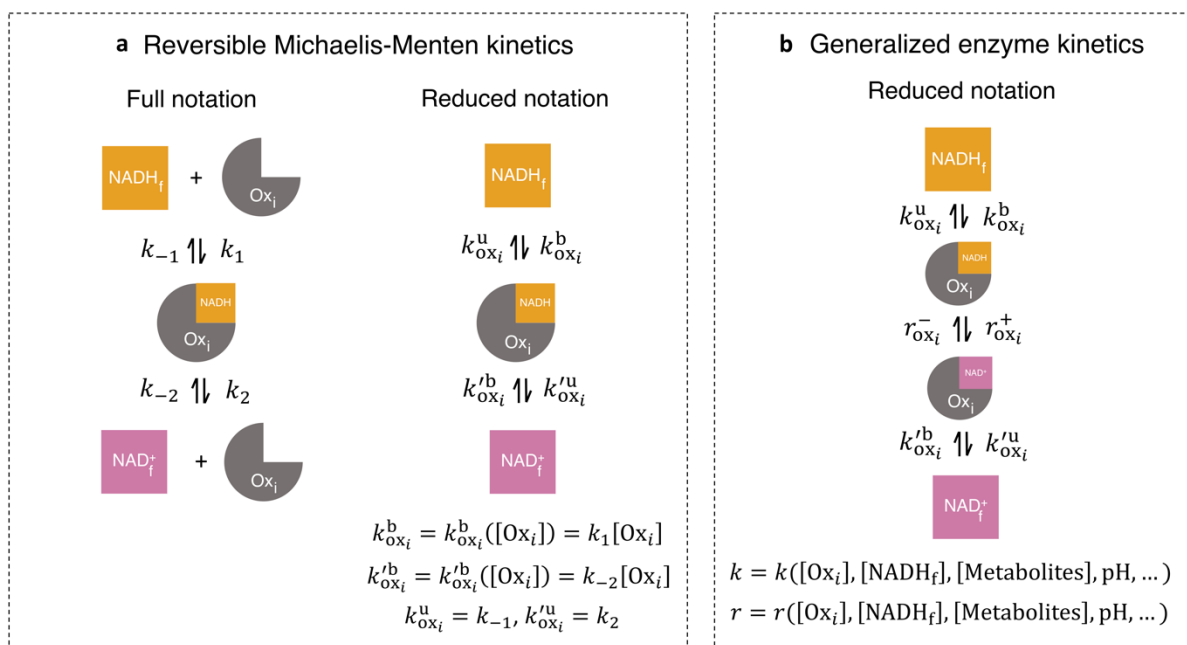
273 **Figure 2-source data | Excel spreadsheet of single oocyte FLIM data used for Figure 2a-f.**

274

275 **Developing a coarse-grained NADH redox model to relate FLIM measurements of NADH**
 276 **to activities of mitochondrial metabolic pathways**

277

278 We next developed a mathematical model of NADH redox reactions to relate these quantitative
 279 FLIM measurements to activities of mitochondrial metabolic pathways. NADH is a central
 280 coenzyme that binds to enzymes and facilitates redox reactions by acting as an electron carrier.
 281 There are two categories of enzymes associated with NADH redox reactions, which together
 282 form a redox cycle: oxidases that oxidize NADH to NAD⁺ and reductases that reduce NAD⁺ to
 283 NADH. The major NADH oxidase in mitochondria is complex I of ETC for mammalian cells.
 284 There are many NADH reductases in mitochondria because NADH can be reduced through
 285 different pathways depending on the energy substrate. These pathways include the TCA cycle,
 286 fatty acid catabolism via beta oxidation, amino acid catabolism such as glutaminolysis and the
 287 malate-aspartate shuttle (Salway 2017). A comprehensive NADH redox model will include all
 288 the oxidases and reductases. For generality, we consider N oxidases and M reductases.



289 **Figure 3 / Generalized enzyme kinetics with reduced notation. a, (left) full notation for reversible Michaelis-Menten kinetics. (right) a mathematically equivalent reduced notation, in which the free enzyme concentration, [Ox_i], is incorporated into the binding rates. b, Generalized enzyme kinetics where all kinetic rates are general functions of enzyme and metabolite concentrations and other factors.**

290 For convenience, we introduced a reduced notation to describe models of the enzyme kinetics of
 291 these oxidases and reductases. We began by illustrating our reduced notation using reversible
 292 Michaelis-Menten kinetics as an example (Keleti, 1986; Miller and Alberty; 1958; Smith,
 293 1992). The conventional, full notation for these kinetics (Figure 3a, left) explicitly displays all
 294 chemical species that are modeled in this reaction scheme – free NADH, NADH_f, free enzyme,
 295 Ox_i, free NAD⁺, NAD_f⁺, and NADH bound to the enzyme – as well as the forward and reverse
 296

297 reaction rates $-k_{-1}$, k_1 , k_{-2} , and k_2 . Our reduced notation for reversible Michaelis-Menten
 298 kinetics (Figure 3a, right) is an alternative way of representing the same mathematical model. In
 299 this reduced notation, only free NADH, free NAD^+ , and NADH bound to the enzyme are
 300 explicitly shown, while the free enzyme concentration is only represented as entering through the
 301 effective binding rates $k_{\text{ox}_i}^b$ and $k_{\text{ox}_i}^u$. The conventional, full notation and the reduced notation are
 302 alternative ways of representing the same mathematical model, but the reduced notation is
 303 convenient to use in the derivation that follows (see Appendix 2).

304
 305 We next introduced a generalized enzyme kinetics using our reduced notation (Figure 3b), which
 306 contains not only free NADH, free NAD^+ , and NADH bound to the enzyme, but also NAD^+
 307 bound to the enzyme, and the reaction rates for oxidation and reduction of the bound coenzymes.
 308 In this reduced notation, all the binding and unbinding rates, and the reaction rates, can be
 309 functions of metabolite concentrations, protein concentrations, and other factors such as pH and
 310 membrane potential. As in the reversible Michaelis-Menten kinetics example, these rates can
 311 depend on the concentration of the free enzyme itself. This dependency on free enzyme
 312 concentration can be non-linear, as could occur if the enzyme oligomerizes. Furthermore, the
 313 rates may depend on the concentration of free NADH, free NAD^+ , and the enzyme complexes.
 314 Thus, while the reduced notation for the generalized enzyme might appear to describe a first
 315 order reaction, it can actually be used to represent reactions of any order, with arbitrary, non-
 316 linear dependencies on the concentration of the enzyme itself, as well as arbitrary, non-linear
 317 dependencies on other factors. In order to model the dynamics of enzymes described by such
 318 generalized kinetics, it is necessary to specify the functional form of all the rates, as well as
 319 specify mathematical models for all the variables that enter these rates (i.e. free enzyme
 320 concentration, membrane potential, pH, etc.) (Appendix 2). However, in what follows, we will
 321 derive results that hold true, irrespective of the functional form of the rates or the presence of
 322 additional, implicit variables. Thus, remarkably, these quantitative predictions are valid for
 323 enzyme kinetics of any order, with arbitrary nonlinearities in the rates.

324
 325 To begin our derivation, we note that under this generalized enzyme kinetics (Figure 3b), the net
 326 flux through the i th oxidase at steady-state is:

$$327 \quad J_{\text{ox}_i} \equiv r_{\text{ox}_i}^+ [\text{NADH} \cdot \text{Ox}_i] - r_{\text{ox}_i}^- [\text{NAD}^+ \cdot \text{Ox}_i] = k_{\text{ox}_i}^b [\text{NADH}_f] - k_{\text{ox}_i}^u [\text{NADH} \cdot \text{Ox}_i] \quad (3),$$

328
 329 where $[\text{NADH} \cdot \text{Ox}_i]$, $[\text{NAD}^+ \cdot \text{Ox}_i]$, $[\text{NADH}_f]$ are the concentrations of the i th oxidase-bound
 330 NADH, NAD^+ and free NADH, respectively. $r_{\text{ox}_i}^+$, $r_{\text{ox}_i}^-$ are the forward and reverse oxidation
 331 rates. $k_{\text{ox}_i}^b$, $k_{\text{ox}_i}^u$ are the binding and unbinding rates. The second equality in equation (3) results
 332 from the steady state condition, where the net binding and unbinding flux equals the net
 333 oxidation flux.
 334

335
 336 We next considered a redox cycle between NADH and NAD^+ with multiple oxidases and
 337 reductases. To account for all possible NADH redox pathways, we developed a detailed NADH
 338 redox model with N oxidases and M reductases described by the generalized enzyme kinetics
 339 (Figure 4a and Figure 4-figure supplement 1). In this model, NADH and NAD^+ can bind and
 340 unbind to each oxidase and reductase. Once bound, NADH can be reversibly oxidized to NAD^+
 341 by the oxidases, and NAD^+ can be reversibly reduced to NADH by the reductases, forming a
 342 redox cycle. The functional dependencies of the binding and unbinding rates, and the reaction

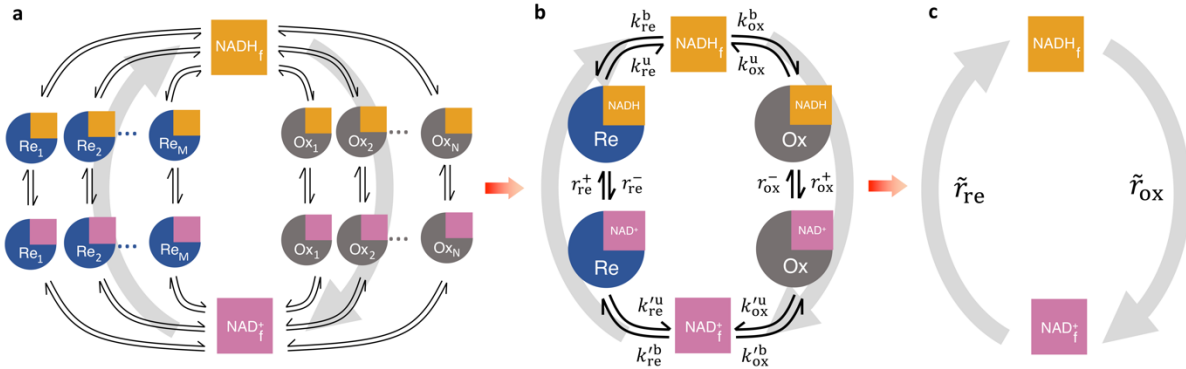
343 rates, can be different for each oxidase and reductase, and each of these rates can be nonlinear
 344 functions of free enzyme concentrations, NADH concentration, and other factors such as pH and
 345 membrane potential. Modeling the dynamics of this redox cycle requires specifying the precise
 346 number of oxidases and reductases, the functional forms of the rates, and mathematical models
 347 for all the variables the rates implicitly depend on. However, we will show that quantitative
 348 predictions regarding the interpretation of FLIM measurements can be made that generally hold,
 349 independent of these modeling choices.

350
 351 FLIM cannot resolve the association of NADH with individual enzymes in cells, but rather,
 352 provides quantitative information on the global states of bound and free NADH. Thus, to
 353 facilitate comparison to FLIM experiments, we coarse-grained the detailed redox model by
 354 mapping all N oxidases into a single effective oxidase and all M reductases into a single effective
 355 reductase (Figure 4b and Appendix 3). This coarse-graining is mathematically exact and involves
 356 no approximations or assumptions.

357
 358 In the coarse-grained redox model, NADH can be bound to the effective oxidase, $\text{NADH} \cdot \text{Ox}$,
 359 bound to the effective reductase, $\text{NADH} \cdot \text{Re}$, or can be free, NADH_f . Hence, the concentration of
 360 NADH bound to all enzymes is, $[\text{NADH}_b] = [\text{NADH} \cdot \text{Ox}] + [\text{NADH} \cdot \text{Re}]$, and the total
 361 concentration of NADH is, $[\text{NADH}] = [\text{NADH}_b] + [\text{NADH}_f]$. The kinetics of the effective
 362 oxidase and reductase are represented by the coarse-grained forward, r_{ox}^+ , and reverse, r_{ox}^- ,
 363 oxidation rates, and the forward, r_{re}^+ , and reverse, r_{re}^- , reduction rates. The global flux through all
 364 the oxidases in the detailed redox model equals the global flux through the coarse-grained
 365 oxidase, which at steady-state is:

$$366 \quad J_{\text{ox}} \equiv \sum_{i=1}^N J_{\text{ox}_i} = r_{\text{ox}}^+ [\text{NADH} \cdot \text{Ox}] - r_{\text{ox}}^- [\text{NAD}^+ \cdot \text{Ox}] = k_{\text{ox}}^b [\text{NADH}_f] - k_{\text{ox}}^u [\text{NADH} \cdot \text{Ox}] \quad (4),$$

367
 368 Where k_{ox}^b is the rate that free NADH binds the effective oxidase, k_{ox}^u is the rate that NADH
 369 unbinds the effective oxidase, and the last equality results because the coarse-grained redox loop
 370 is a linear pathway so the global oxidative flux must equal the global binding and unbinding flux
 371 at steady-state. The conservation of global flux explicitly relates the effective binding and
 372 unbinding rates and the reaction rates of the coarse-grained model to those of the detailed model
 373 (Appendix 3, Figure 4-figure supplement 1). The binding and unbinding kinetics of NADH and
 374 NAD^+ to the effective oxidase and reductase are described by eight coarse-grained binding and
 375 unbinding rates (Figure 4b). The coarse-grained reaction rates and binding and unbinding rates
 376 can be arbitrary functions of metabolite concentrations, enzyme concentrations, and other factors
 377 (i.e. pH, membrane potential, etc.). These effective rates can even be functions of $[\text{NADH}_f]$,
 378 $[\text{NAD}_f^+]$, and the concentration of other variables, and thus can include reactions of arbitrary
 379 order. Hence this coarse-grained model is a generic model of NADH redox reactions. Fully
 380 specifying this model would require explicitly choosing the functional form of all the rates and
 381 incorporating additional equations to describe the dynamics of all the implicit variables that the
 382 rates depend on (Appendix 2). We next demonstrate that quantitative predictions regarding the
 383 interpretation of FLIM measurements of NADH can be made that are valid irrespective of the
 384 form of the rates or the presence of implicit variables.



386
 387 **Figure 4 | Coarse-graining the NADH redox model.** **a**, Schematic of the detailed NADH redox model. We
 388 consider all possible NADH redox pathways by modeling N oxidases (Ox) and M reductases (Re). Free NADH,
 389 NADH_f , and free NAD^+ , NAD_f^+ , can bind and unbind with each oxidase and reductase. Once bound, NADH can be
 390 oxidized reversibly to NAD^+ by the oxidases, and NAD^+ can be reduced reversibly to NADH by the reductases,
 391 forming a redox cycle. Grey arrows represent the total fluxes through all oxidases and reductases of the redox cycle.
 392 **b**, Coarse-grained NADH redox model. All oxidases and reductases are coarse-grained into a single effective
 393 oxidase and reductase, respectively. r_{ox}^+ and r_{ox}^- are the coarse-grained forward and reverse oxidation rates of the
 394 oxidase; r_{re}^+ and r_{re}^- are the coarse-grained forward and reverse reduction rates of the reductase. $k_{\text{ox}}^b, k_{\text{ox}}^u, k_{\text{re}}^b, k_{\text{re}}^u$
 395 and $k_{\text{ox}}^b, k_{\text{ox}}^u, k_{\text{re}}^b, k_{\text{re}}^u$ are the coarse-grained binding and unbinding rates of NADH and NAD^+ , respectively, to the
 396 oxidase and reductase. **c**, At steady state, all the kinetics of the model can be further coarse-grained into the turnover
 397 rate of free NADH, \tilde{r}_{ox} , and the turnover rate of free NAD^+ , \tilde{r}_{re} , characterizing the two branches of the cycle.
 398

399 Accurately predicting ETC flux from FLIM of NADH using the NADH redox model

400
 401 At steady-state, the model can be further coarse-grained, without approximation, to consider only
 402 free NADH, with a turnover rate of \tilde{r}_{ox} , and free NAD^+ , with a turnover rate of \tilde{r}_{re} (Figure 4c).
 403 Our key prediction is that the steady-state global oxidative flux of NADH is (Appendix 4):
 404

$$405 \quad J_{\text{ox}} = k_{\text{ox}}^b[\text{NADH}_f] - k_{\text{ox}}^u[\text{NADH} \cdot \text{Ox}] = \tilde{r}_{\text{ox}}[\text{NADH}_f], \quad (5a)$$

406 where

$$407 \quad \tilde{r}_{\text{ox}} = \alpha(\beta - \beta_{\text{eq}}), \quad (5b)$$

408 and

$$409 \quad \beta = f/(1 - f). \quad (5c)$$

410
 411 This prediction results from the steady state assumption where the net binding and unbinding
 412 flux of NADH from the oxidase balances the net oxidative flux through the oxidase (Equation
 413 (4) and Appendix 4). The turnover rate of free NADH, \tilde{r}_{ox} , is proportional to the difference
 414 between the NADH bound ratio β , i.e. the ratio between bound and free NADH concentrations,
 415 and the equilibrium NADH bound ratio, β_{eq} (i.e. what the bound ratio would be if the global
 416 oxidative flux is zero). β_{eq} and the prefactor α are independent of the reaction rates of the
 417 oxidase and reductase and can be explicitly related to the binding and unbinding rates of the
 418 coarse-grained model (Appendix 4, equation S43 and S45).
 419
 420

421 In mitochondria, the major NADH oxidation pathway is the ETC. Thus, Equations 5a-c predict
 422 that there is a direct connection between quantities that can be measured by FLIM of NADH in

423 mitochondria (i.e. β and $[\text{NADH}_f]$) and the flux through the ETC (i.e. J_{ox}). Equations 5a-c
424 suggests a procedure for using FLIM to infer flux through the ETC: if a condition can be found
425 under which there is no net flux through the ETC, then β_{eq} can be measured with FLIM. Once
426 β_{eq} is known, then subsequent FLIM measurements of β allows \tilde{r}_{ox} , and hence J_{ox} , to be inferred
427 (up to a constant of proportionality α) (Appendix 5).

428
429 Equations 5a-c are valid irrespective of the functional forms of the rate laws, which may have
430 nonlinear dependencies on metabolite concentrations, enzyme concentrations, and other factors.
431 While equation 5a seems to imply first order kinetics in $[\text{NADH}_f]$, the rates can also be arbitrary
432 functions of $[\text{NADH}_f]$, so Equations 5a-c hold for kinetics of any order. Equations 5a-c are also
433 applicable if the rates depend on additional variables that have their own dynamical equations (as
434 long as the system is at steady-state): as an example, Appendix 9 shows that Equations 5a-c
435 result when the N oxidases and M reductases are each described by reversible Michaelis-Menten
436 kinetics, a model in which the rates depend on the concentration of free enzymes (which is a
437 dynamical variable). More generally, if detailed biophysical models of the NADH oxidases are
438 available, then parameters of these models can be explicitly mapped to the coarse-grained
439 parameters of the NADH redox model. Appendix 9 and Table 1 contain mappings between the
440 coarse-grained model and a number of previously proposed detailed biophysical models of
441 NADH oxidation in the ETC (Beard, 2005; Korzeniewski and Zoladz, 2001; Hill, 1977; Jin and
442 Bethke 2002; Chang et al., 2011). However, since Equations 5a-c are valid for a broad set of
443 models, they can be used for flux inference without the need to specify the functional form of the
444 rates or the variables they depend on. This is because the rates are coarse-grained into two
445 effective parameters α and β_{eq} , which can be experimentally determined. This generality results
446 from the steady state assumption and the topology of the reactions resulting in the net binding
447 and unbinding flux of NADH from the oxidase balancing the net oxidative flux. Thus, Equations
448 5a-c provide a general procedure to infer the ETC flux from FLIM measurements of NADH in
449 mitochondria.

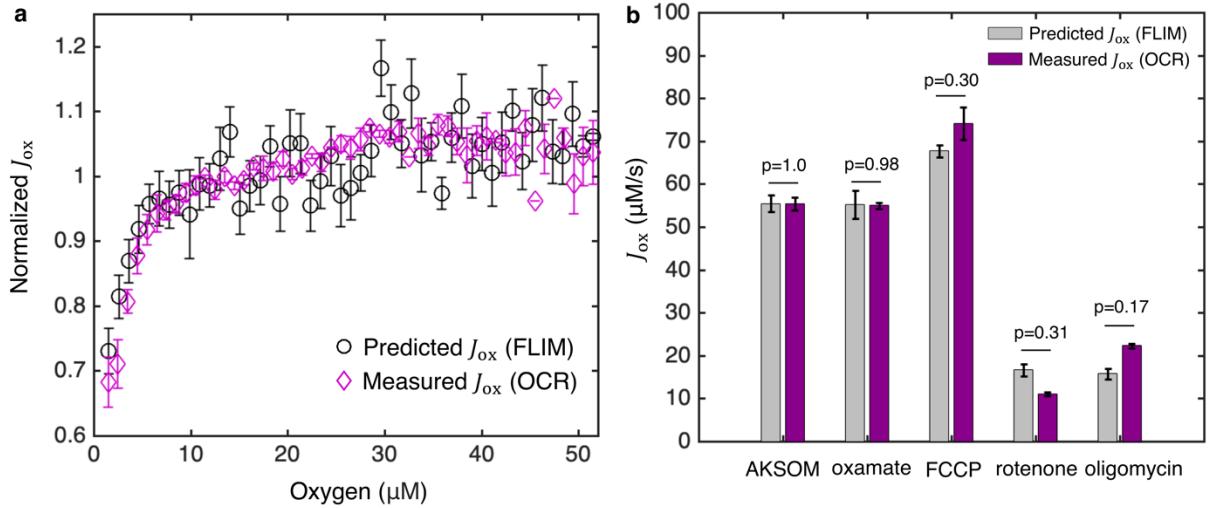
450
451 We applied this procedure to analyze our oxygen drop experiments (Figure 1) by assuming that
452 there was no net flux through the ETC at the lowest oxygen level achieved for each oocyte
453 (implying that the measured value of β at that oxygen concentration corresponds to β_{eq} for that
454 oocyte). We also assumed that α and β_{eq} do not change with oxygen levels, which is reasonable
455 since, as noted above, they are independent of the reaction rates of the oxidase and reductase.
456 The measured value of β_{eq} allowed us to obtain a prediction for J_{ox} as a function of oxygen
457 concentration for the oocytes (Figure 5a). To test these predictions, we directly determined J_{ox} as
458 a function of oxygen concentration by measuring the oxygen consumption rate (OCR) of the
459 oocytes using a nanorespirometer (Lopes et al., 2005) (Methods). The direct measurements of J_{ox}
460 from OCR quantitatively agree with the predictions of J_{ox} from FLIM for all oxygen
461 concentrations (Figure 5a), strongly arguing for the validity of the model and the inference
462 procedure. This agreement supports the assumption that α and β_{eq} are independent of oxygen
463 levels.

464
465 So far we have inferred the ETC flux up to a constant of proportionality α , allowing the relative
466 changes of ETC flux to be inferred from FLIM of NADH. α cannot be determined by FLIM
467 alone. If an absolute measurement of the ETC flux can be obtained at one condition, then α can

468 be calibrated to predict absolute ETC fluxes for other conditions. OCR measurement provides a
469 means to calibrate α (Appendix 5, Equation (S48)). We used oocytes cultured in AKSOM media
470 at $50 \pm 2 \mu\text{M}$ oxygen as a reference state, which, from our OCR measurements yielded $J_{\text{ox}} =$
471 $56.6 \pm 2.0 \mu\text{M} \cdot \text{s}^{-1}$ (SEM) and hence a constant of proportionality of $\alpha = 5.4 \pm 0.2 \text{ s}^{-1}$. Using
472 this value of α , we can predict absolute values of J_{ox} under various perturbations assuming α
473 remains a constant. We note that J_{ox} is a flux density with units of concentration per second, an
474 intensive quantity that does not depend on the mitochondrial volume. Multiplying J_{ox} by the
475 volume of mitochondria in an oocyte gives the total ETC flux, proportional to oxygen
476 consumption rate, in that oocyte. In all subsequent discussions, ETC flux refers to flux density
477 unless otherwise noted.

478
479 We next applied the inference procedure and a constant of $\alpha = 5.4 \pm 0.2 \text{ s}^{-1}$ to analyze the
480 experiments of oxamate, FCCP, rotenone and oligomycin perturbations (Figure 2). We dropped
481 oxygen levels to determine β_{eq} in the presence of oxamate (Figure 5-figure supplement 1h) and
482 applied Equations 5a-c to infer the impact of oxamate on J_{ox} at $50 \mu\text{M}$ oxygen (i.e. control levels
483 of oxygen). Surprisingly, while the addition of oxamate greatly impacts FLIM parameters,
484 including a $29\% \pm 2\%$ (SEM) decrease in intensity and a $10\% \pm 3\%$ increase in bound ratio
485 (Figure 2a), this procedure revealed that the predicted ETC flux with oxamate ($J_{\text{ox}} = 55.2 \pm$
486 $3.2 \mu\text{M} \cdot \text{s}^{-1}$) is the same as that without oxamate ($J_{\text{ox}} = 55.4 \pm 1.9 \mu\text{M} \cdot \text{s}^{-1}$) (Figure 5b; $p =$
487 0.95), which was confirmed by direct measurements of oocytes' OCR that yielded $J_{\text{ox}} = 55.4 \pm$
488 $1.5 \mu\text{M} \cdot \text{s}^{-1}$ and $J_{\text{ox}} = 54.9 \pm 0.7 \mu\text{M} \cdot \text{s}^{-1}$ before and after the addition of oxamate, respectively
489 (Figure 5b; $p = 0.85$). We next analyzed the FCCP experiment. We obtained β_{eq} by dropping
490 oxygen in the presence of FCCP (Figure 5-figure supplement 1h) and applied equations 5a-c to
491 infer the impact of FCCP on J_{ox} at $50 \mu\text{M}$ oxygen. We predicted that FCCP increased the flux to
492 $J_{\text{ox}} = 67.7 \pm 1.5 \mu\text{M} \cdot \text{s}^{-1}$, which was confirmed by the directly measured $J_{\text{ox}} = 74.0 \pm$
493 $3.7 \mu\text{M} \cdot \text{s}^{-1}$ from OCR (Figure 5b; $p = 0.30$). Following the same FLIM based inference
494 procedures, we predicted that the addition of rotenone and oligomycin reduced the fluxes to
495 $J_{\text{ox}} = 16.7 \pm 1.4 \mu\text{M} \cdot \text{s}^{-1}$ and $J_{\text{ox}} = 15.7 \pm 1.3 \mu\text{M} \cdot \text{s}^{-1}$, respectively, which was again
496 confirmed by corresponding direct measurements of OCR that yielded $J_{\text{ox}} = 11.1 \pm$
497 $0.4 \mu\text{M} \cdot \text{s}^{-1}$ and $J_{\text{ox}} = 22.3 \pm 0.6 \mu\text{M} \cdot \text{s}^{-1}$ (Figure 5b; $p=0.31$ and $p=0.17$). The quantitative
498 agreement between predicted fluxes from FLIM and directly measured fluxes from OCR under a
499 variety of conditions (i.e. varying oxygen tension, sodium oxamate, FCCP, rotenone and
500 oligomycin), demonstrates that Equations 5a-c can be successfully used to infer flux through the
501 ETC in mouse oocytes. This agreement also supports the assumption that α is a constant across
502 these different perturbations.

503



504
505 **Figure 5 | Coarse-grained NADH redox model enables accurate prediction of flux through the ETC from**
506 **FLIM measurements of NADH. a,** Predicted flux through the ETC, J_{ox} , from the FLIM of NADH ($n=68$ oocytes)
507 agrees quantitatively with J_{ox} from oxygen consumption rate (OCR) measurements ($N=3$ measurements) for all
508 oxygen concentrations. J_{ox} is normalized by its value at $50 \mu\text{M}$ oxygen. **b,** Predicted J_{ox} from FLIM and measured
509 J_{ox} from OCR for AKSOM ($n=68$, $N=4$) and with perturbations of 9 mM oxamate ($n=20$, $N=2$), $5 \mu\text{M}$ FCCP ($n=31$,
510 $N=2$), $5 \mu\text{M}$ rotenone ($n=28$, $N=2$) and $5 \mu\text{M}$ oligomycin ($n=37$, $N=3$). Predicted J_{ox} agrees with measured J_{ox} in all
511 cases. n denotes number of oocytes for single oocyte FLIM measurements. N denotes number of replicates for batch
512 oocytes OCR measurements. Each batch contains 10-15 oocytes. P values are calculated from two-sided two-sample
513 t-test. Error bars denote standard error of the mean across individual oocytes for FLIM measurements and across
514 batches of oocytes for OCR measurements.
515

516 **Figure 5-source data | Excel spreadsheet of single oocyte FLIM data and batch OCR data used for Figure 5b.**
517

518 The work described above used the relation $\tilde{r}_{ox} = \alpha(\beta - \beta_{eq})$ to predict the flux through the
519 ETC from FLIM measurements. We next show that the model also predicts a relationship
520 between \tilde{r}_{ox} and the fluorescence lifetime of enzyme-bound NADH, τ_1 , in mitochondria. This
521 provides a second means to use the model to infer \tilde{r}_{ox} , and hence J_{ox} , from FLIM of NADH.
522 Specifically, we assumed that NADH bound to the oxidases have a different average lifetime,
523 τ_{ox} , than NADH bound to the reductases, τ_{re} , which is reasonable because NADH bound to
524 different enzymes do exhibit different fluorescence lifetimes (Sharick et al., 2018). This
525 assumption implies that the experimentally measured long lifetime of NADH in mitochondria, τ_1 ,
526 is a weighted sum of these two lifetimes,
527

$$528 \quad \tau_1 = \tau_{ox} \frac{[\text{NADH}\cdot\text{Ox}]}{[\text{NADH}\cdot\text{Ox}] + [\text{NADH}\cdot\text{Re}]} + \tau_{re} \frac{[\text{NADH}\cdot\text{Re}]}{[\text{NADH}\cdot\text{Ox}] + [\text{NADH}\cdot\text{Re}]} \quad (6).$$

529
530 Using the coarse-grained NADH redox model at steady-state, Equation (6) leads to a non-trivial
531 prediction that τ_1 is linearly related to $1/\beta$ (Appendix 5):
532

$$533 \quad \tau_1 = A \frac{1}{\beta} + B \quad (7),$$

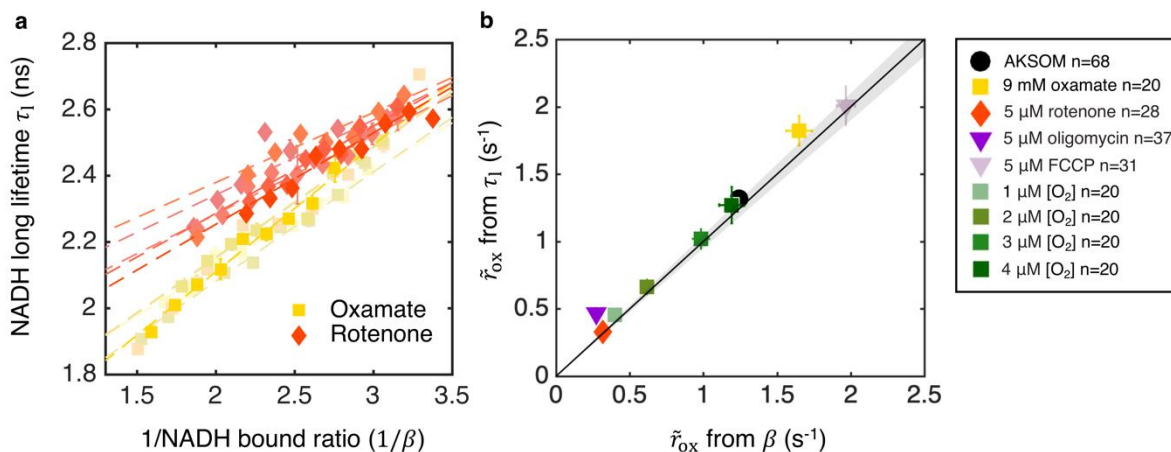
534
535 where the slope A and offset B can be explicitly related to τ_{ox} , τ_{re} , and the coarse-grained
536 binding and unbinding rates. Such a linear relationship is indeed observed in individual oocytes

537 subject to oxygen drops (Figure 6a and Figure 6-figure supplement 1), supporting the
 538 assumptions of the model. Combining Equations (7) and (5b) leads to a predicted relationship
 539 between \tilde{r}_{ox} and NADH long fluorescence lifetime (Appendix 5):
 540

$$541 \quad \tilde{r}_{\text{ox}} = \alpha \frac{A}{\tau_{\text{eq}} - B} \left(\frac{\tau_{\text{eq}} - \tau_1}{\tau_1 - B} \right) \quad (8),$$

542
 543 where τ_{eq} is the equilibrium NADH long fluorescence lifetime, i.e. the value of the long lifetime
 544 when the global oxidative flux is zero. This provides a second means to infer \tilde{r}_{ox} from FLIM
 545 measurements: dropping oxygen and plotting the relationship between τ_1 and $1/\beta$ provides a
 546 means to measure (A) and (B) from Equation (7), while τ_{eq} can be obtained from the NADH long
 547 fluorescence lifetime obtained at the lowest oxygen level. Once A, B and τ_{eq} are known, \tilde{r}_{ox} can
 548 be inferred solely from NADH long fluorescence lifetime τ_1 , using Equation (8).
 549

550 We next used the lifetime method (Equation 8) and the bound ratio method (Equation 5b) to
 551 separately infer \tilde{r}_{ox} in oocytes subject to a wide variety of conditions (varying oxygen levels,
 552 with oxamate, FCCP, rotenone, and oligomycin). We obtained A, B, β_{eq} and τ_{eq} for these
 553 different conditions (Figure 5-figure supplement 1 and Figure 6-figure supplement 1), and used
 554 the two different methods to provide two independent measures of \tilde{r}_{ox} (assuming α is constant
 555 across all conditions). The predictions of \tilde{r}_{ox} from these two methods quantitatively agree under
 556 all conditions (Figure 6b, $p = 0.73$), which is a strong self-consistency check that further supports
 557 the use of the model to infer ETC flux from FLIM measurements of NADH.
 558



559
 560 **Figure 6 | Coarse-grained NADH redox model self-consistently predicts NADH turnover rate from bound**
 561 **ratio and long fluorescence lifetime.** **a**, NADH long lifetime, τ_1 , is linearly related to the inverse of NADH bound
 562 ratio, $1/\beta$, from the oxygen drop experiment of individual oocytes treated with oxamate and rotenone (results from
 563 5 representative oocytes are shown for each condition). Each shade corresponds to results from an individual oocyte
 564 (symbols are experimental measurements and dashed lines are linear fits). **b**, NADH turnover rate \tilde{r}_{ox} obtained from
 565 NADH long lifetime (τ_1) using equation (8) agrees quantitatively with that from NADH bound ratio (β), obtained
 566 from equation 5b, across all perturbations ($p=0.73$). The solid line denotes where \tilde{r}_{ox} from lifetime equals that from
 567 bound ratio, the gray region denotes $\pm 5\%$ variation from equality. Error bars represent standard error of the mean
 568 (s.e.m) across different oocytes. P value is calculated from Student's t-test.
 569

570 **Figure 6-source data | Excel spreadsheet of single oocyte FLIM data used for Figure 6b.**
 571

572 **The NADH redox model enables accurate prediction of ETC flux in human tissue culture**
573 **cells**

574
575 After thoroughly testing the NADH redox model and the inference procedure in mouse oocytes,
576 we next investigated if it can be used in other cell types. We chose human tissue culture cells for
577 this purpose, since they are widely used as model systems to study metabolic dysfunctions in
578 human diseases including cancer (Vander Heiden et al. 2009) and neuropathology (Lin et al.
579 2006).

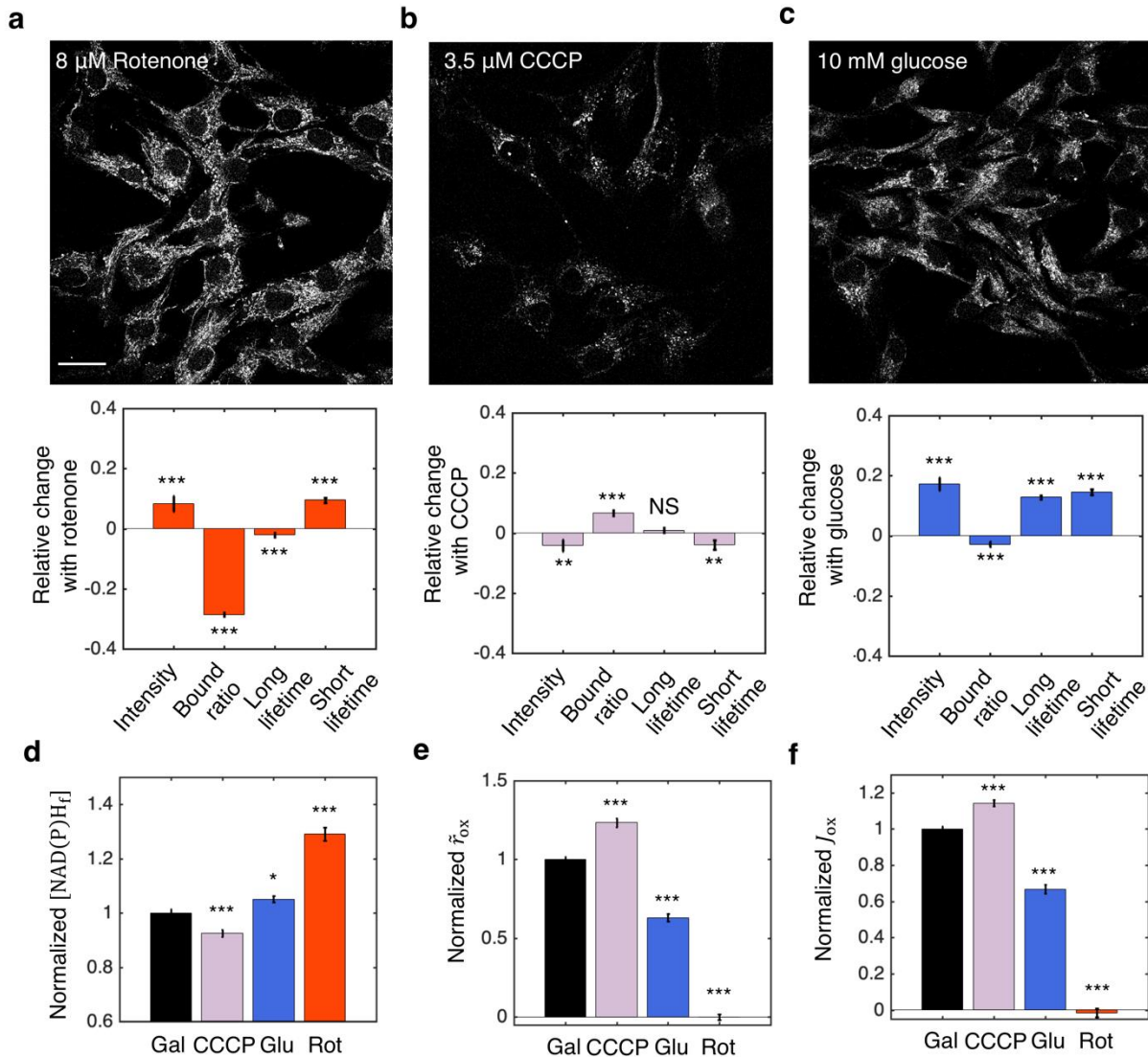
580
581 While mouse oocytes have a negligible level of NADPH compared to NADH (Bustamante et al.,
582 2017), the concentrations of NADH and NADPH are similar in tissue culture cells (10-100 μM
583 averaged over the whole cell) (Lu et al. 2018, Park et al. 2016, Blacker et al. 2014). Since
584 NADPH and NADH have overlapping fluorescent spectra (Patterson et al., 2000), the presence
585 of NADPH may complicate the interpretation of FLIM experiments. Thus, we investigated the
586 impact of background fluorescence, such as from NADPH, on the flux inference procedure. If
587 the background fluorescence does not change with the perturbations under study, then it can be
588 treated as an additive offset that systematically makes the measured concentrations of free and
589 bound NADH different from their actual values. In this case, a derivation in Appendix 5
590 demonstrates that the background fluorescence can be incorporated into the equilibrium bound
591 ratio β_{eq} and does not impact the flux inference procedures. In other words, if the modified β_{eq}
592 can be reliably determined, then the measured concentrations of free and bound fluorescent
593 species can be used in place of the true values of NADH in Equations 5a-c to infer the ETC flux.
594 An alternative possibility is that the background fluorescence does change with the perturbations
595 under study, but in a manner that is proportional to the change in NADH. In this case, the
596 background fluorescence can be incorporated into the equilibrium bound ratio α and, once more,
597 does not impact the flux inference procedures (Appendix 5). If the background fluorescence
598 changes in some more complicated manner, then the inference procedure may no longer be valid.
599 Thus, depending on the behavior of NADPH, it either might or might not interfere with the
600 inference procedure: no impact if NADPH is either constant or proportional to changes in
601 NADH, a possible impact otherwise. Therefore, the validity of the inference procedure in the
602 presence of significant NADPH fluorescence must be established empirically.

603
604 We next tested the inference procedures experimentally in hTERT-RPE1 (hTERT-immortalized
605 retinal pigment epithelial cell line) tissue culture cells. We started by exploring the impact of
606 metabolic perturbations on mitochondrial NAD(P)H: the combined signal from NADH and
607 NADPH (which are indistinguishable) from mitochondria. We first cultured the cells in DMEM
608 with 10 mM galactose (Methods). We then inhibited complex I of the ETC by adding 8 μM of
609 rotenone to the media. This resulted in a significant increase of mitochondrial NAD(P)H
610 intensity (Figure 7a upper). We segmented mitochondria using a machine-learning based
611 algorithm from the intensity images of NAD(P)H, and fitted the fluorescence decay curves of
612 mitochondrial NAD(P)H to obtain changes in FLIM parameters (Methods). All FLIM parameters
613 displayed significant changes (Figure 7a lower, $p < 0.001$, and Figure 7-figure supplement 1c).
614 We next uncoupled proton translocation from ATP synthesis by adding 3.5 μM CCCP to the
615 media. This led to a decrease of NAD(P)H intensity in the mitochondria (Figure 7b upper) and
616 significant changes in NAD(P)H bound ratio and short lifetime, but in opposite directions as
617 compared to rotenone perturbation (Figure 7b lower, $p < 0.01$, and Figure 7-figure supplement

618 1c). Finally, we perturbed the nutrient conditions by culturing the cells in DMEM with 10 mM
619 glucose. FLIM imaging revealed an increase of mitochondrial NAD(P)H intensity (Figure 7c
620 upper) and significant changes in all FLIM parameters as compared to the galactose condition
621 (Figure 7c lower, $p < 0.001$, and Figure 7-figure supplement 1d).

622
623 Inference of the ETC flux from FLIM measurements requires a measurement of β_{eq} . Since
624 rotenone is known to drastically decrease the OCR of hTERT-RPE1 cells to near zero (MacVicar
625 and Lane 2014), we used the NAD(P)H bound ratio measured in the presence of rotenone as β_{eq} .
626 Different values of β_{eq} were obtained for glucose and galactose conditions by adding 8 μ M of
627 rotenone to each condition (Figure 7-figure supplement 1d). We next calculated the
628 concentrations of free NAD(P)H, $[NAD(P)H_f]$, from the FLIM parameters using Equation (2a).
629 $[NAD(P)H_f]$ displayed significant changes for all perturbations (Figure 7d). Using Equation (5b)
630 and assuming α is a constant, we calculated the NAD(P)H turnover rate, \tilde{r}_{ox} , from the FLIM
631 measurements and β_{eq} . \tilde{r}_{ox} changed significantly for all perturbations (Figure 7e). Multiplying
632 \tilde{r}_{ox} and $[NAD(P)H_f]$, we obtained the predicted ETC flux, J_{ox} , which increased under FCCP,
633 decreased under glucose and reduced to zero under rotenone (Figure 7f).

634
635 To test the model predictions, we compared the predicted ETC flux with previous direct OCR
636 measurements of the same cell type that we used, under the same conditions (MacVicar and Lane
637 2014). Remarkably, the predicted changes in ETC fluxes are in quantitative agreement with the
638 directly measured OCR across all conditions as estimated from Figure 1A of MacVicar and
639 Lane, 2014: CCCP is predicted to increase the ETC flux by $14\% \pm 3\%$ (SEM), in agreement
640 with the $18\% \pm 21\%$ increase from OCR measurement ($p=0.80$); Glucose is predicted to
641 decrease ETC flux by $33\% \pm 3\%$, in agreement with the $46\% \pm 9\%$ decrease from OCR
642 measurements ($p=0.30$), shifting metabolism from oxidative phosphorylation to anaerobic
643 glycolysis. Since we used β from rotenone treatment as β_{eq} , the predicted decrease in ETC flux
644 after the addition of rotenone is $101\% \pm 2\%$, which is in agreement with the $82\% \pm 2\%$
645 decrease from OCR measurement ($p=0.28$). This quantitative agreement between predicted ETC
646 fluxes and measured OCR across all perturbations demonstrated the applicability of the NADH
647 redox model and the flux inference procedures to tissue culture cells, even though they contain
648 substantial levels of NADPH.



649
 650 **Figure 7 | NADH redox model accurately predicts ETC flux in hTERT-RPE1 human tissue culture cells. a-c:**
 651 NAD(P)H intensity images (scale bar 30 μm) and the corresponding changes of FLIM parameters in response to
 652 metabolic perturbations with the addition of 8 μM rotenone (a) (N=61), 3.5 μM CCCP (b) (N=72) and the change of
 653 nutrients from 10 mM galactose to 10 mM glucose (c) (N=77). Rotenone and CCCP are added to culturing media
 654 with 10 mM galactose (N=145). Measurements were taken within 30 minutes after the addition of the drugs. N
 655 specifies the number of images analyzed for each condition. A typical image contains dozens of cells as shown in
 656 a-c. **d-f:** free NAD(P)H concentrations ($[\text{NAD(P)H}_f]$) (d) NAD(P)H turnover rate ($\tilde{\tau}_{\text{ox}}$) (e), and inferred ETC flux
 657 (J_{ox}) (f) in response to CCCP, rotenone and glucose perturbations. Student's t-test is performed pairwise between
 658 perturbations and the 10 mM galactose condition. * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$. Error bars represent standard
 659 error of the mean (s.e.m) across different images.

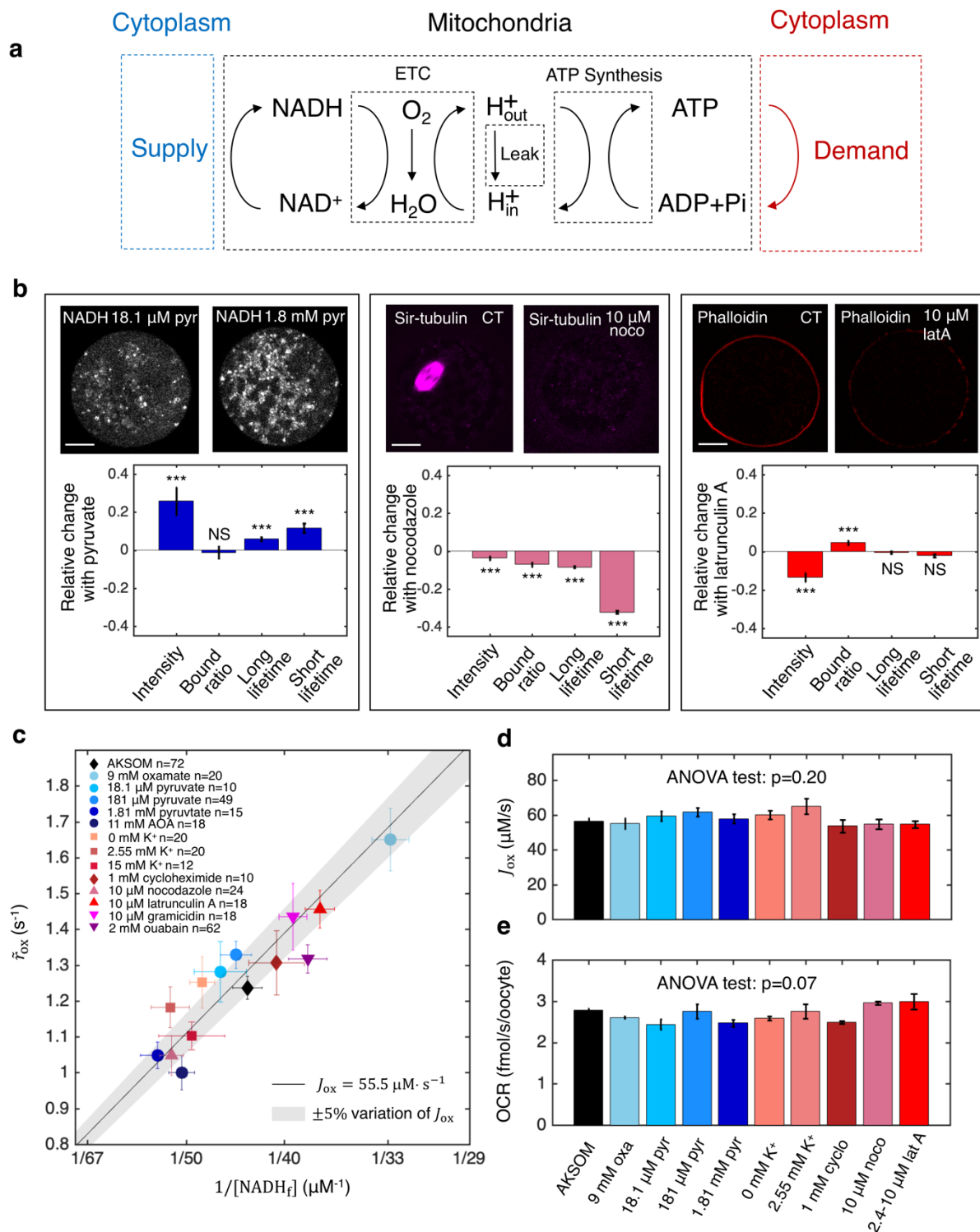
660
 661 **Figure 7-source data | Excel spreadsheet of single image FLIM data used for Figure 7a-f.**

662
 663 **Homeostasis of ETC flux in mouse oocytes: perturbations of nutrient supply and energy**
 664 **demand impact NADH metabolic state but do not impact ETC flux**

665
 666 Having established the validity of the NADH redox model and the associated flux inference
 667 procedures, we next applied it to study energy metabolism in mouse oocytes. We began by

668 investigating the processes that determine the ETC flux in MII mouse oocytes. Mitochondrial
669 based energy metabolism can be viewed as primarily consisting of three coupled cycles: the
670 NADH/NAD⁺ redox cycle (which our NADH redox model describes), the proton
671 pumping/dissipation cycle, and the ATP/ADP production/consumption cycle (Figure 8a). At the
672 most upstream portion of this pathway, the reduction of NAD⁺ to NADH is powered by a supply
673 of nutrients, while at the most downstream portion, energy-demanding cellular processes
674 hydrolyze ATP to ADP. To test whether nutrient supply and energy demand set ETC flux, we
675 investigated the effect of perturbing these processes. To perturb supply, we first varied the
676 concentration of pyruvate in the media from 181 μM (which is standard for AKSOM) to either
677 18.1 μM or 1.81 mM, and observed significant changes in NADH intensity and FLIM
678 parameters (Figure 8b left), demonstrating that the NADH metabolic state is altered. To perturb
679 demand, we began by adding 10 μM nocodazole to the media, which disassembled the meiotic
680 spindle, an energy user, and resulted in significant changes in NADH FLIM parameters (Figure
681 8b center). Similarly, the addition of 10 μM latrunculin A disassembled the actin cortex and also
682 produced significant changes in NADH FLIM parameters (Figure 8b right).

683
684 We next performed additional perturbations of nutrient supply, inhibiting the conversion of
685 lactate to pyruvate by lactate dehydrogenase (with 9 mM oxamate) and inhibiting the malate-
686 aspartate shuttle (with 11 mM AOA). We performed additional perturbations of energy demand
687 by inhibiting protein synthesis (with 1 mM cycloheximide) and ion homeostasis, by varying
688 extracellular potassium concentrations from 0 mM to 15 mM, inhibiting the Na⁺/K⁺ pump (with
689 2 mM ouabain), and adding an ionophore (10 μM gramicidin). All perturbations resulted in
690 significant changes in NADH FLIM parameters (Figure 8-figure supplement 1), showing that
691 NADH metabolic state is generally impacted by varying nutrient supply and cellular energy
692 demand. We next used the NADH redox model and the measured FLIM parameters to infer the
693 concentration and effective turnover rate of free NADH for these perturbations. The free NADH
694 concentrations, $[\text{NADH}_f]$, and turnover rates, \tilde{r}_{ox} , displayed large variations across the
695 perturbations, ranging from $33.5 \pm 1.0 \mu\text{M}$ (SEM) to $56.0 \pm 2.8 \mu\text{M}$ and from $1.0 \pm 0.05 \text{ s}^{-1}$ to
696 $1.65 \pm 0.09 \text{ s}^{-1}$ respectively (Figure 8c). Surprisingly, the changes in $[\text{NADH}_f]$ and \tilde{r}_{ox} were
697 highly anti-correlated such that the data points primarily fell within a region where the inferred
698 ETC flux, $J_{\text{ox}} = \tilde{r}_{\text{ox}}[\text{NADH}_f]$, is a constant $55.5 \mu\text{M} \cdot \text{s}^{-1}$ (Figure 8c solid line, shaded region
699 indicates 5% error). Indeed, ANOVA tests confirmed that perturbing nutrient supplies and
700 cellular energy demand lead to no significant change in either the inferred ETC flux (Figure 8d,
701 $p = 0.20$) or directly measured OCR (Figure 8e, $p = 0.07$). Thus, while nutrient supply and
702 cellular energy demand strongly affect mitochondrial NADH redox metabolism, they do not
703 impact ETC flux. In contrast, ETC flux is impacted by perturbing proton leak and ATP synthesis
704 (Figure 5). Taken together, this suggests that the ETC flux in mouse oocytes is set by the
705 intrinsic properties of their mitochondria, which can adjust their NADH redox metabolism to
706 maintain a constant flux when nutrient supplies and cellular energy demand are varied. The
707 mechanistic basis of this homeostasis of ETC flux is unclear and will be an exciting topic for
708 future research.



709
 710 **Figure 8 | Homeostasis of ETC flux in mouse oocytes: perturbations of nutrient supply and energy demand**
 711 **impact NADH metabolic state but do not impact ETC flux.** **a:** The three coupled cycles of mitochondrial based
 712 energy metabolism: the NADH/NAD⁺ redox cycle, the proton pumping/dissipation cycle, and the ATP/ADP
 713 production/consumption cycle. Nutrients supplied from the cytoplasm (blue) power the reduction of NAD⁺ to
 714 NADH. Energy-demanding cellular processes in the cytoplasm (red) hydrolyze ATP to ADP. **b:** Oocyte images
 715 (top) and change in NADH FLIM parameters relative to control (bottom) for changing pyruvate concentration (left),

716 addition of 10 μM nocodazole (center) and addition of 10 μM latrunculin A (right). Student's t-test were performed
717 for the change of FLIM parameters (* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$). The spindle disassembles after addition of 10
718 μM nocodazole (top, center) and the actin cortex disassembles after addition of 10 μM latrunculin A (top, right). **c**:
719 NADH turnover rate (\tilde{r}_{ox}) and NADH free concentrations ($[\text{NADH}_f]$) inferred from FLIM measurements under a
720 variety of perturbations of nutrient supply and energy demand. Error bars are standard error of the mean (s.e.m)
721 across oocytes. The black line corresponds to \tilde{r}_{ox} and $[\text{NADH}_f]$ values with an inferred flux of $J_{\text{ox}} = 55.5 \mu\text{M} \cdot \text{s}^{-1}$,
722 and the gray shaded region corresponds to a variation of $\pm 5\%$ around that value. **d**: The inferred ETC flux and **e**:
723 measured OCR show no change across different perturbations of nutrient supply and energy demand (ANOVA,
724 $p = 0.20$ and $p = 0.07$ respectively).

725
726 **Figure 8-source data | Excel spreadsheet of single oocyte FLIM data and batch OCR data used for Figure 8c-**
727 **e.**

728

729 **Subcellular spatial gradient of ETC flux in mouse oocytes: spatially inhomogeneous** 730 **mitochondrial proton leak leads to a higher ETC flux in mitochondria closer to cell** 731 **periphery**

732

733 Our results presented so far were performed by averaging together FLIM measurements from all
734 mitochondria within an oocyte. However, FLIM data is acquired with optical resolution,
735 enabling detailed subcellular measurements. To see if there are spatial variations in FLIM
736 measurements within individual oocytes, we computed the mean NADH fluorescence decay time
737 for each mitochondrial pixel. The mean NADH fluorescence decay time displays a clear spatial
738 gradient, with higher values closer to the oocyte center (Figure 9a).

739

740 To quantify this gradient in more detail, we partitioned mouse oocytes into equally-spaced
741 concentric regions (Figure 9b) and fitted the fluorescence decay curves from mitochondrial
742 pixels within each region to obtain FLIM parameters as a function of distance from the oocyte
743 center. NADH intensity, bound ratio and long lifetime in mitochondria all display significant
744 spatial gradient within oocytes (Figure 9c). Next, using Equations 5a-c and β_{eq} obtained at the
745 lowest oxygen level, and confirming that β_{eq} is uniform within the oocyte with complete
746 inhibition of ETC using high concentration of rotenone (Figure 9-figure supplement 1), we
747 predicted the ETC flux, J_{ox} , as a function of distance from the oocyte's center. The ETC flux
748 displayed a strong spatial gradient within oocytes, with a higher flux closer to the cell periphery
749 (Figure 9d). Note that, as described above, J_{ox} is actually a flux density with units of
750 concentration per second. Thus, the measured flux gradient is not merely a reflection of
751 variations in mitochondrial density, but instead indicates the existence of subcellular spatial
752 heterogeneities in mitochondrial activities.

753

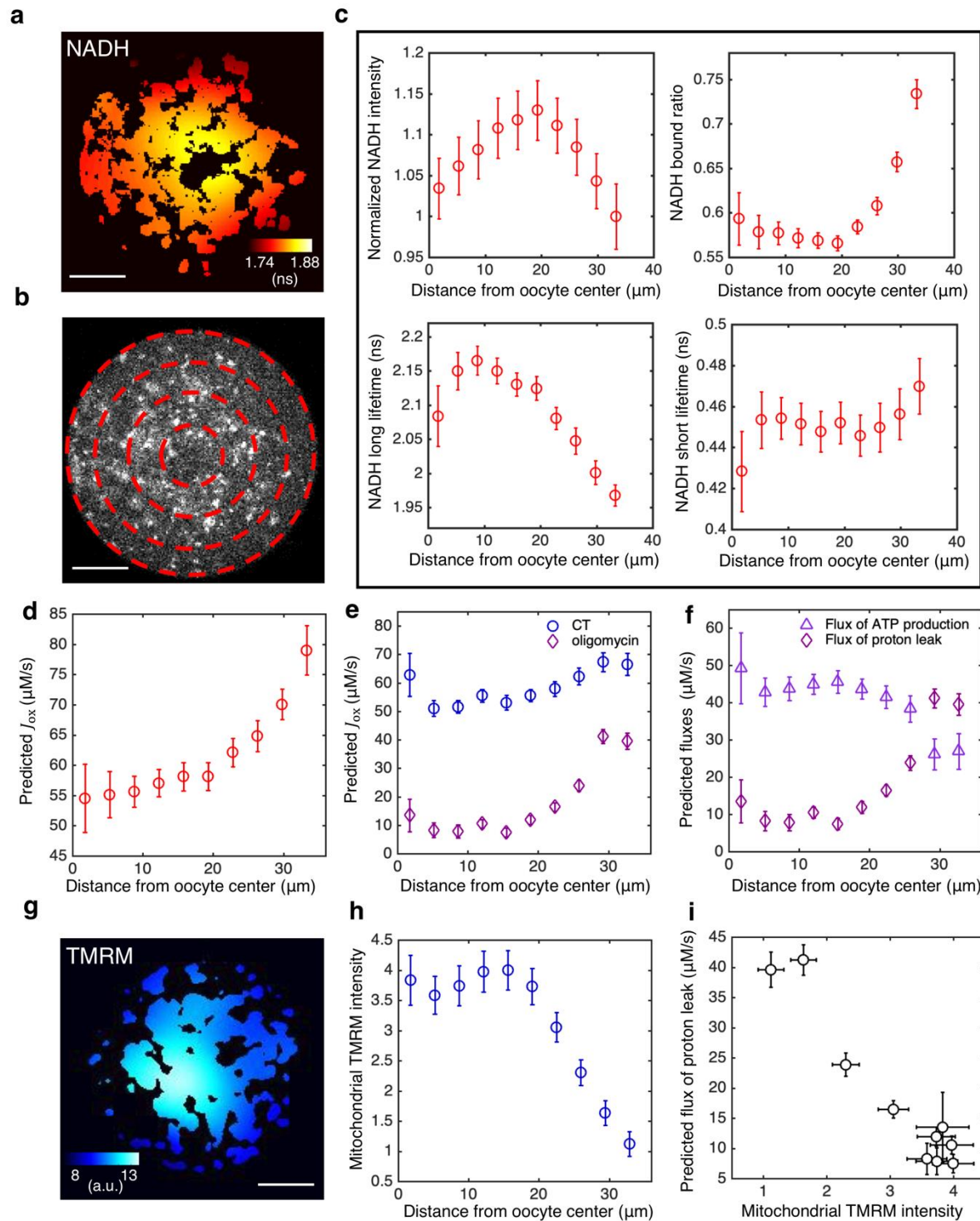
754 To investigate the origin of this flux gradient, we inhibited ATP synthase using 5 μM of
755 oligomycin and repeated measurements of subcellular spatial variations in inferred fluxes. After
756 inhibition, J_{ox} decreased at all locations throughout the oocytes and displayed an even more
757 dramatic flux gradient (Figure 9e). If oligomycin completely blocks ATP synthase, then the
758 remaining flux must be the result of proton leak. If it is further assumed that proton leak remains
759 the same with and without oligomycin, then the flux due to ATP synthase in control oocytes can
760 be determined by subtracting the flux after oligomycin inhibition (i.e. the proton leak) from the
761 flux before inhibition. Performing this procedure throughout oocytes indicates that proton leak
762 greatly increases in mitochondria near the periphery of oocytes, where ATP production decreases
763 (Figure 9f). This implies that the subcellular gradient in ETC flux is primarily caused by a

764 gradient in proton leak and that mitochondria near the periphery of oocytes are less active in
765 ATP production than those in the middle of the oocyte.

766
767 We hypothesized that a gradient in proton leak would result in a gradient of mitochondrial
768 membrane potential, with lower membrane potential closer to the cell periphery where proton
769 leak is the greatest. To test this, we measured mitochondrial membrane potential using the
770 membrane potential-sensitive dye TMRM, which preferentially accumulates in mitochondria
771 with higher membrane potential (AL-Zubaidi et al., 2019). We observed a strong spatial gradient
772 of the intensity of TMRM in mitochondria within oocytes, with dimmer mitochondria near the
773 cell periphery (Figure 9g, h), indicating that mitochondria near the periphery of the oocyte have a
774 lower membrane potential. This result is robust to locally normalizing TMRM intensity by
775 mitochondrial mass using a membrane potential insensitive dye (Mitotracker Red FM), or using
776 an alternative membrane potential-sensitive dye, JC-1 (Figure 9-figure supplement 2). The
777 predicted flux of proton leak and mitochondrial TMRM intensity shows a strong negative
778 correlation (Figure 9i), confirming our hypothesis.

779
780 Taken together, these results show that MII mouse oocytes contain subcellular spatial
781 heterogeneities of mitochondrial metabolic activities. The observation that proton leak is
782 responsible for the gradient of ETC flux suggests that the flux heterogeneity is a result of
783 intrinsic mitochondrial heterogeneity. This is consistent with our conclusion from the
784 homeostasis of ETC flux (Figure 8) that it is the intrinsic rates of mitochondrial respiration, not
785 energy demand or supply, that controls the ETC flux. The causes and consequences of the
786 subcellular spatial variation in mitochondrial activity remain unclear and is an exciting topic for
787 future research.

788
789



790
 791 **Figure 9 | Subcellular mitochondrial heterogeneity in mouse oocytes: spatially inhomogeneous mitochondrial**
 792 **proton leak leads to a higher ETC flux in mitochondria closer to cell periphery.** **a**, Heatmap of the mean NADH
 793 fluorescence decay time in mitochondria exhibits a subcellular spatial gradient within oocytes. **b**, NADH intensity
 794 image of the oocyte partitioned with equally-spaced concentric rings. **c**, Mitochondrial normalized NADH intensity
 795 (upper left), bound ratio β (upper right), long fluorescence lifetime τ_1 (lower left), and short fluorescence lifetime
 796 τ_s (lower right) as a function of distance from the oocyte center (n=67). **d**, Predicted ETC flux from FLIM of
 797 NADH as a function of distance from the oocyte center (n=67). **e**, ETC flux gradient is enhanced by 5 μM

798 oligomycin (n=37), suggesting the flux gradient is determined by proton leak. CT is AKSOM with oxamate (n=32).
799 9 mM oxamate is present in oligomycin condition to reduce cytoplasmic NADH signal for better mitochondrial
800 segmentation. **f**, Opposing flux gradients of proton leak and ATP production, where proton leak (ATP production) is
801 maximal (minimal) at the cell periphery. **g**, Heatmap of the TMRM intensity in mitochondria, which increases with
802 mitochondrial membrane potential, exhibits a subcellular spatial gradient within oocytes. **h**, Mitochondrial TMRM
803 intensity as a function of distance from the oocyte center (n=16). **i**, Predicted flux of proton leak correlates
804 negatively with mitochondrial membrane potential as measured by mitochondrial TMRM intensity. Scale bar 20
805 μm . Error bars represent standard error of the mean (s.e.m) across different oocytes.

806

807 **Discussion**

808

809 **The NADH redox model is a general model to relate FLIM measurements of NADH to** 810 **ETC fluxes**

811

812 Despite extensive studies and applications of FLIM in metabolic research (Bird et al., 2005;
813 Skala et al., 2007; Heikal, 2010; Sharick et al., 2018; Sanchez et al., 2018; Liu et al., 2018;
814 Sanchez et al., 2019; Ma et al., 2019), it remains a challenge to relate FLIM measurements to the
815 activities of the underlying metabolic pathways in cells. We overcame this challenge by
816 developing a coarse-grained NADH redox model that leads to quantitative predictions for the
817 relationship between FLIM measurements and the flux through the Electron Transport Chain
818 (ETC). The model was constructed by explicitly coarse-graining a detailed NADH redox model
819 with an arbitrary number of oxidases and reductases that represent all the possible enzymes
820 involved in NADH redox reactions. The reactions in the detailed NADH redox model can be of
821 arbitrary order and depend on implicit variables (i.e. free enzyme concentration, membrane
822 potential, pH, etc.) which obey their own dynamical equations. The dynamics of the redox model
823 will, of course, depend on the precise number of oxidases and reductases, the functional forms of
824 the rates, and specific mathematical models for all the variables the rates implicitly depend on.
825 However, the quantitative predictions relating FLIM measurements and ETC flux are
826 independent of these modeling choices. Coarse-graining the detailed NADH redox model
827 reduces all oxidases to an effective oxidase and all reductases to an effective reductase. The
828 kinetic rates of the coarse-grained model can be related to those of the detailed model by keeping
829 the global fluxes through the oxidases and the reductases the same in both models. The coarse-
830 grained model predicts that the flux through the ETC is a product of the turnover rate and the
831 concentration of free NADH (Equation 5a). The turnover rate is proportional to the difference
832 between the nonequilibrium and the equilibrium NADH bound ratio (Equation 5b), which are
833 measurable by FLIM of NADH (Equation 5c). Thus, this model provides a generic framework to
834 relate FLIM measurements of NADH to the flux through the ETC in mitochondria.

835

836 The central assumption required for the validity of Equations 5a-c is that the redox reactions, and
837 binding and unbinding processes, can be approximated as being at steady state (i.e. undergoing
838 only quasistatic changes over perturbations or development). At steady state, the net binding and
839 unbinding flux balances the oxidative flux of NADH. Therefore, the measurement of binding and
840 unbinding state of NADH from FLIM allows the inference of the ETC flux, irrespective of the
841 detailed behaviors of the oxidative reactions.

842

843 Remarkably, all the binding and unbinding rates of the NADH redox model are coarse-grained
844 into two effective parameters: α and β_{eq} , which can be experimentally measured. We determined

845 the value of α from an OCR measurement (Appendix 5, Equation (S48)), and we determined the
846 value of β_{eq} from FLIM of NADH at low oxygen levels or from rotenone perturbation
847 (Appendix 5, Figure 5-figure supplement 1h). In MII mouse oocytes, α does not significantly
848 vary in response to oxygen, or drug and nutrient perturbations. This is demonstrated by the
849 agreement between the predicted ETC flux and the measured OCR with a constant α of $5.4 \pm$
850 0.2 s^{-1} across a variety of conditions (Figure 5). α is predicted to depend only on the coarse-
851 grained unbinding rates of NADH from the enzymes (Equation (S43)), so the observed
852 constancy of α implies that the perturbations in this study primarily impacted the
853 reduction/oxidation reaction rates (and not the unbinding rates). In other scenarios, such as when
854 the concentrations of enzymes change, the coarse-grained unbinding rates might change, so α
855 might not be a constant. In contrast, β_{eq} does vary with drug and nutrient perturbations, but not
856 with oxygen level, allowing β_{eq} to be obtained at the lowest oxygen level for different drug and
857 nutrient conditions (Figure 5-figure supplement 1h and Figure 8-figure supplement 1h). Using
858 these two parameters, we inferred the effective turnover rate of free NADH, $\tilde{\tau}_{\text{ox}}$, from FLIM
859 measurements of NADH. By multiplying this turnover rate with the concentration of free
860 NADH, $[\text{NADH}_f]$ (also obtained from FLIM measurements using Equation 2a), we inferred the
861 ETC flux from Equation 5a. Thus, all the complex behaviors of the binding and unbinding and
862 reaction rates are captured by the variations in FLIM parameters of NADH, and our coarse-
863 grained model provides a generic way to interpret these variations.

864
865 While we found that β_{eq} is smaller than β in mouse oocytes, this does not generically have to be
866 true. Thus, if a perturbation is observed to decrease the NADH bound ratio β , it does not
867 necessarily imply a decrease of the ETC flux. Similarly, a decrease of NADH long lifetime is not
868 necessarily associated with an increase of the ETC flux. Therefore, measurements of α and β_{eq}
869 are required to use Equations 5a-c to infer ETC flux from FLIM measurements of NADH.

870

871 **The underlying assumptions and limitations of the NADH redox model**

872

873 In this section, we clarify the underlying assumptions and limitations of the model to facilitate
874 accurate interpretation of FLIM measurements of NADH in different biological contexts.

875

876 To use the coarse-grained NADH model, segmentation needs to be performed to separate the
877 mitochondrial NADH signal from the cytoplasmic NADH signal, because they encode different
878 metabolic fluxes. In mouse oocytes, the segmentation can be reliably performed based on NADH
879 images due to the higher NADH intensity in mitochondria than cytoplasm. Mitochondrial
880 movements are also slow in MII oocyte (Video 1), hence long exposure times can be used to
881 obtain high contrast NADH images. For cells where NADH contrast is low, such as in yeast cells
882 (Papagiannakis et al., 2016; Shaw and Nunnari, 2002), MitoTracker dye (Appendix 1, Figure 1-
883 figure supplement 1) or mitochondrial associated fluorescent proteins (Westermann and Neupert,
884 2000) will likely be needed for reliable segmentation of mitochondria.

885

886 One of the most important assumptions that enables the coarse-grained model to be used to
887 predict fluxes is that the NADH redox cycle can be well approximated as being at steady state,
888 i.e. the rate of change of NADH concentrations is much slower than the kinetic rates, including
889 the binding/unbinding rates and the reaction rates. This is true for mouse oocytes, where the
890 NADH intensity does not significantly change over the course of hours. This assumption also

891 holds for slow processes such as the cell cycle (Papagiannakis et al., 2016), which occurs on the
892 timescale of hours compared to timescales of seconds for the kinetic rates. This claim is
893 supported by the success of the model on human tissue culture cells. The steady-state
894 approximation could fail for rapid dynamics of NADH, such as the transient overshoot of NADH
895 in neurons induced by acute external stimulus (Díaz-García et al., 2020), but this needs to be
896 tested experimentally.

897
898 While NADH and NADPH share the same fluorescence spectrum, NADH concentration is 40
899 times greater than the concentration of NADPH for the whole mouse oocytes and presumably
900 even higher for mitochondria (Bustamante et al., 2017). NADPH concentration can be
901 comparable to that of NADH for other cell types such as tissue culture cells (Park et al., 2016).
902 However, we have shown that the presence of NADPH signal and other background fluorescence
903 signals only affect the equilibrium bound ratio β_{eq} or the prefactor α , and hence does not affect
904 the flux inference procedure if β_{eq} can be reliably determined and α remains a constant
905 (Appendix 5). This was validated in tissue culture cells by comparing predicted ETC flux (Figure
906 7) with previous OCR measurements (MacVicar and Lane 2014).

907
908 Finally, when relating NADH FLIM measurements to the ETC flux we did not explicitly
909 consider the contribution to the flux through FADH₂. This is a valid approximation when the
910 FADH₂ oxidative flux is much smaller than the NADH oxidative flux, as is often the case since
911 pyruvate dehydrogenase plus the TCA cycle yields 4 NADH molecules but only one FADH₂
912 molecule per cycle. Alternatively, if the FADH₂ flux is proportional to the NADH flux then a
913 rescaled value of α can be used in Equation 5b to effectively account for both fluxes. The
914 proportionality of FADH₂ flux and NADH flux is expected when NADH and FADH₂ are
915 produced from the same redox cycle with fixed stoichiometry, such as the pyruvate
916 dehydrogenase and TCA cycle. This proportionality will break down if significant amounts of
917 NADH and FADH₂ are produced in independent cycles where the stoichiometry varies, for
918 example, when the glycerol phosphate shuttle acts as a reductase in mitochondria for FADH₂ but
919 not for NADH.

920
921 Given these underlying assumptions, the model needs to be tested before being applied to other
922 biological systems. The present study provides an example for such tests in mouse oocytes and
923 human tissue culture cells by comparing the predicted ETC flux from FLIM with direct
924 measurements of oxygen consumption rate across a wide range of perturbations.

925 926 **Towards spatiotemporal regulations of metabolic fluxes in cells**

927
928 Cells transduce energy from nutrients to power various cellular processes. The ETC flux
929 represents the total rate of energy conversion by mitochondria. Despite detailed knowledge of the
930 biochemistry of mitochondrial metabolism, it is still unclear what cellular processes determine
931 ETC flux or how cells partition energetic fluxes to different cellular processes, including
932 biosynthesis, ion pumping, and cytoskeleton assemblies. Energetic costs of specific cellular
933 processes have been estimated from theoretical calculations (Stouthamer, 1973) or through
934 inhibition experiments (Mookerjee 2017). The latter typically involves measurements of the
935 change of metabolic fluxes, such as OCR, upon inhibition of specific cellular processes, and
936 interpreting this change as the energetic cost of the inhibited process. This interpretation is valid

937 if metabolic flux is determined by the energy demand of different cellular processes in an
 938 additive manner. This assumption has not been thoroughly tested. Using the NADH redox
 939 model, we discovered a homeostasis of ETC flux in mouse oocytes where perturbing energy
 940 demand and supply do not impact ETC flux despite significantly changing NADH metabolic
 941 state. On the other hand, perturbing ATP synthesis and proton leak greatly impacted the ETC
 942 flux. From these results, we concluded that it is the intrinsic rates of mitochondrial respiration,
 943 rather than energy supply or demand, that controls the ETC flux in mouse oocytes. While NADH
 944 metabolic state significantly changed in response to perturbing energy demand and supply,
 945 indicating cell metabolism was indeed impacted, it is unclear if these perturbations also
 946 influenced ATP, ADP or AMP levels. Future work, including direct measurements of ATP, ADP
 947 and AMP levels, will be required to uncover the mechanism of flux homeostasis. More broadly,
 948 our work demonstrates that it is a prerequisite to understand the regulation of ETC fluxes in
 949 order to correctly interpret the changes of ETC flux upon inhibiting subcellular processes.

950
 951 The mechanism of the homeostasis of ETC flux is unclear. One possibility is the presence of flux
 952 buffering pathways, where the change of ATP fluxes induced by process inhibition is offset by
 953 the opposing change of fluxes through the buffering pathways. Enzymes such as adenylate
 954 kinase are known to buffer concentrations of adenine nucleotide (De la Fuente et al. 2014), but it
 955 is unclear if they also buffer fluxes. Another possibility is a global coupling of cellular processes,
 956 where the change of ATP consumption by one process is offset by the change of others. Changes
 957 in proton leak could also compensate for changes in ATP production. Additional work will be
 958 required to distinguish between these (and other) possibilities.

959
 960 FLIM data is obtained with optical resolution, enabling subcellular measurements of NADH
 961 metabolic state. Interpreting these measurements using the NADH redox model enables
 962 inference of metabolic fluxes with subcellular resolution. Using this method, we discovered a
 963 subcellular spatial gradient of ETC flux in mouse oocytes, where the ETC flux is higher in
 964 mitochondria closer to the cell periphery. We found that this flux gradient is primarily a result of
 965 a spatially heterogeneous mitochondrial proton leak. It will be an exciting aim for future research
 966 to uncover the causes and consequences of the subcellular spatial variation in mitochondrial
 967 activity.

968

969 **Materials and methods**

970

Key Resources Table				
Reagent type (species) or resource	Designation	Source or reference	Identifiers	Additional information
cell line (<i>Homo-sapiens</i>)	hTERT-RPE1	Iain Cheeseman Lab	ATCC Cat# CRL-4000, RRID:CVCL_4388	

biological sample (mouse)	MII oocytes	Embryotech	Strain: B6C3F1	
commercial assay or kit	MitoTracker Red FM	ThermoFisher	Cat.#: M22425	
commercial assay or kit	TMRM	Sigma-Aldrich	Cat.#: T5428 CAS: 115532-50-8	
commercial assay or kit	JC-1	ThermoFisher	Cat.#: T3168	
commercial assay or kit	SiR-Tubulin	Cytoskeleton Inc	Cat.#:CY-SC006	
commercial assay or kit	Phalloidin	ThermoFisher	Cat.#:F432	
chemical compound, drug	Sodium oxamate	Sigma-Aldrich	Cat.#:O2751 CAS: 565-73-1	
chemical compound, drug	Rotenone	Sigma-Aldrich	Cat.#:R8875 CAS: 83-79-4	
chemical compound, drug	Oligomycin A	Sigma-Aldrich	Cat.#:75351 CAS: 579-13-5	
chemical compound, drug	FCCP	Sigma-Aldrich	Cat.#:C2920 CAS: 370-86-5	
chemical compound, drug	CCCP	Sigma-Aldrich	Cat.#:C2759 CAS: 555-60-2	

chemical compound, drug	Glucose	Sigma-Aldrich	Cat.#:D9434 CAS: 50-99-7	
chemical compound, drug	Galactose	Millipore	Cat.#:48260 CAS: 59-23-4	
chemical compound, drug	Pyruvate	Sigma-Aldrich	Cat.#:P2256 CAS: 113-24-6	
chemical compound, drug	Cycloheximide	Sigma-Aldrich	Cat.#:C4859 CAS: 66-81-9	
chemical compound, drug	Nocodazole	Sigma-Aldrich	Cat.#:M1404 CAS: 31430-18-9	
chemical compound, drug	Latrunculin A	Sigma-Aldrich	Cat.#:L5163 CAS:76343-93-6	
chemical compound, drug	Gramicidin	Sigma-Aldrich	Cat.#:50845 CAS:11029-61-1	
chemical compound, drug	Ouabain	Sigma-Aldrich	Cat.#:O3125 CAS:11018-89-6	
chemical compound, drug	Aminooxyacetic acid (AOA)	Sigma-Aldrich	Cat.#:C13408 CAS:2921-14-4	
software, algorithm	FLIM data acquisition (SPCM)	Becker & Hickl	RRID:SCR_018310	

software, algorithm	FLIM data acquisition (Labview)	National Instruments	RRID:SCR_014325	
software, algorithm	FLIM data analysis (MATLAB R2015b)	MathWorks	RRID:SCR_001622	
software, algorithm	OCR data acquisition (SensorTrace Profiling)	Unisense		

971

972

Culturing of mouse oocytes

973

974 Frozen MII mouse oocytes (Strain B6C3F1) were purchased from EmbryoTech. Oocytes were
 975 thawed and cultured in droplets of AKSOM media purchased from Millipore Sigma in plastic
 976 petri dish. Mineral oil from VitroLife was applied to cover the droplets to prevent evaporation of
 977 the media. Oocytes were then equilibrated in an incubator at 37°C, with 5% CO₂ and air
 978 saturated oxygen before imaging. For imaging, oocytes were transferred to a 2 µl media droplet
 979 in a 35 mm glass bottom FluoroDish from WPI covered with 400-500 µl of oil. The glass bottom
 980 dish was placed in an ibidi chamber with temperature and gas control during imaging.
 981 Temperature was maintained at 37 °C via heated chamber and objective heater. CO₂ was
 982 maintained at 5% using gas tanks from Airgas.

983

Cell lines

984

986 The hTERT-RPE1 cell line is an established wild-type cell line received from the Cheeseman lab
 987 that has been validated based on behavior and properties. The hTERT-RPE1 cell line was
 988 maintained and tested for mycoplasma contamination in the Needleman lab on a regular basis
 989 (Southern Biotech).

990

Culturing of hTERT-RPE1 cells

991

993 Cell lines were maintained at 37°C and 5% CO₂. Cells were grown in Dulbecco's Modified
 994 Eagle Medium (DMEM) (11966025, Gibco) supplemented with 10% Fetal Bovine Serum (FBS),
 995 0.5 mM sodium pyruvate, 5 mM HEPES, 1% penicillin and streptomycin, and either 10 mM
 996 glucose or 10 mM galactose. Cells were passaged in glucose or galactose at least three times
 997 before imaging. Cells were plated on 35 mm glass bottom FluoroDishes from WPI for imaging.
 998 Right before imaging, the media was replaced with 1 mL of phenol red-free DMEM (A1443001,
 999 Gibco) supplemented with 0.5 mM sodium pyruvate, 4 mM L-glutamine, 10 mM HEPES, and
 1000 either 10 mM glucose or 10 mM galactose.

1001

FLIM measurements

1002

1003

1004 Our FLIM system consists of a two-photon confocal microscope with a 40X 1.25NA water
1005 immersion Nikon objective, Becker and Hickler Time Correlated Single Photon Counting
1006 (TCSPC) acquisition system and a pulsed MaiTai DeepSee Ti:Sapphire laser from Spectra-
1007 Physics. NADH autofluorescence was obtained at 750 nm excitation wavelength with a 460/50
1008 nm emission filter. Laser power at the objective was maintained at 3 mW. The scanning area was
1009 512 by 512 pixels with a pixel size of 420 nm. Acquisition time was 30 seconds per frame.
1010 Oocytes were imaged with optical sectioning across their equators. A histogram of NADH
1011 fluorescence decay times was obtained at each pixel of the image.

1012

1013 **Oxygen measurements**

1014

1015 Oxygen level was measured in the Ibidi chamber with an electrode-based oxygen sensor
1016 (Gaslab). Since the oil layer covering the media droplet was very thin, the oxygen level in the
1017 droplet was assumed to be in instant equilibration with the chamber.

1018

1019 **Image and FLIM data analysis**

1020

1021 To separate mitochondrial NADH signal from cytoplasmic signal, we performed machine
1022 learning based segmentation algorithms on NADH intensity images. We used the freeware ilastik
1023 (Berg et al., 2019), which implements a supervised learning algorithm for pixel classification.
1024 The classifiers were trained to separate mitochondrial pixels from cytoplasmic pixels with a
1025 greater than 80% accuracy, as tested by MitoTracker Red FM (Appendix 1, Figure 1-figure
1026 supplement 1). We grouped photons from all mitochondrial pixels to obtain a histogram of
1027 NADH decay times for each oocyte and for each image of tissue culture cells. To extract the
1028 FLIM parameters of NADH bound fraction f , long lifetime τ_1 and short lifetime τ_s , we fitted the
1029 histogram with $G = \text{IRF} * (C_1 F + C_2)$, where $*$ indicates a convolution, and IRF is the instrument
1030 response function of the FLIM system, measured using a urea crystal. $F(\tau) = f \cdot \exp\left(-\frac{\tau}{\tau_1}\right) +$

1031 $(1 - f) \cdot \exp\left(-\frac{\tau}{\tau_s}\right)$ is the two-exponential model for the NADH fluorescence decay. C_1 is the
1032 amplitude of the decay and C_2 is the background noise. The fitting was performed with a custom
1033 MATLAB code using a Levenberg-Marquardt algorithm (Yoo, 2018). To obtain the intensity, I ,
1034 of mitochondrial NADH, we first measured the average number of photons per mitochondrial
1035 pixel, and divided it by the pixel area, $0.185 \mu\text{m}^2$, and pixel scanning time $4.09 \mu\text{s}$. The flux of
1036 ETC is inferred using Equations 5a-c for each oocyte and for tissue culture cells in a single
1037 image. Heatmaps of mean NADH fluorescence decay times were obtained by computing NADH
1038 fluorescence decay time of each mitochondrial pixel and averaging over neighboring
1039 mitochondrial pixels weighted by a gaussian kernel with a standard deviation of 20 pixels. All
1040 FLIM measurements were taken from distinct individual oocytes and distinct images of tissue
1041 culture cells. Error bars in all figures of FLIM represent standard error of the mean across
1042 different individual oocytes or across different images for tissue culture cells. Number of oocytes
1043 is reported with n . Number of images for tissue culture cells is reported with N .

1044

1045 **Error analysis**

1046

1047 FLIM curves were independently fit for each individual oocyte. The reported error bars in this
1048 manuscript are standard errors of the mean (SEMs) across these measurements, which depends

1049 on the level of variation (the standard deviation) between the oocytes. Two sources of variation
1050 in FLIM measurements across the oocytes are: 1) true biological variations between oocytes and
1051 2) fitting errors in the FLIM analysis. To estimate the error of fitting, we performed
1052 bootstrapping with randomly drawn points with substitution from each fluorescence decay curve
1053 for 53 oocytes. There are ~66000 photons per oocyte, from which we generated 10 bootstrapped
1054 decay curves per oocyte to estimate the fitting error. The fitting error is computed as the variance
1055 and covariance of the fitted parameters across bootstrapped decay curves and averaged over 53
1056 oocytes.

1057
1058 At high oxygen level in the AKSOM condition, the bootstrapping yields a variance of $2.2 \times$
1059 10^{-4} , $4.6 \times 10^{-3} \text{ ns}^2$, $6.0 \times 10^{-4} \text{ ns}^2$ for bound fraction, long lifetime and short lifetime,
1060 respectively. The cell-to-cell variances obtained from a single fit per oocyte are 4.4×10^{-4} ,
1061 $9.5 \times 10^{-3} \text{ ns}^2$, $1.6 \times 10^{-3} \text{ ns}^2$ for bound fraction, long lifetime, short lifetime, respectively.
1062 Hence the bootstrapping error accounts for 50%, 49% and 40% of the cell-to-cell variance in
1063 bound fraction, long lifetime and short lifetime, respectively. The bootstrapping yields a
1064 covariance of $-1.0 \times 10^{-3} \text{ ns}^2$ between bound fraction and long lifetime, which only accounts
1065 for ~20% of the covariance between these two variables during oxygen drop experiment. The
1066 inferred mean flux for oocytes at high oxygen levels in AKSOM is $\langle J_{\text{ox}} \rangle = 56.6 \mu\text{M/s}$.
1067 Propagating the error of fitting in all parameters from the bootstrapping analysis to the inferred
1068 flux gives a standard error of the mean in J_{ox} of 1.1 $\mu\text{M/s}$. The standard error of the mean in J_{ox}
1069 obtained from a single fit per oocyte was 2.0 $\mu\text{M/s}$. Thus, fitting errors account for ~50% of the
1070 standard error of the mean in J_{ox} .

1071 1072 **Metabolic and demand perturbations**

1073
1074 Oxygen drop experiments for oocytes were performed by mixing nitrogen-balanced 5% O₂ gas
1075 with 0% O₂ gas at different ratios to create a continuous oxygen drop profile. CO₂ was
1076 maintained at 5%. Oocytes were imaged for 10mins at 5% O₂, 30 mins during the continuous
1077 drop from 5% O₂ to approximately 0% O₂, and 20mins after quickly returning to 5% O₂. Oxygen
1078 levels were simultaneously monitored with an electrode-based oxygen sensor in the ibidi
1079 chamber. 5% O₂ corresponds to ~50 μM of oxygen concentration in the culturing media. All the
1080 drug perturbations for oocytes were performed by equilibrating oocytes in the AKSOM media
1081 containing the corresponding drug for 15-30 mins before the oxygen drop experiments. Pyruvate
1082 and potassium perturbations were performed by making KSOM media following Cold Spring
1083 Harbor Laboratory protocols with varying concentrations of sodium pyruvate and potassium,
1084 respectively. For oligomycin, FCCP, rotenone and pyruvate perturbations, 9 mM of sodium
1085 oxamate was also added to the media to suppress cytoplasmic NADH signal for better
1086 mitochondrial segmentation. The addition of the oxamate does not change the ETC flux of the
1087 mitochondria (Figure 5b).

1088
1089 For hTERT-RPE1 cells, drug perturbations were performed by replacing the media with drug-
1090 containing media through pipetting. Cells were imaged for 20-30 minutes immediately after drug
1091 perturbations.

1092
1093 All drugs were purchased from Sigma Aldrich. Temperature was maintained at 37 °C. CO₂ was
1094 maintained at 5%.

1095

1096 **Oxygen consumption rate (OCR) measurement**

1097

1098 The oxygen consumption rate of the oocytes was measured using the nanorespirometer from
1099 Unisense (Lopes et al., 2005). A batch of 10 to 15 oocytes were placed at the bottom of a glass
1100 capillary with a diameter of 0.68 mm and a height of 3 mm. The capillary well is filled with
1101 AKSOM media or drug-containing media for metabolic perturbations. After an equilibration
1102 time of ~2 hours, a steady state linear oxygen gradient is established in the capillary well due to
1103 the balance of oocyte respiration and oxygen diffusion. A motor-controlled electrode-based
1104 oxygen sensor (Unisense) is used to measure the oxygen gradient. The oxygen consumption rate
1105 is calculated as the product of the oxygen gradient, diffusivity of oxygen in the media, taken to
1106 be $3.37 \times 10^{-5} \text{ cm}^2/\text{s}$, and the cross sectional area of the capillary well, which was 0.36 mm^2 .
1107 The entire system was enclosed in a custom built chamber with temperature and gas control.
1108 Temperature was maintained at 37 °C. Oxygen level was continuously varied during oxygen
1109 drop experiments by slowly mixing 20% O₂ with 0% O₂ from gas tanks, and maintained at the
1110 air saturation level for drug and pyruvate perturbations. OCR was measured on a group of 10 to
1111 15 oocytes at a time. Single-oocyte OCR was obtained by dividing the measured OCR by the
1112 number of oocytes in the group. Error bars in all figures of OCR represent standard error of the
1113 mean across different groups of oocytes normalized by the number of oocytes in each group.
1114 Number of oocytes is reported with n. Number of groups is reported with N.

1115

1116 **Statistical analysis**

1117

1118 For the comparison between inferred ETC flux and measured ETC flux of the oocytes, two
1119 sample t-test was performed on the vectors of inferred single-cell ETC flux (with n elements,
1120 where n is the number of oocytes) and the batch OCR measurements (with N elements, where N
1121 is the number of batch groups). For the comparison between inferred ETC flux and measured
1122 ETC flux of the tissue culture cells, two sample t-test was performed on the vectors of inferred
1123 relative change of ETC flux (with n elements, where n is the number of images) and the relative
1124 change of OCR estimated from Figure 1A of MacVicar and Lane, 2014 (with N elements, where
1125 N is the estimated number of OCR data points).

1126

1127 **Mitochondrial membrane potential measurement**

1128

1129 The spatial distribution of mitochondrial membrane potential within oocytes was measured with
1130 a potential-sensitive dye TMRM (Sigma Aldrich). Oocytes were cultured in AKSOM with 100
1131 nM TMRM for 30 minutes before imaging. TMRM signal was obtained at 830 nm excitation
1132 wavelength with 560/40 nm emission filter. Mitochondrial TMRM intensity in different regions
1133 of the oocyte was computed by dividing the total number of photons from that region by the
1134 number of pixels in the same region. Heatmaps of mitochondrial TMRM intensity were obtained
1135 by computing photon counts for each mitochondrial pixel and averaging over neighboring
1136 mitochondrial pixels weighted by a gaussian kernel with a standard deviation of 20 pixels. To
1137 normalize TMRM intensity by mitochondrial mass, we cultured oocytes in AKSOM with 100
1138 nM MitoTracker Red FM and 25 nM TMRM for 30 minutes before imaging. We also cultured
1139 oocytes in AKSOM with 1 µg/ml JC-1 dye for 3 hours before imaging.

1140

1141 Mitochondrial membrane potential of hTERT-RPE1 cells was measured with TMRM. The cells
1142 were cultured in DMEM with 100 nM TMRM for 15-30 minutes before imaging. To measure
1143 membrane potential under drug perturbations, the original media was pipetted out and replaced
1144 with media containing both 100 nM TMRM and the drug. The cells were imaged for 20-30
1145 minutes immediately after drug perturbations. TMRM intensity ratio was obtained by
1146 normalizing the mitochondrial TMRM intensity by the cytoplasmic TMRM intensity.

1147

1148 **Appendix 1**

1149

1150 **Segmentation of mitochondria and calculation of NADH concentrations**

1151

1152 **Segmentation of mitochondria**

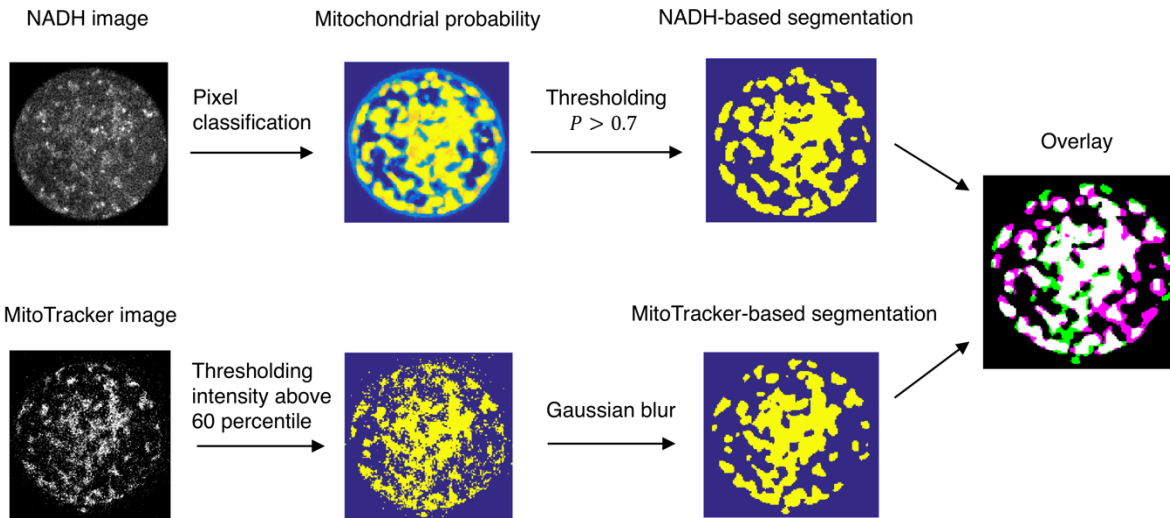
1153

1154 We used Ilastik, a machine-learning-based software for image analysis, to classify pixels in the
1155 NADH intensity images containing mitochondria (Berg et al., 2019). For each experiment, we
1156 generated a time lapse movie of NADH (Video 1). We used a few images in the movie as the
1157 training data set to train the software to classify mitochondrial pixels by manually selecting
1158 clustered high brightness pixels. Other pixels are classified as either cytoplasm or background.
1159 We then applied the trained pixel classifier to generate a mitochondrial probability map for each
1160 image in the entire movie, with each pixel assigned a probability between 0 to 1 to be
1161 mitochondrial pixel. Pixels with a probability higher than 0.7 were considered to be
1162 mitochondrial pixels.

1163

1164 To test the accuracy of this segmentation algorithm, we immersed the oocytes in AKSOM media
1165 containing MitoTracker Red FM, a dye that specifically labels mitochondria. Pixels with
1166 intensity above 60 percentile in the MitoTracker image were considered to be mitochondrial
1167 pixels. We imaged NADH and MitoTracker for the same oocyte and compared the resulting
1168 distribution of mitochondria (Figure 1-figure supplement 1). We defined the accuracy of the
1169 NADH-based segmentation as the fraction of photons originating from true mitochondrial pixels.
1170 The accuracy of the segmentation is $80.6 \pm 1.0\%$ (SEM) for the control condition as averaged
1171 over 7 oocytes. We repeated the analysis for oxamate, oligomycin, FCCP and rotenone
1172 perturbations, and obtained an accuracy of segmentation of $78.6 \pm 1.4\%$, $84.1 \pm 1.6\%$, $83.7 \pm$
1173 0.5% , $81.7 \pm 2.0\%$, respectively, similar to the control condition.

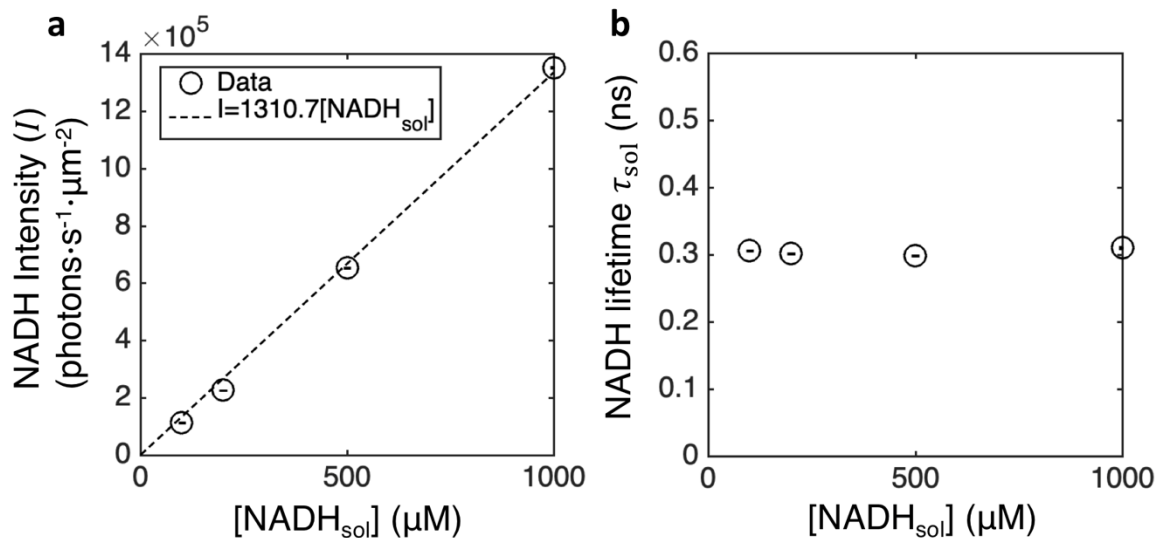
1174



1175
1176

Figure 1-figure supplement 1 | Machine learning based segmentation of mitochondria from NADH intensity images. The NADH-based segmentation image is overlaid with MitoTracker-based segmentation image. The white region corresponds to the overlap. The accuracy of the NADH-based segmentation is quantified as the ratio of the photon count from the overlap pixels to the photon count from mitochondrial pixels based on NADH segmentation.

1177 **Converting NADH intensity to NADH concentrations**
1178



1179 **Figure 1-figure supplement 2 | Calibration and conversion of NADH concentrations from fluorescence**
1180 **intensities and lifetimes in vitro.** **a**, NADH intensity vs titrated NADH concentrations in AKSOM solution. **b**,
1182 fluorescence lifetime of NADH in AKSOM solution.
1183

1184 Since the molecular brightness of NADH depends on the fluorescence lifetime of NADH, which
1185 changes drastically upon binding enzymes, the NADH concentration is not linearly proportional
1186 to NADH intensity. FLIM provides an accurate way of measuring NADH concentrations by
1187 simultaneously measuring fluorescence intensity and lifetime. We now derive the NADH
1188 intensity-concentration relation from the FLIM measurements. Assuming molecular brightness is

1189 proportional to the fluorescence lifetime, and therefore that free and bound NADH have different
 1190 contributions to the measured intensity, we have

1191
 1192
$$I = c_s \tau_s [\text{NADH}_f] + c_s \tau_1 [\text{NADH}_b] \quad (\text{S1}),$$

1194 where I is the intensity of NADH and c_s is a calibration factor that depends on the laser power.
 1195 From equation (S1), we obtained the concentrations of free and bound NADH:

1197
$$[\text{NADH}_f] = \frac{I(1-f)}{c_s[(\tau_1-\tau_s)f+\tau_s]} \quad (\text{S2}),$$

1198
$$[\text{NADH}_b] = [\text{NADH}_f] \frac{f}{1-f} \quad (\text{S3}),$$

1199 where f is the fraction of bound NADH.

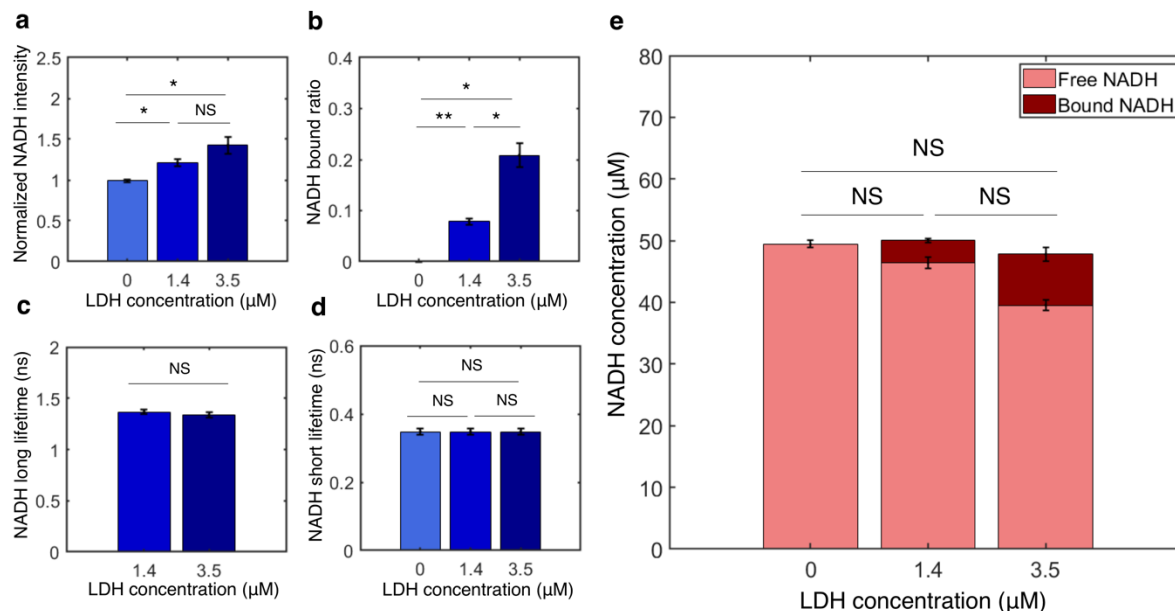
1202 To get the calibration factor c_s , we titrated NADH in AKSOM solutions and fitted the calibration
 1203 curve using:

1205
$$I = c_s \tau_{\text{sol}} [\text{NADH}_{\text{sol}}] \quad (\text{S4}),$$

1207 where τ_{sol} is the lifetime of NADH in solution. τ_{sol} was directly measured by FLIM (Figure 1-
 1208 figure supplement 2b), allowing us to obtain c_s from the fit (Figure 1-figure supplement 2a).

1210 **FLIM can be used to accurately measure concentrations of bound and free NADH *in vitro***

1211



1212
 1213 **Figure 1-figure supplement 3 | Measurement of concentrations of free and bound NADH *in vitro* from FLIM**
 1214 **of NADH.** a-d, NADH intensity, bound ratio, long lifetime and short lifetime from FLIM of NADH with various
 1215 concentrations of lactate dehydrogenase (LDH) *in vitro*. e. Concentrations of free and bound NADH calculated from
 1216 FLIM of NADH. Error bars are standard error across replicates. N=2. Student's t-test is performed. *p<0.05,
 1217 **p<0.01, ***p<0.001.

1218
1219 To test if absolute concentrations of free and bound NADH can be accurately measured from
1220 FLIM of NADH, we prepared solutions with known total concentration of NADH, and titrated
1221 the concentration of lactate dehydrogenase (LDH), an enzyme to which NADH can bind. We
1222 prepared the solutions with 50 mM TRIS buffer, 150 mM NaCl at pH 7.6 and 37°C. We added a
1223 total concentration of 50 μ M NADH to the solution and titrated LDH concentrations at 0, 1.4 μ M
1224 and 3.5 μ M. We first performed single exponential fitting of the NADH decay curve at 0 μ M
1225 LDH, where all NADH are free, to obtain the NADH short lifetime (Figure 1-figure supplement
1226 3d). From the NADH intensity (Figure 1-figure supplement 3a), we obtained the calibration
1227 factor c_s using equation (S4) with $[\text{NADH}_{\text{sol}}] = 50 \mu\text{M}$. We then fixed the short lifetime and
1228 performed two-exponential fitting of the NADH decay curve at LDH concentrations of 1.4 μ M
1229 and 3.5 μ M to obtain the bound ratio (Figure 1-figure supplement 3b) and long lifetime (Figure
1230 1-figure supplement 3c). As expected, NADH bound ratio increases with LDH concentrations, as
1231 there is more enzyme for NADH to bind. Finally, we calculated free NADH concentration
1232 $[\text{NADH}_f]$ and bound NADH concentration $[\text{NADH}_b]$ using equations (S2) and (S3) from the
1233 FLIM parameters. Remarkably, the free and bound concentrations of NADH both change with
1234 LDH concentrations but the total concentration remains at 50 μ M (Figure 1-figure supplement
1235 3e). This result shows that equations (S2)-(S3) can be used to accurately measure the
1236 concentrations of free and bound NADH from FLIM measurements of NADH.

1237 1238 **Appendix 2**

1239 1240 **Reversible Michaelis-Menten kinetics, full and reduced notations**

1241
1242 The kinetic equations of the reversible Michaelis-Menten kinetics (Figure 3a, left) for the i th
1243 oxidase are

$$1244 \frac{d[\text{NADH}_f]}{dt} = k_{-1}[\text{NADH} \cdot \text{Ox}_i] - k_1[\text{Ox}_i][\text{NADH}_f] \quad (\text{S5}),$$

$$1245 \frac{d[\text{NADH} \cdot \text{Ox}_i]}{dt} = k_1[\text{Ox}_i][\text{NADH}_f] - k_{-1}[\text{NADH} \cdot \text{Ox}_i] + k_{-2}[\text{Ox}_i][\text{NAD}_f^+] - k_2[\text{NADH} \cdot$$

$$1246 \text{Ox}_i] \quad (\text{S6}),$$

$$1247 \frac{d[\text{NAD}_f^+]}{dt} = k_2[\text{NADH} \cdot \text{Ox}_i] - k_{-2}[\text{Ox}_i][\text{NAD}_f^+] \quad (\text{S7}),$$

$$1248 \frac{d[\text{Ox}_i]}{dt} = k_{-1}[\text{NADH} \cdot \text{Ox}_i] - k_1[\text{Ox}_i][\text{NADH}_f] + k_2[\text{NADH} \cdot \text{Ox}_i] - k_{-2}[\text{Ox}_i][\text{NAD}_f^+] \quad (\text{S8}).$$

1249
1250 Where $[\text{NADH}_f]$ is the concentration of free NADH, $[\text{NAD}_f^+]$ is the concentration of free NAD^+ ,
1251 $[\text{Ox}_i]$ is the concentration of free oxidase, and $[\text{NADH} \cdot \text{ox}_i]$ is the concentration of the NADH-
1252 oxidase complex. k_{-1} , k_1 , k_{-2} , and k_2 are the forward and reverse reaction rates.

1253
1254 In the reduced notation as introduced in Figure 3a (right), the same enzyme kinetics is described
1255 by

$$1256 \frac{d[\text{NADH}_f]}{dt} = k_{\text{ox}_i}^u[\text{NADH} \cdot \text{Ox}_i] - k_{\text{ox}_i}^b[\text{NADH}_f] \quad (\text{S9}),$$

$$1257 \frac{d[\text{NADH} \cdot \text{Ox}_i]}{dt} = k_{\text{ox}_i}^b[\text{NADH}_f] - k_{\text{ox}_i}^u[\text{NADH} \cdot \text{Ox}_i] + k_{\text{ox}_i}'^b[\text{NAD}_f^+] - k_{\text{ox}_i}'^u[\text{NADH} \cdot \text{Ox}_i] \quad (\text{S10}),$$

1260 $\frac{d[\text{NAD}_f^+]}{dt} = k_{\text{ox}_i}^u [\text{NADH} \cdot \text{Ox}_i] - k_{\text{ox}_i}^b [\text{NAD}_f^+] \text{ (S11)},$

1261

1262 Where $k_{\text{ox}_i}^b$ and $k_{\text{ox}_i}^u$ are the effective binding and unbinding rates of NADH to the oxidase, and
 1263 $k_{\text{ox}_i}^b$ and $k_{\text{ox}_i}^u$ are the effective binding and unbinding rates of NAD^+ to the oxidase. In this
 1264 reduced notation, the concentration of the free oxidase $[\text{Ox}_i]$ is absorbed into the effective
 1265 binding rates: i.e. $k_{\text{ox}_i}^u = k_{-1}$, $k_{\text{ox}_i}^b = k_1[\text{Ox}_i]$, $k_{\text{ox}_i}^u = k_2$ and $k_{\text{ox}_i}^b = k_{-2}[\text{Ox}_i]$. Hence $[\text{Ox}_i]$
 1266 becomes an implicit variable whose behavior is not evident from the reduced notation diagram
 1267 (Figure 3a, right). Modeling the full dynamics of a reversible Michaelis-Menten enzyme requires
 1268 specifying the equation for $[\text{Ox}_i]$:
 1269

1270 $\frac{d[\text{Ox}_i]}{dt} = k_{-1} [\text{NADH} \cdot \text{Ox}_i] - k_1 [\text{Ox}_i] [\text{NADH}_f] + k_2 [\text{NADH} \cdot \text{Ox}_i] - k_{-2} [\text{Ox}_i] [\text{NAD}_f^+] \text{ (S12)}.$

1271

1272 The reduced notation (Figure 3a, right; Equations S9 – S12) and the full notation (Figure 3a, left;
 1273 Equations S5-S8) are mathematically identical and describe the exact same kinetics.
 1274

1274

1275 **Generalized enzyme kinetics, reduced notation**

1276

1277 The reduced notation for the i th oxidase displaying generalized enzyme kinetics (Figure 3b)
 1278 refers to the following class of mathematical models:
 1279

1280 $\frac{d[\text{NADH}_f]}{dt} = k_{\text{ox}_i}^u [\text{NADH} \cdot \text{Ox}_i] - k_{\text{ox}_i}^b [\text{NADH}_f] \text{ (S13)},$

1281 $\frac{d[\text{NADH} \cdot \text{Ox}_i]}{dt} = k_{\text{ox}_i}^b [\text{NADH}_f] - k_{\text{ox}_i}^u [\text{NADH} \cdot \text{Ox}_i] - r_{\text{ox}_i}^+ [\text{NADH} \cdot \text{Ox}_i] + r_{\text{ox}_i}^- [\text{NAD}^+ \cdot \text{Ox}_i] \text{ (S14)},$

1282 $\frac{d[\text{NAD}^+ \cdot \text{Ox}_i]}{dt} = r_{\text{ox}_i}^+ [\text{NADH} \cdot \text{Ox}_i] - r_{\text{ox}_i}^- [\text{NAD}^+ \cdot \text{Ox}_i] - k_{\text{ox}_i}^u [\text{NAD}^+ \cdot \text{Ox}_i] + k_{\text{ox}_i}^b [\text{NAD}_f^+] \text{ (S15)},$

1283 $\frac{d[\text{NAD}_f^+]}{dt} = k_{\text{ox}_i}^u [\text{NAD}^+ \cdot \text{Ox}_i] - k_{\text{ox}_i}^b [\text{NAD}_f^+] \text{ (S16)}.$

1284

1285 Where $[\text{NADH}_f]$ is the concentration of free NADH, $[\text{NAD}_f^+]$ is the concentration of free NAD^+ ,
 1286 $[\text{Ox}_i]$ is the concentration of free oxidase, $[\text{NADH} \cdot \text{Ox}_i]$ is the concentration of the NADH-
 1287 oxidase complex, and $[\text{NAD}^+ \cdot \text{Ox}_i]$ is the concentration of the NAD^+ -oxidase complex. $k_{\text{ox}_i}^b$ and
 1288 $k_{\text{ox}_i}^u$ are the effective binding and unbinding rates of NADH to the oxidase, $k_{\text{ox}_i}^b$ and $k_{\text{ox}_i}^u$ are the
 1289 effective binding and unbinding rates of NAD^+ to the oxidase, and $r_{\text{ox}_i}^+$ and $r_{\text{ox}_i}^-$ are the forward
 1290 and reverse oxidation rates. These rates can be arbitrary functions of implicit variables, such as
 1291 the concentration of free oxidase, $[\text{Ox}_i]$, the mitochondrial membrane potential, ΔG_H , pH, and
 1292 other factors:
 1293

1294 $k_{\text{ox}_i}^u = k_{\text{ox}_i}^u([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17a)}$

1294 $k_{\text{ox}_i}^b = k_{\text{ox}_i}^b([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17b)}$

1295 $r_{\text{ox}_i}^+ = r_{\text{ox}_i}^+([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17c)}$

1296 $r_{\text{ox}_i}^- = r_{\text{ox}_i}^-([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17d)}$

1297 $k_{\text{ox}_i}^u = k_{\text{ox}_i}^u([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17e)}$

1297 $k_{\text{ox}_i}^b = k_{\text{ox}_i}^b([\text{Ox}_i], \Delta G_H, \text{pH}, [\text{NADH}_f], \dots) \text{ (S17f)}$

1298

1299 Thus, while Equations S13-S16 superficially appear to be linear and first order, they can actually
 1300 refer to non-linear reactions of any order because the rate can depend on $[\text{NADH}_f]$ and other
 1301 variables (Equations S17).

1302
 1303 The implicit variables that these rates depend on can each be governed by their own dynamics
 1304 that are arbitrary functions of other variables:
 1305

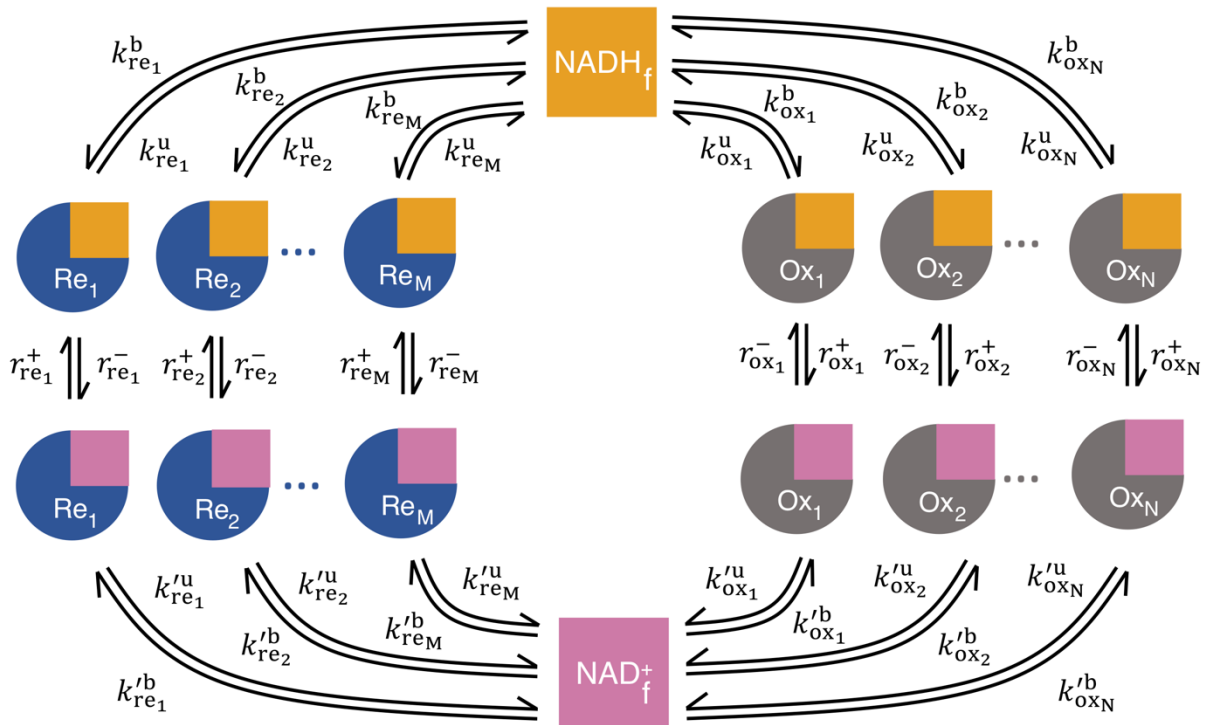
1306
$$\frac{d[\text{Ox}_i]}{dt} = \dots; \frac{d[\Delta G_H]}{dt} = \dots; \frac{d[\text{pH}]}{dt} = \dots; \text{etc. (S18)}$$

1307
 1308 Describing the dynamics of the enzyme requires specifying the implicit variables that the rates
 1309 depend on, the functional form of these dependencies, and the additional equations for the
 1310 dynamics of the implicit variables (Equations S18). However, we will show that the predicted
 1311 relationship between FLIM measurements of NADH and fluxes do not depend on these
 1312 modeling choices. Thus, the reduced notation is convenient for deriving these relations for a
 1313 broad class of models.

1314
 1315 **Appendix 3**

1316
 1317 **Coarse-graining the detailed NADH redox model**

1318



1319
 1320 **Figure 4-figure supplement 1| The detailed NADH redox model.** The model consists of redox loops with N
 1321 oxidases and M reductases. Each of the oxidase and reductase follows the generalized enzyme kinetics. The binding
 1322 and unbinding rate of NADH to the i th oxidase (reductase) is $k_{ox_i}^b$ and $k_{ox_i}^u$ ($k_{re_i}^b$ and $k_{re_i}^u$). The binding and
 1323 unbinding rate of NAD⁺ to the i th oxidase (reductase) is $k_{ox_i}^{b'}$ and $k_{ox_i}^{u'}$ ($k_{re_i}^{b'}$ and $k_{re_i}^{u'}$). Once bound, the forward and
 1324 reverse reaction rates are $r_{ox_i}^+$ and $r_{ox_i}^-$ for the i th oxidase; $r_{re_i}^+$ and $r_{re_i}^-$ for the i th reductase. All rates can be

1325 arbitrary functions of metabolite concentrations, enzyme concentrations, and other factors (such as pH and
 1326 mitochondrial membrane potential).

1327
 1328 We consider an NADH redox loop consisting of M reductases and N oxidases (Figure 4-figure
 1329 supplement 1), each of which is described by the generalized enzyme kinetics (Figure 3b;
 1330 Equations S13-S16). We coarse-grain this detailed NADH redox model by coarse-graining all
 1331 oxidases into a single effective oxidase and all reductases into a single effective reductase
 1332 (Figure 4b). We relate the kinetic rates of the coarse-grained model to those of the detailed
 1333 model by keeping the global binding and unbinding fluxes and the global reaction fluxes through
 1334 the oxidases and reductases the same as the detailed model.

1335
 1336 We first coarse-grain the oxidases and reductases:
 1337

$$[\text{NADH} \cdot \text{Ox}] = \sum_{i=1}^N [\text{NADH} \cdot \text{Ox}_i], \quad [\text{NADH} \cdot \text{Re}] = \sum_{i=1}^M [\text{NADH} \cdot \text{Re}_i] \quad (\text{S19})$$

1338
 1339 We require the global binding and unbinding fluxes of NADH to the effective oxidase and
 1340 reductase to be equal to the sum of their binding and unbinding fluxes to all of the individual
 1341 oxidases and reductases:
 1342

$$J_{\text{ox}}^b = [\text{NADH}_f] \sum_{i=1}^N k_{\text{ox}_i}^b = k_{\text{ox}}^b [\text{NADH}_f] \quad (\text{S20}),$$

$$J_{\text{ox}}^u = \sum_{i=1}^N k_{\text{ox}_i}^u [\text{NADH} \cdot \text{Ox}_i] = k_{\text{ox}}^u [\text{NADH} \cdot \text{Ox}] \quad (\text{S21}),$$

$$J_{\text{re}}^b = [\text{NADH}_f] \sum_{i=1}^M k_{\text{re}_i}^b = k_{\text{re}}^b [\text{NADH}_f] \quad (\text{S22}),$$

$$J_{\text{re}}^u = \sum_{i=1}^M k_{\text{re}_i}^u [\text{NADH} \cdot \text{Re}_i] = k_{\text{re}}^u [\text{NADH} \cdot \text{Re}] \quad (\text{S23}),$$

1343
 1344 which leads to

$$k_{\text{ox}}^b = \sum_{i=1}^N k_{\text{ox}_i}^b, \quad k_{\text{re}}^b = \sum_{i=1}^M k_{\text{re}_i}^b \quad (\text{S24}),$$

$$k_{\text{ox}}^u = \sum_{i=1}^N k_{\text{ox}_i}^u \frac{[\text{NADH} \cdot \text{Ox}_i]}{[\text{NADH} \cdot \text{Ox}]}, \quad k_{\text{re}}^u = \sum_{i=1}^M k_{\text{re}_i}^u \frac{[\text{NADH} \cdot \text{Re}_i]}{[\text{NADH} \cdot \text{Re}]} \quad (\text{S25}).$$

1345
 1346 We require the global forward and reverse reaction flux through the effective oxidase and
 1347 reductase to be equal to the sum of the reaction fluxes through all of the individual oxidases and
 1348 reductases:
 1349

$$J_{\text{ox}}^+ = \sum_{i=1}^N r_{\text{ox}_i}^+ [\text{NADH} \cdot \text{Ox}_i] = r_{\text{ox}}^+ [\text{NADH} \cdot \text{Ox}] \quad (\text{S26}),$$

$$J_{\text{ox}}^- = \sum_{i=1}^N r_{\text{ox}_i}^- [\text{NAD}^+ \cdot \text{Ox}_i] = r_{\text{ox}}^- [\text{NAD}^+ \cdot \text{Ox}] \quad (\text{S27}),$$

1350 which leads to
1351

$$r_{\text{ox}}^+ = \sum_{i=1}^N r_{\text{ox}_i}^+ \frac{[\text{NADH} \cdot \text{Ox}_i]}{[\text{NADH} \cdot \text{Ox}]} \quad (\text{S28}),$$

$$r_{\text{ox}}^- = \sum_{i=1}^N r_{\text{ox}_i}^- \frac{[\text{NAD}^+ \cdot \text{Ox}_i]}{[\text{NAD}^+ \cdot \text{Ox}]} \quad (\text{S29}).$$

1352
1353 By applying the same procedure to NAD^+ , we can obtain the effective reduction rates r_{re}^+ , r_{ox}^-
1354 and the effective binding and unbinding rates of NAD^+ : k_{ox}^{b} , k_{re}^{b} , k_{ox}^{u} , k_{re}^{u} . We omit the
1355 derivation here because these rates are not needed to infer ETC flux. We hence explicitly related
1356 the kinetic rates of the coarse-grained model (Figure 4b) to those of the detailed model (Figure 4-
1357 figure supplement 1). We note that under the generalized enzyme kinetics (Figure 3b; Equations
1358 S13-S16), all kinetic rates are considered to be general functions of enzyme concentrations,
1359 metabolite concentrations and other factors, and thus, all of the rates in the coarse-grained model
1360 can also depend on all of those factors. These implicit variables can obey their own dynamical
1361 equations (S18). The coarse-graining presented here is mathematically exact and independent of
1362 both the functional forms of these rates and the functional form of the dynamic equations of the
1363 implicit variables.

1364 Appendix 4 1365

1366 Predicting the ETC flux using the coarse-grained NADH redox model 1367

1368 The coarse-grained NADH redox model 1369

1370 We start with the equations characterizing the dynamics of the coarse-grained NADH redox
1371 model as described in Figure 4b:
1372

$$1373 \frac{d[\text{NADH} \cdot \text{Re}]}{dt} = k_{\text{re}}^{\text{b}} [\text{NADH}_f] - k_{\text{re}}^{\text{u}} [\text{NADH} \cdot \text{Re}] + r_{\text{re}}^+ [\text{NAD}^+ \cdot \text{Re}] - r_{\text{re}}^- [\text{NADH} \cdot \text{Re}] \quad (\text{S30}),$$

$$1374 \frac{d[\text{NADH}_f]}{dt} = k_{\text{re}}^{\text{u}} [\text{NADH} \cdot \text{Re}] + k_{\text{ox}}^{\text{u}} [\text{NADH} \cdot \text{Ox}] - k_{\text{re}}^{\text{b}} [\text{NADH}_f] - k_{\text{ox}}^{\text{b}} [\text{NADH}_f] \quad (\text{S31}),$$

$$1375 \frac{d[\text{NADH} \cdot \text{Ox}]}{dt} = k_{\text{ox}}^{\text{b}} [\text{NADH}_f] - k_{\text{ox}}^{\text{u}} [\text{NADH} \cdot \text{Ox}] - r_{\text{ox}}^+ [\text{NADH} \cdot \text{Ox}] + r_{\text{ox}}^- [\text{NAD}^+ \cdot \text{Ox}] \quad (\text{S32}),$$

$$1376 \frac{d[\text{NAD}^+ \cdot \text{Ox}]}{dt} = k_{\text{ox}}^{\text{b}} [\text{NAD}_f^+] - k_{\text{ox}}^{\text{u}} [\text{NAD}^+ \cdot \text{Ox}] + r_{\text{ox}}^+ [\text{NADH} \cdot \text{Ox}] - r_{\text{ox}}^- [\text{NAD}^+ \cdot \text{Ox}] \quad (\text{S33}),$$

$$1377 \frac{d[\text{NAD}_f^+]}{dt} = k_{\text{re}}^{\text{u}} [\text{NAD}^+ \cdot \text{Re}] + k_{\text{ox}}^{\text{u}} [\text{NAD}^+ \cdot \text{Ox}] - k_{\text{re}}^{\text{b}} [\text{NAD}_f^+] - k_{\text{ox}}^{\text{b}} [\text{NAD}_f^+] \quad (\text{S34}),$$

$$1378 \frac{d[\text{NAD}^+ \cdot \text{Re}]}{dt} = k_{\text{re}}^{\text{b}} [\text{NAD}_f^+] - k_{\text{re}}^{\text{u}} [\text{NAD}^+ \cdot \text{Re}] - r_{\text{re}}^+ [\text{NAD}^+ \cdot \text{Re}] + r_{\text{re}}^- [\text{NADH} \cdot \text{Re}] \quad (\text{S35}),$$

1380

1381 where $[\text{NADH}_f]$ and $[\text{NAD}_f^+]$ are the concentrations of free NADH and free NAD^+ ; $[\text{NADH} \cdot \text{Re}]$
1382 and $[\text{NAD}^+ \cdot \text{Re}]$ are concentrations of reductase-bound NADH and NAD^+ ; $[\text{NADH} \cdot \text{Ox}]$ and
1383 $[\text{NAD}^+ \cdot \text{Ox}]$ are concentrations of oxidase-bound NADH and NAD^+ ; k denotes binding (b) and
1384 unbinding (u) rates, with subscript re and ox denoting reductase and oxidase, respectively; r_{re}^+
1385 and r_{re}^- are the forward and reverse reaction rates of the reductase; r_{ox}^+ and r_{ox}^- are the forward
1386 and reverse reaction rates of the oxidase. The reaction rates, and binding and unbinding rates, can
1387 be arbitrary functions of metabolite concentrations, enzyme concentrations, and other variables
1388 (such as membrane potential, oxygen concentration, etc, each of which can obey their own
1389 dynamical equations).

1390

1391 **Predicting the ETC flux**

1392

1393 The flux through the ETC is

1394

$$J_{\text{ox}} \equiv r_{\text{ox}}^+[\text{NADH} \cdot \text{Ox}] - r_{\text{ox}}^-[\text{NAD}^+ \cdot \text{Ox}] \quad (\text{S36}).$$

1395

1396 At steady state (or in the quasistatic limit), all the time derivatives are zero. Setting
1397 $d[\text{NADH} \cdot \text{Ox}]/dt$ (equation (S32)) to zero, we obtained the steady state flux through the ETC:

1398

$$J_{\text{ox}} = k_{\text{ox}}^b[\text{NADH}_f] - k_{\text{ox}}^u[\text{NADH} \cdot \text{Ox}] \quad (\text{S37}).$$

1400

1401 Setting $d[\text{NADH}_f]/dt$ (equation (S31)) to zero gives:

1402

$$(k_{\text{ox}}^b + k_{\text{re}}^b)[\text{NADH}_f] = k_{\text{ox}}^u[\text{NADH} \cdot \text{Ox}] + k_{\text{re}}^u[\text{NADH} \cdot \text{Re}] \quad (\text{S38}).$$

1403

1404 and using:

1405

$$[\text{NADH} \cdot \text{Re}] + [\text{NADH} \cdot \text{Ox}] = [\text{NADH}_b] \quad (\text{S39}),$$

1406

1407 from which we solved for $[\text{NADH} \cdot \text{Ox}]$:

1408

1409

$$[\text{NADH} \cdot \text{Ox}] = \frac{k_{\text{re}}^b + k_{\text{ox}}^b}{k_{\text{ox}}^u - k_{\text{re}}^u} [\text{NADH}_f] - \frac{k_{\text{re}}^u}{k_{\text{ox}}^u - k_{\text{re}}^u} [\text{NADH}_b] \quad (\text{S40}).$$

1410

1411 Substituting $[\text{NADH} \cdot \text{Ox}]$ in equation (S37) with equation (S40), we obtained our central result:

1412

$$J_{\text{ox}} = \tilde{r}_{\text{ox}} [\text{NADH}_f] \quad (\text{S41}).$$

1413

1414 From equation (S41) we see that the flux through the ETC is a product of the turnover rate of
1415 free NADH, \tilde{r}_{ox} , and the concentration of free NADH, $[\text{NADH}_f]$, where

1416

1417

$$\tilde{r}_{\text{ox}} = \alpha(\beta - \beta_{\text{eq}}) \quad (\text{S42}),$$

1418

1419 and

$$\alpha = \frac{k_{\text{ox}}^u k_{\text{re}}^u}{k_{\text{ox}}^u - k_{\text{re}}^u} \quad (\text{S43}),$$

1422
 1423 where we defined the NADH bound ratio and its equilibrium counterpart as:
 1424

$$\beta = \frac{[\text{NADH}_b]}{[\text{NADH}_f]} \quad (\text{S44}),$$

$$\beta_{\text{eq}} = \beta_{\text{eq}}^{\text{ox}} + \beta_{\text{eq}}^{\text{re}} \quad (\text{S45}),$$

$$\beta_{\text{eq}}^{\text{ox}} = \frac{k_{\text{ox}}^b}{k_{\text{ox}}^u} \quad (\text{S46}),$$

$$\beta_{\text{eq}}^{\text{re}} = \frac{k_{\text{re}}^b}{k_{\text{re}}^u} \quad (\text{S47}).$$

1427
 1428 **Appendix 5**

1429
 1430 **Flux inference procedures using the coarse-grained NADH redox model**

1431
 1432 Equations (S41-S42), or equivalently equations 5a-c from the main text, can be used to infer the
 1433 flux through the ETC, J_{ox} , from FLIM measurements of NADH across a wide range of
 1434 metabolic perturbations (Figure 5-figure supplement 1). To do so, we infer the turnover rate of
 1435 free NADH, \tilde{r}_{ox} , and the concentration of free NADH, $[\text{NADH}_f]$. The product of \tilde{r}_{ox} and
 1436 $[\text{NADH}_f]$ gives J_{ox} . $[\text{NADH}_f]$ can be obtained using equation (S2) (Figure 5-figure supplement
 1437 1e). In this section, we describe two procedures to obtain \tilde{r}_{ox} : one from the measurement of
 1438 NADH bound ratio β , and the other from the measurement of NADH long fluorescence lifetime
 1439 τ_1 .

1440
 1441 **Inferring \tilde{r}_{ox} from NADH bound ratio β**

1442
 1443 Equation (S42), $\tilde{r}_{\text{ox}} = \alpha(\beta - \beta_{\text{eq}})$, provides a method to obtain \tilde{r}_{ox} . We measure the NADH
 1444 bound ratio, β , using $\beta = f/(1 - f)$, where f is the NADH bound fraction obtained by fitting
 1445 the fluorescence decay curve of NADH (See Methods). We obtain the equilibrium bound ratio,
 1446 β_{eq} , by dropping the oxygen level to the lowest achievable value with our setup: $[\text{O}_2] = 0.26 \pm$
 1447 $0.04 \mu\text{M}$, and assuming β_{eq} does not change with oxygen levels. Note that β_{eq} does change with
 1448 drug perturbations, and therefore needs to be separately determined for each condition (Figure 5-
 1449 figure supplement 1h). We obtain α using direct measurement of J_{ox} from oxygen consumption
 1450 rate (OCR) measurements:

$$\alpha = \frac{J_{\text{ox}}}{(\beta - \beta_{\text{eq}})[\text{NADH}_f]} = 2 \frac{\text{OCR}}{(\beta - \beta_{\text{eq}})[\text{NADH}_f]V_m} \quad (\text{S48}),$$

1451
 1452 where $V_m = 9.5 \times 10^4 \mu\text{m}^3$ is the average volume of mitochondria per oocyte approximated
 1453 from the area fraction of mitochondria based on the segmentation, where the mitochondrial area
 1454 fraction is estimated at 46% and oocyte volume at $2 \times 10^5 \mu\text{m}^3$. Using $\text{OCR} = 2.68 \pm 0.06 \text{ fmol/s}$
 1455 per oocyte in the control condition (AKSOM media at $50 \mu\text{M}$ oxygen level), we get $\alpha = 5.4 \pm$
 1456 0.2 s^{-1} . α is approximated as a constant that does not vary with perturbations, hence α calibrated
 1457

1458 at one condition can be used for all other conditions (as confirmed by the agreement between
1459 FLIM based inference and OCR measurements in Figure 5 and 8).

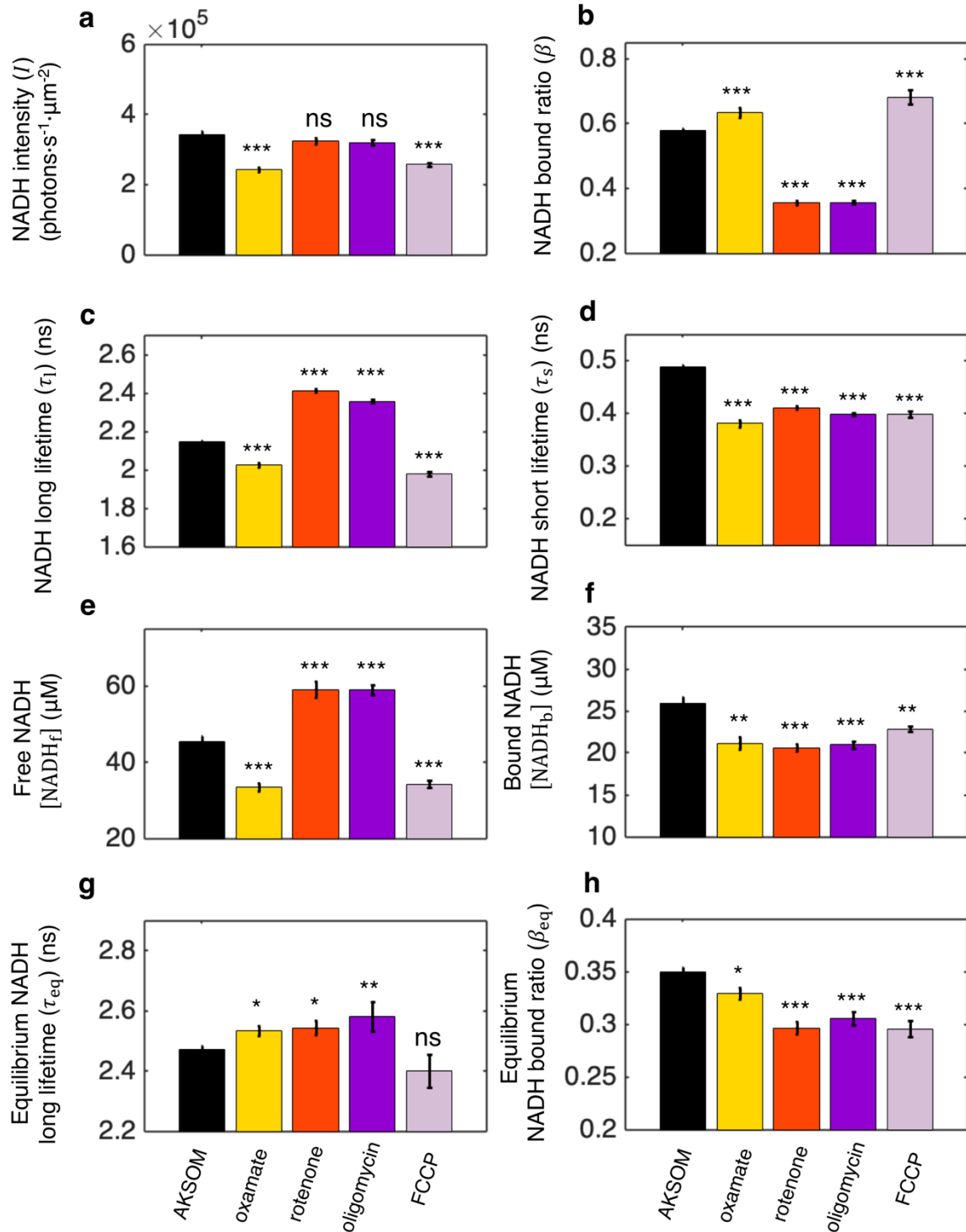
1460

1461 Once α is calibrated at the control condition using equation (S48), and β_{eq} is determined from an
1462 oxygen drop experiment, then subsequent FLIM measurements of β and $[\text{NADH}_f]$ can be used
1463 with equation (S42) and (S41) to determine the absolute value of \tilde{r}_{ox} and J_{ox} for all conditions
1464 (Figure 5).

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Figure 5-figure supplement 1 | FLIM measurements of NADH in mitochondria under different biochemical perturbations. **a**, NADH intensity. **b-d**, NADH bound ratio and NADH long and short fluorescence lifetimes obtained from fitting FLIM decay curves using the two-exponential decay model (Method). **e-f**, free and bound NADH concentrations obtained by using equations (S2) and (S3), and the calibration from equation (S4). **g-h**, Equilibrium NADH long lifetime and bound ratio, measured at the lowest oxygen level under different conditions. 9 mM sodium oxamate was present in all conditions except for AKSOM to suppress the cytoplasmic signal for better

1476 mitochondrial segmentation. AKSOM (n=68), 9 mM oxamate (n=20), 5 μ M rotenone (n=28), 5 μ M oligomycin
 1477 (n=37) and 5 μ M FCCP (n=31). n is the number of oocytes. Error bars represent standard error of the mean (s.e.m).
 1478 Student's t-test is performed pairwise between perturbations and AKSOM condition. *p<0.05, **p<0.01,
 1479 ***p<0.001.

1480 **Figure 5-figure supplement 1 source data | Excel spreadsheet of single oocyte FLIM data used for Figure 5-**
 1481 **figure supplement 1a-h.**

1482

1483 **Inferring \tilde{r}_{ox} from NADH long fluorescence lifetime τ_1**

1484

1485 In this section, we derive an alternative procedure for determining the turnover rate of free
 1486 NADH \tilde{r}_{ox} , and hence J_{ox} , using changes in the NADH long fluorescence lifetime. The NADH
 1487 long fluorescence lifetime, τ_1 , is associated with enzyme-bound NADH (Sharick et al., 2018). In
 1488 the coarse-grained NADH redox model described above, and in Figure 4b, the enzyme-bound
 1489 NADH consists of reductase-bound NADH ([NADH · Re]) and oxidase-bound NADH ([NADH ·
 1490 Ox]). We therefore assume that the experimentally measured NADH long lifetime, τ_1 , is a linear
 1491 combination of the lifetimes of [NADH · Ox] and [NADH · Re]:

1492

$$1493 \quad \tau_1 = \tau_{\text{ox}} \frac{[\text{NADH} \cdot \text{Ox}]}{[\text{NADH} \cdot \text{Ox}] + [\text{NADH} \cdot \text{Re}]} + \tau_{\text{re}} \frac{[\text{NADH} \cdot \text{Re}]}{[\text{NADH} \cdot \text{Ox}] + [\text{NADH} \cdot \text{Re}]} \quad (\text{S49}),$$

1494

1495 where τ_{ox} and τ_{re} are the fluorescence lifetimes corresponding to the oxidase-bound NADH and
 1496 reductase-bound NADH, respectively. Solving for [NADH · Ox] and [NADH · Re] as a function
 1497 of β using equations (S39)-(S40) and (S44), and substituting into equation (S49), we predict that
 1498 the NADH long fluorescence lifetime τ_1 is linearly related to the inverse of the NADH bound
 1499 ratio $1/\beta$:

1500

$$1501 \quad \tau_1 = A \frac{1}{\beta} + B \quad (\text{S50}),$$

1502 with

$$1503 \quad A = (\tau_{\text{ox}} - \tau_{\text{re}}) \frac{k_{\text{ox}}^{\text{b}} + k_{\text{re}}^{\text{b}}}{k_{\text{o,u}} - k_{\text{r,u}}} \quad (\text{S51}),$$

$$1504 \quad B = \frac{k_{\text{ox}}^{\text{u}} \tau_{\text{re}} - k_{\text{re}}^{\text{u}} \tau_{\text{ox}}}{k_{\text{ox}}^{\text{u}} - k_{\text{re}}^{\text{u}}} \quad (\text{S52}).$$

1505

1506 The predicted linear relationship between τ_1 and $1/\beta$ is empirically observed during oxygen drop
 1507 experiments, as shown in Figure 6a and Figure 6-figure supplement 1. This is a self-consistency
 1508 check that argues for the validity of the assumption in equation (S49).

1509

1510 At equilibrium, when there is no flux through the ETC (i.e. $J_{\text{ox}} = 0$), equation (S50) gives:

1511

$$1512 \quad \tau_{\text{eq}} = A \frac{1}{\beta_{\text{eq}}} + B \quad (\text{S53}),$$

1513

1514 where τ_{eq} is the NADH long lifetime at equilibrium. Solving for β and β_{eq} as a function of τ_1
 1515 and τ_{eq} from equations (S50) and (S53) and substituting into equation (S42), we obtain \tilde{r}_{ox} in
 1516 terms of τ_1 :

1517

1518

$$\tilde{\tau}_{\text{ox}} = \alpha \frac{A}{\tau_{\text{eq}} - B} \left(\frac{\tau_{\text{eq}} - \tau_1}{\tau_1 - B} \right) \quad (\text{S54}),$$

1519

1520 where A and B are the slope and offset of the linear relation between τ_1 and $1/\beta$ in equation
1521 (S50).

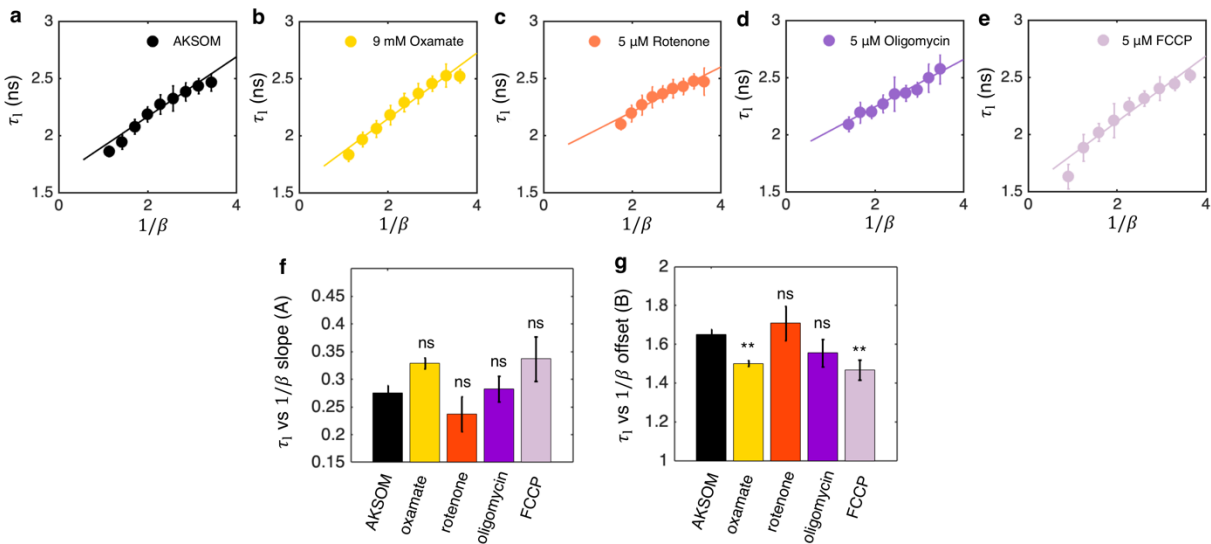
1522

1523 We experimentally measured A and B for each oocyte from the slope and offset of a linear fit
1524 between τ_1 and $1/\beta$ during oxygen drop experiments across all drug perturbations (Figure 6a;
1525 Figure 6-figure supplement 1). We obtained the equilibrium long lifetime, τ_{eq} , by FLIM
1526 measurements at the lowest achievable oxygen level in our set up: $[\text{O}_2] = 0.26 \pm 0.04 \mu\text{M}$. Once
1527 A , B , and τ_{eq} are measured, equation (S54) can be used to determine $\tilde{\tau}_{\text{ox}}$ from FLIM
1528 measurements of τ_1 . If α is not known, this procedure can only be used to obtain $\tilde{\tau}_{\text{ox}}$ up to a
1529 constant of proportionality. If α is independently measured from equation (S48) at one condition,
1530 then equation (S54) can be used to determine the absolute value of $\tilde{\tau}_{\text{ox}}$ for all conditions (Figure
1531 6b).

1532

1533 As described in the main text, $\tilde{\tau}_{\text{ox}}$ inferred from τ_1 using equation (S54) produces the same
1534 results as $\tilde{\tau}_{\text{ox}}$ inferred from β using equation (S42) (Figure 6b). The agreement between these
1535 two methods is a strong self-consistency check of the NADH redox model.

1536



1537

1538

Figure 6-figure supplement 1 | NADH long fluorescence lifetime τ_1 is linearly related to the inverse of the NADH bound ratio $1/\beta$. a-e, τ_1 vs $1/\beta$ during oxygen drop for all drug perturbations and the corresponding linear fitting. The fitting is performed for each oocyte independently. The plot shows the average fitting across all oocytes. f-g, slope (A) and offset (B) obtained by fitting equation (S50) to τ_1 vs $1/\beta$. Student's t-test is performed pairwise between perturbations and AKSOM condition. Error bars represent standard error of the mean (s.e.m). *p<0.05, **p<0.01, ***p<0.001.

1539

1540 **Figure 6-figure supplement 1 source data | Excel spreadsheet of single oocyte FLIM data used for Figure 6-**
1541 **figure supplement 1f-g.**

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1546

1547 **Accounting for NADPH and other background fluorescence**

1548

1549 Equation (S41) provides a method to infer ETC flux since all factors in it, except for the constant
1550 of proportionality, α , depend only on $[\text{NADH}_b]$ and $[\text{NADH}_f]$, which can be measured from
1551 FLIM of NADH. One potential complication with this procedure is that NADPH, another
1552 autofluorescent electron carrier, shares a similar fluorescence spectrum with NADH, resulting in
1553 a mixed NAD(P)H signal from the autofluorescence measurement. While NADH concentration
1554 is 40 times greater than the concentration of NADPH for the whole mouse oocytes (Bustamante
1555 et al., 2017), and presumably even higher for mitochondria, NADPH concentration can be
1556 comparable to that of NADH for other cell types such as tissue culture cells (Park et al., 2016).
1557 In this section, we generalize equation (S41) to predict the ETC flux by explicitly considering the
1558 potential contributions of other fluorescence species, such as NADPH, to the measured
1559 autofluorescence signal.

1560

1561 We start from the fact that concentrations of bound and free fluorescent species measured from
1562 FLIM using Equations (S2)-(S3), $[\text{N}_f]$ and $[\text{N}_b]$, could be different from the actual
1563 concentrations of free and bound NADH, $[\text{NADH}_f]$ and $[\text{NADH}_b]$. If the signal from NADPH
1564 and other additional fluorescence species is additive, then:

1565

$$\begin{aligned} [\text{N}_f] &= [\text{NADH}_f] + C_f \text{ (S55),} \\ [\text{N}_b] &= [\text{NADH}_b] + C_b \text{ (S56),} \end{aligned}$$

1566

1567 where C_f and C_b are the non-NADH contributions to the measured concentrations of free and
1568 bound fluorescent species. We substitute equations (S55)-(S56) to the predicted ETC flux in
1569 equation (S41) and obtain

1570

$$J_{\text{ox}} = \alpha \left(\frac{[\text{N}_b] - C_b}{[\text{N}_f] - C_f} - \beta_{\text{eq}} \right) ([\text{N}_f] - C_f) \text{ (S57).}$$

1571

1572 Rearranging, we obtain

1573

$$J_{\text{ox}} = \alpha (\beta_{\text{N}} - \beta_{\text{N,eq}}) [\text{N}_f] \text{ (S58),}$$

1574

1575 where

1576

$$\begin{aligned} \beta_{\text{N}} &= \frac{[\text{N}_b]}{[\text{N}_f]} \text{ (S59),} \\ \beta_{\text{N,eq}} &= \beta_{\text{eq}} + \left(\frac{C_b}{C_f} - \beta_{\text{eq}} \right) \frac{C_f}{[\text{N}_f]} \text{ (S60).} \end{aligned}$$

1577

1578 Comparing equation (S58) with (S41), we notice that the background fluorescence does not
1579 change the form of the equation of the predicted ETC flux because the concentrations of the

1580 background fluorescent species are incorporated into the equilibrium bound ratio $\beta_{N,eq}$. If $\beta_{N,eq}$
 1581 can be reliably measured, the background fluorescence will not affect the flux inference
 1582 procedures. In other words, $[N_f]$ and $[N_b]$ can be used for flux inference in place of $[NADH_f]$ and
 1583 $[NADH_b]$ in Equations (S41)-(S42). Therefore, an additive offset to the measured concentrations
 1584 of free and bound species will not affect the flux inference procedure, whether that additive
 1585 offset comes from NADPH or from other sources of fluorescent background.

1586
 1587 Alternatively, if the signal from background fluorescence changes proportionally with NADH,
 1588 then:

$$[N_f] = [NADH_f] + C'_f[NADH_f] = (1 + C'_f)[NADH_f] \quad (S61),$$

$$[N_b] = [NADH_b] + C'_b[NADH_b] = (1 + C'_b)[NADH_b] \quad (S62),$$

1590 we have

$$J_{ox} = \alpha_N(\beta_N - \beta'_{N,eq})[N_f] \quad (S63),$$

1592
 1593 where

$$\alpha_N = \frac{\alpha}{1 + C'_b} \quad (S64),$$

$$\beta_N = \frac{[N_b]}{[N_f]} \quad (S65),$$

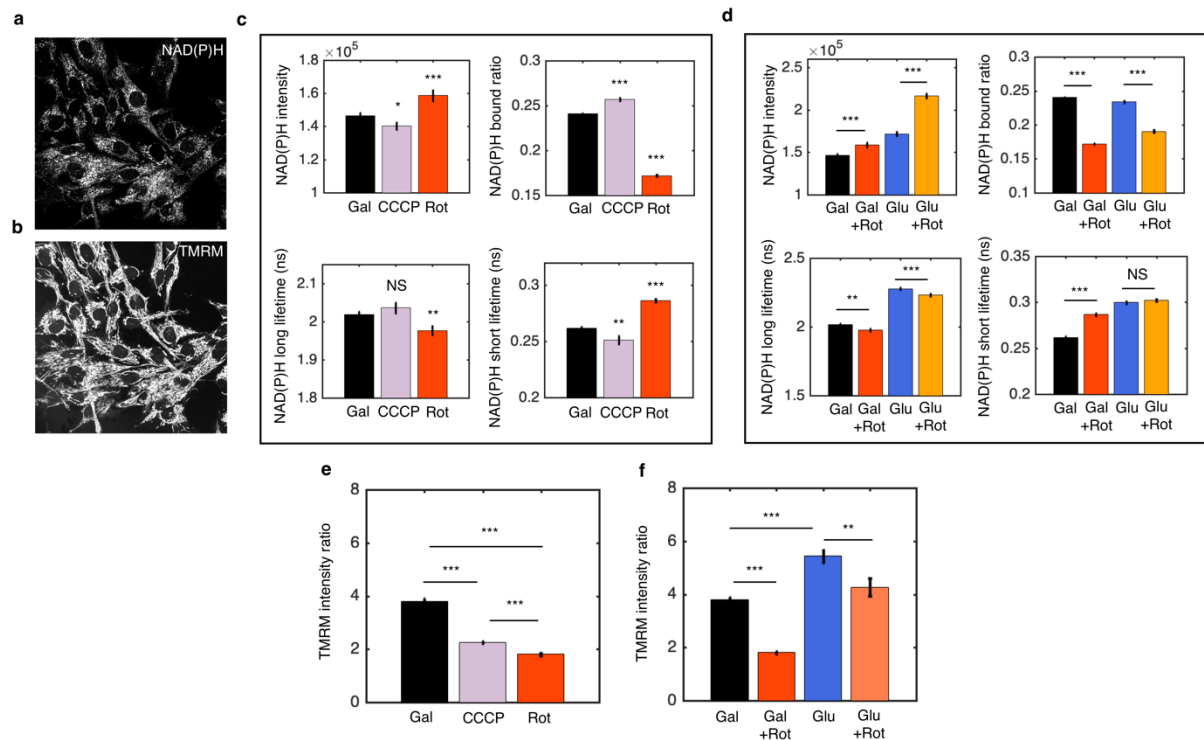
$$\beta'_{N,eq} = \frac{1 + C'_b}{1 + C'_f} \beta_{eq} \quad (S66).$$

1594
 1595 Comparing equation (S63) with (S41), we again obtained the same form for J_{ox} , but with a
 1596 rescaled α_N . Therefore, a background fluorescence signal that changes proportionally with
 1597 NADH will not affect the flux inference procedure, whether that background comes from
 1598 NADPH or from other sources.

1599
 1600 **Appendix 6**

1601
 1602 **NAD(P)H FLIM parameters and TMRM measurements for hTERT-RPE1**
 1603 **human tissue culture cells**

1604



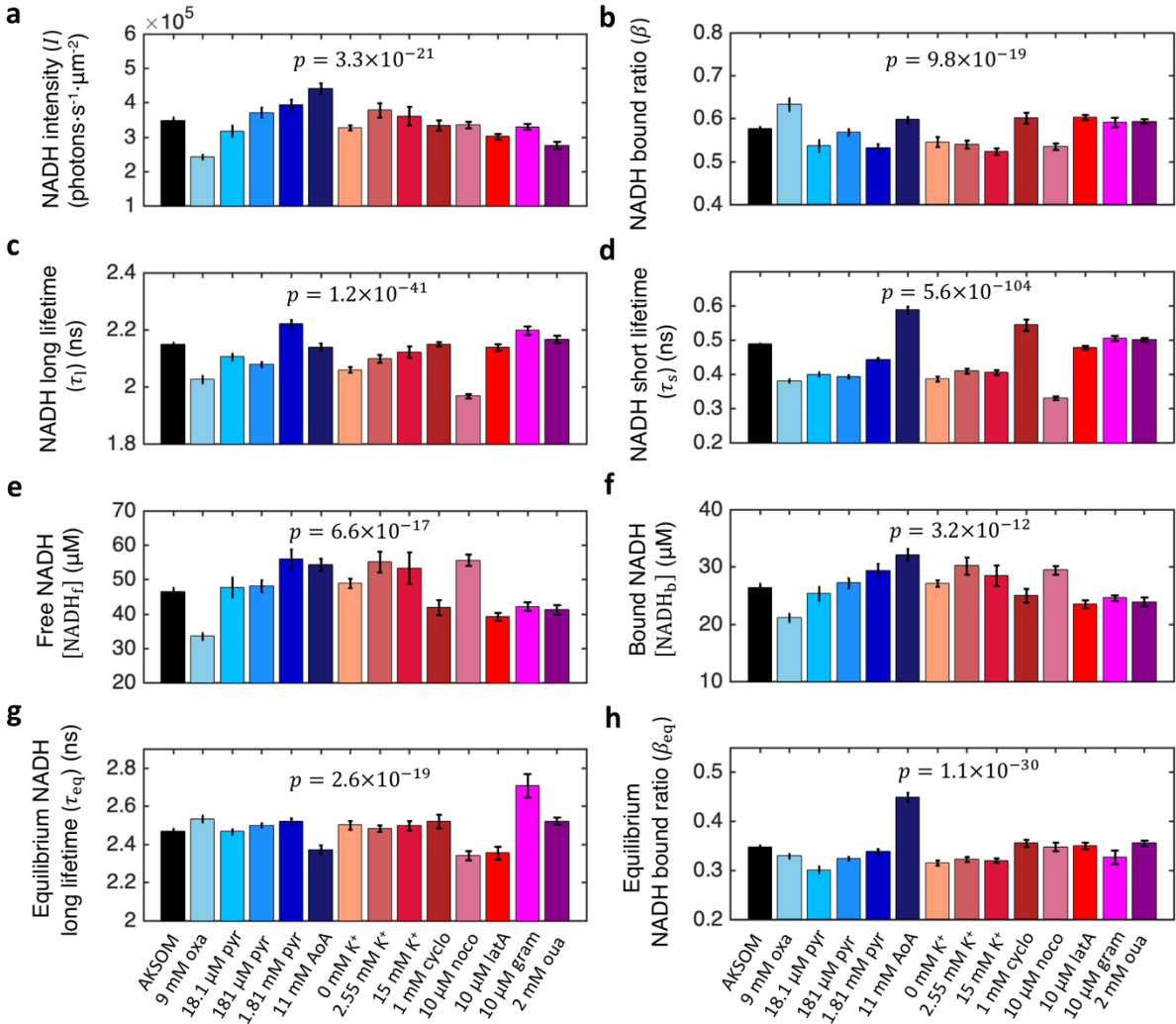
1605
 1606 **Figure 7-figure supplement 1 | NAD(P)H FLIM parameters in response to mitochondrial inhibitors and**
 1607 **nutrient perturbations for hTERT-RPE1 cells. a-b:** NAD(P)H intensity image (a) and TMRM intensity image (b)
 1608 for cells cultured in media with 10 mM galactose. **c:** NAD(P)H FLIM parameters with 8 μ M rotenone (N=61) and
 1609 3.5 μ M CCCP (N=72) added to the galactose media. Cells were imaged for 20-30 minutes immediately after the
 1610 drug perturbations. N specifies the number of images analyzed for each condition. A typical image contains dozens
 1611 of cells as shown in a-b. **d:** NAD(P)H FLIM parameters for cells growing in galactose media and in glucose media
 1612 and the respective 8 μ M rotenone perturbations. **e-f:** TMRM intensity ratio between mitochondria and cytoplasm
 1613 for drug and nutrient perturbations. Student's t-test is performed. * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$. Error bars
 1614 represent standard error of the mean (s.e.m) across different images.

1615
 1616 **Figure 7-figure supplement 1 source data | Excel spreadsheet of single image TMRM data used for Figure 7-**
 1617 **figure supplement 1e-f.**

1618
 1619 **Appendix 7**

1620
 1621 **NADH FLIM parameters for mouse oocytes in response to perturbing**
 1622 **nutrient supply and energy demand**

1623



1624
 1625 **Figure 8-figure supplement 1 | NADH FLIM parameters under all nutrient supply and energy demand**
 1626 **perturbations.** All FLIM parameters display significant changes in response to all nutrient supply and energy
 1627 demand perturbations. p value results from the ANOVA test. Number of oocytes: n=72, 20, 10, 49, 15, 18, 20, 20,
 1628 12, 10, 24, 18, 18, 62 in corresponding order from AKSOM to ouabain. Error bars represent standard error of the
 1629 mean (s.e.m) across different oocytes.

1630
 1631 **Figure 8-figure supplement 1 source data | Excel spreadsheet of single oocyte FLIM data used for Figure 8-**
 1632 **figure supplement 1a-h.**

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1642 **Appendix 8**

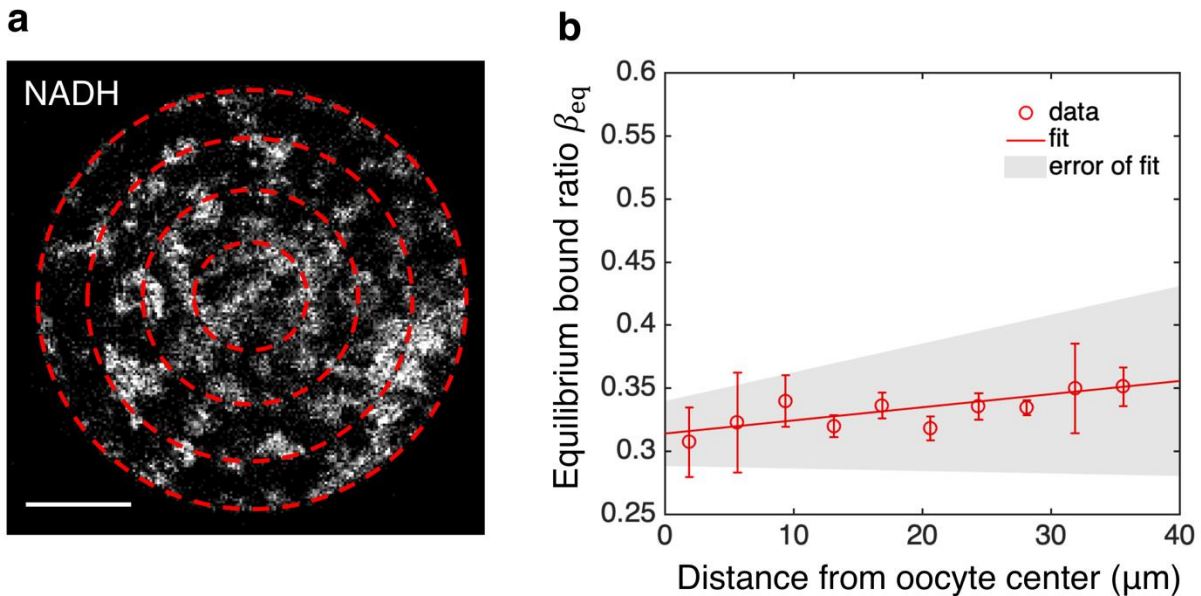
1643

1644 **Spatial gradient of mitochondrial metabolism in mouse oocytes**

1645

1646 β_{eq} is uniform within the oocyte

1647



1648

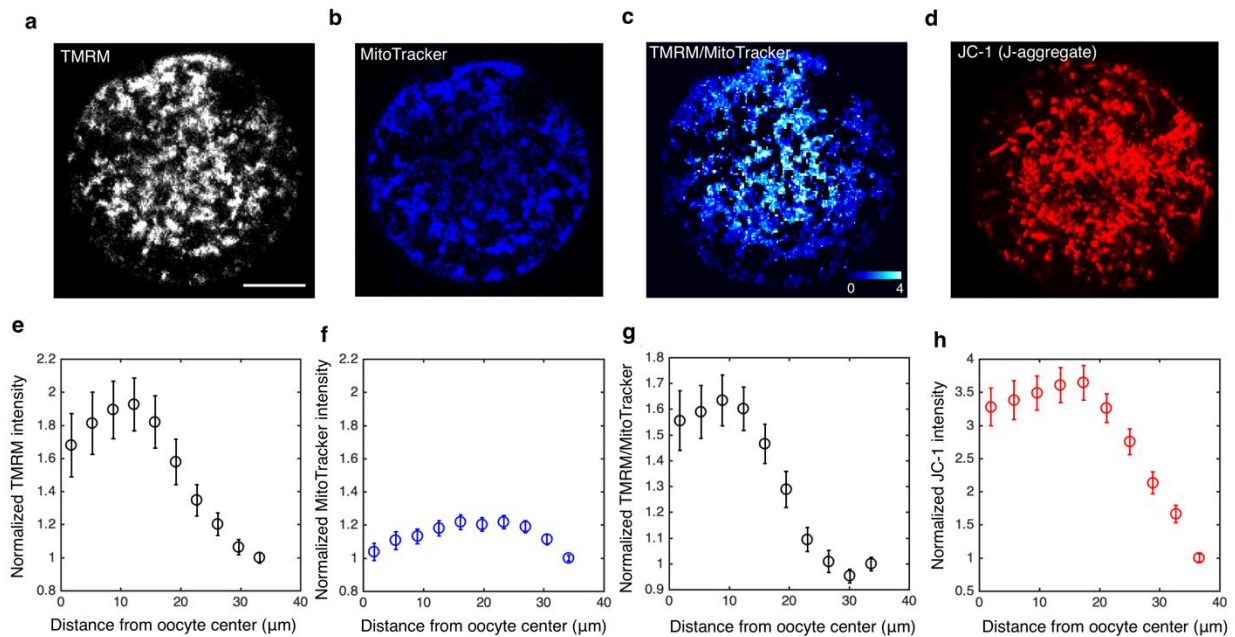
1649 **Figure 9-figure supplement 1 | β_{eq} is uniform within the oocyte.** **a**, NADH intensity image with oocyte
1650 partitioned by equal-distanced concentric rings. **b**, Equilibrium bound ratio β_{eq} as a function of distance from the
1651 oocyte's center obtained by completely inhibiting ETC with rotenone (n=10). The error bar denotes the SEM across
1652 individual oocyte. The line is from a linear fit of the data. The shaded region represents the error of fit from SEM of
1653 the slope and offset across 10 oocytes.

1654

1655 To obtain subcellular ETC flux as a function of distance to the oocyte's center using equations
1656 5a-c in the main text, we need to know the spatial variation of β_{eq} . While the NADH bound ratio
1657 at the lowest oxygen level gives a good approximation for the average β_{eq} of the cell (Figure 5-
1658 figure supplement 1h), subpopulations of mitochondria closer to the cell periphery are exposed to
1659 slightly higher oxygen level than those away from the cell periphery, obscuring the
1660 determination of the spatial variation of β_{eq} from oxygen drop experiment. Hence to obtain the
1661 spatial variation of β_{eq} throughout the oocyte, we inhibited the ETC completely using 15 μM of
1662 rotenone, an inhibitor of complex I in the ETC, for an extended period of time until the NADH
1663 bound ratio reaches the lowest level. We then fitted the NADH decay curves from mitochondrial
1664 pixels within equal-distanced concentric rings (Figure 9-figure supplement 1a) to obtain β_{eq} as
1665 a function of distance from the oocyte's center (Figure 9-figure supplement 1b). A linear fit
1666 yielded a slope of 0.001 ± 0.0012 (SEM), which is statistically indistinguishable from 0
1667 ($p=0.42$). Therefore, the resulting β_{eq} is uniform throughout the oocyte and is equal to the
1668 average β_{eq} obtained by fitting the decay curve from all mitochondrial pixels in the oocyte at the
1669 lowest oxygen level (Figure 5-figure supplement 1h). Hence, we used a constant β_{eq} throughout
1670 the oocyte to compute the subcellular ETC flux (Figure 9d).

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Subcellular spatial gradient of mitochondrial membrane potential



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Figure 9-figure supplement 2 | Subcellular spatial gradient of mitochondrial membrane potential. a-d, Intensity images of TMRM, MitoTracker Red FM, TMRM/MitoTracker ratio, JC-1 (J-aggregate). e-h, Normalized subcellular intensity gradient of the corresponding dyes as a function of distance from the oocyte's center (n=18 for each dye). The intensities are normalized by the intensity of the dye closest to the cell periphery.

1680 As shown in the main text, we observed a strong spatial gradient of the intensity of TMRM in
1681 mitochondria in oocytes. TMRM is a potential-sensitive dye that preferentially accumulates in
1682 mitochondria with higher membrane potential (Figure 9 g,h). To test whether this spatial gradient
1683 is due to the subcellular variation of mitochondrial membrane potential or the variation in
1684 mitochondrial mass, we labelled mitochondria with a potential-insensitive dye MitoTracker Red
1685 FM to quantify mitochondrial mass, together with TMRM. We did not observe a strong gradient
1686 of MitoTracker intensity (Figure 9-figure supplement 2b,f) as compared to TMRM intensity
1687 (Figure 9-figure supplement 2a,e) within the same oocyte, indicating the mitochondrial mass is
1688 uniformly distributed. We further normalized the TMRM intensity by the MitoTracker intensity,
1689 and observed a strong spatial gradient of the ratio (Figure 9-figure supplement 2c,g). These
1690 results suggest that the spatial gradient of TMRM is due to the variation of mitochondrial
1691 membrane potential, rather than the variation of mitochondrial mass. Finally, to test the
1692 robustness of the result, we used an alternative potential-sensitive dye JC-1, and observed a
1693 similar spatial gradient of mitochondrial membrane potential (Figure 9-figure supplement 2d,h).
1694 Taken together, these results show that the subcellular spatial gradient of mitochondrial
1695 membrane potential is a robust observation that does not depend on the variation of
1696 mitochondrial mass or the type of dye used.

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Appendix 9

Flux prediction for a NADH redox model with each enzyme described by the reversible Michaelis-Menten kinetics

In this section, we derive the ETC flux for a NADH redox model where each of the N oxidase and M reductase obeys reversible Michaelis-Menten kinetics (Equations S9-S11). We achieve this by reducing the flux prediction of the generalized enzyme kinetics to that of the reversible Michaelis-Menten kinetics.

We first consider an NADH redox model with a single oxidase and a single reductase, each of which obeys reversible Michaelis-Menten kinetics (i.e. N=M=1). The flux through the oxidase is:

$$J_{\text{ox}} = k_1[\text{Ox}_1][\text{NADH}_f] - k_{-1}[\text{NADH} \cdot \text{Ox}_1] \quad (\text{S67})$$

We show that equations (S41-S43) that characterize the flux of the generalized NADH redox model can be reduced to equation (S67) that characterizes the flux of the reversible Michaelis-Menten model in the limit:

$$k_{\text{re}}^u \gg k_{\text{ox}}^u, \quad k_{\text{re}}^u \gg k_{\text{re}}^b, \quad k_{\text{re}}^u \gg k_{\text{ox}}^b \quad (\text{S68}).$$

In this limit, we have from equation (S43):

$$\alpha \approx \alpha_{\text{MM}} = -k_{\text{ox}}^u = -k_{-1} \quad (\text{S69}),$$

where “MM” stands for “Michaelis-Menten”. Similarly, from equation (S45-S47) we have

$$\beta_{\text{eq}} \approx \beta_{\text{eq}}^{\text{MM}} = \frac{k_{\text{ox}}^b}{k_{\text{ox}}^u} = \frac{k_1[\text{Ox}_1]}{k_{-1}} \quad (\text{S70}).$$

From equation (S40) we have in this limit:

$$[\text{NADH}_b] \approx [\text{NADH} \cdot \text{Ox}_1] \quad (\text{S71}).$$

Substituting the expressions for α_{MM} , $\beta_{\text{eq}}^{\text{MM}}$ and $[\text{NADH}_b]$ from equations (S69)-(S71) to the predicted ETC flux in equation (S41), we obtain

$$J_{\text{ox}} = \alpha_{\text{MM}}(\beta - \beta_{\text{eq}}^{\text{MM}})[\text{NADH}_f] = k_1[\text{Ox}_1][\text{NADH}_f] - k_{-1}[\text{NADH} \cdot \text{Ox}_1] \quad (\text{S72}),$$

Thus, we have shown that the flux of the generalized NADH redox model reduces to the flux of the reversible Michaelis-Menten model in the limit where the unbinding rate of NADH from the reductase is much faster than any other rates in the model.

1741 We note that the predicted flux-concentration relation for the reversible Michaelis-Menten model
 1742 (equation (S72)) remains exactly the same as the generalized model (equation (S41)), but with
 1743 different expressions for α and β_{eq} as expressed in equations (S69)-(S70).

1744
 1745 Next, we generalize the results in equation (S72) to a detailed model with N oxidase and M
 1746 reductase, each of which is described by the reversible Michaelis-Menten kinetics. Unpacking
 1747 the coarse-grained binding and unbinding rates from equations (S24)-(S25), we obtain
 1748

$$\alpha_{\text{MM}} = - \sum_{i=1}^N k_{-1,i} \frac{[\text{NADH} \cdot \text{Ox}_i]}{[\text{NADH} \cdot \text{Ox}]} \quad (\text{S73}),$$

$$\beta_{\text{eq}}^{\text{MM}} = \frac{\sum_{i=1}^N k_{1,i} [\text{Ox}_i]}{\sum_{i=1}^N k_{-1,i} \frac{[\text{NADH} \cdot \text{Ox}_i]}{[\text{NADH} \cdot \text{Ox}]}} \quad (\text{S74}),$$

1749 where $k_{1,i}$ and $k_{-1,i}$ denote the binding and unbinding rates of NADH to the i th oxidase.

1751 **Connecting the NADH redox model to detailed biophysical models of mitochondrial** 1752 **metabolism**

1753
 1754 In this section, we show that the coarse-grained NADH redox model described above, and in
 1755 Figure 4b of the main text, can be directly related to detailed biophysical models of
 1756 mitochondrial metabolism, including previously published models (Beard, 2005; Korzeniewski
 1757 and Zoladz, 2001; Hill, 1977; Jin and Bethke 2002; Chang et al., 2011).

1758
 1759 In mitochondria, NADH oxidation is catalyzed by complex I of the electron transport chain,
 1760 which has the overall reaction:



1762 where two electrons are transferred from NADH to ubiquinone Q, and 4 protons are pumped out
 1763 of the mitochondrial matrix. To connect our model with detailed model of complex I, we rewrite
 1764 the flux through the ETC:

$$J_{\text{ox}} = r_{\text{ox}}^+ [\text{NADH} \cdot \text{Ox}] - r_{\text{ox}}^- [\text{NAD}^+ \cdot \text{Ox}] \quad (\text{S76}),$$

1766
 1767
 1768
 1769 Using

$$[\text{NADH} \cdot \text{Ox}] = \alpha \left(\frac{\beta_{\text{eq}}^{\text{re}}}{k_{\text{ox}}^{\text{u}}} + \frac{\beta_{\text{eq}}^{\text{ox}}}{k_{\text{re}}^{\text{u}}} - \frac{\beta}{k_{\text{ox}}^{\text{u}}} \right) [\text{NADH}_f] \quad (\text{S77}),$$

$$[\text{NAD}^+ \cdot \text{Ox}] = \alpha' \left(\frac{\beta_{\text{eq}}^{\text{re}}}{k_{\text{ox}}^{\text{u}}} + \frac{\beta_{\text{eq}}^{\text{ox}}}{k_{\text{re}}^{\text{u}}} - \frac{\beta'}{k_{\text{ox}}^{\text{u}}} \right) [\text{NAD}_f^+] \quad (\text{S78}),$$

1771
 1772 where

1773
$$\alpha = \frac{k_{\text{ox}}^{\text{u}} k_{\text{re}}^{\text{u}}}{k_{\text{ox}}^{\text{u}} - k_{\text{re}}^{\text{u}}}, \beta = \frac{[\text{NADH}_b]}{[\text{NADH}_f]}, \beta_{\text{eq}}^{\text{ox}} + \beta_{\text{eq}}^{\text{re}} = \beta_{\text{eq}}, \beta_{\text{eq}}^{\text{ox}} = \frac{k_{\text{ox}}^{\text{b}}}{k_{\text{ox}}^{\text{u}}}, \beta_{\text{eq}}^{\text{re}} = \frac{k_{\text{re}}^{\text{b}}}{k_{\text{re}}^{\text{u}}} \quad (\text{S79})$$

1774

1775
$$\alpha' = \frac{k_{\text{ox}}^{\text{u}} k_{\text{re}}^{\text{u}}}{k_{\text{ox}}^{\text{u}} - k_{\text{re}}^{\text{u}}}, \beta' = \frac{[\text{NAD}_f^+]}{[\text{NAD}_f^+]}, \beta_{\text{eq}}^{\text{ox}} + \beta_{\text{eq}}^{\text{re}} = \beta_{\text{eq}}, \beta_{\text{eq}}^{\text{ox}} = \frac{k_{\text{ox}}^{\text{b}}}{k_{\text{ox}}^{\text{u}}}, \beta_{\text{eq}}^{\text{re}} = \frac{k_{\text{re}}^{\text{b}}}{k_{\text{re}}^{\text{u}}} \quad (\text{S80})$$

1776 as

1777
$$J_{\text{ox}} = \tilde{r}_{\text{ox}}^+ [\text{NADH}_f] - \tilde{r}_{\text{ox}}^- [\text{NAD}_f^+] = \tilde{r}_{\text{ox}} [\text{NADH}_f] \quad (\text{S81}),$$

1778

1779 where

1780

1781
$$\tilde{r}_{\text{ox}}^+ = \alpha \left(\frac{\beta_{\text{eq}}^{\text{re}}}{k_{\text{ox}}^{\text{u}}} + \frac{\beta_{\text{eq}}^{\text{ox}}}{k_{\text{re}}^{\text{u}}} - \frac{\beta}{k_{\text{ox}}^{\text{u}}} \right) r_{\text{ox}}^+ \quad (\text{S82}),$$

1782
$$\tilde{r}_{\text{ox}}^- = \alpha' \left(\frac{\beta_{\text{eq}}^{\text{re}}}{k_{\text{ox}}^{\text{u}}} + \frac{\beta_{\text{eq}}^{\text{ox}}}{k_{\text{re}}^{\text{u}}} - \frac{\beta'}{k_{\text{ox}}^{\text{u}}} \right) r_{\text{ox}}^- \quad (\text{S83}),$$

$$\tilde{r}_{\text{ox}} = \alpha(\beta - \beta_{\text{eq}}) = \left(\tilde{r}_{\text{ox}}^+ + \tilde{r}_{\text{ox}}^- \frac{1 + \beta}{1 + \beta'} \right) - \frac{N}{[\text{NADH}_f]} \tilde{r}_{\text{ox}}^- \quad (\text{S84}).$$

1783

1784 The last equality in Equation (S84) is obtained by assuming that the total concentration of
1785 NADH plus NAD^+ is constant:

1786

$$N = [\text{NADH}_f] + [\text{NAD}_f^+] + [\text{NADH}_b] + [\text{NAD}_b^+] \quad (\text{S85}).$$

1787

1788 Equation (S81) allows us to connect our coarse-grained model to previously published detailed
1789 models of complex I. By equating the flux through complex I, J_{C1} , in previous models to the flux
1790 through the ETC in our NADH redox model, J_{ox} , we can determine \tilde{r}_{ox} (and \tilde{r}_{ox}^+ and \tilde{r}_{ox}^-) in
1791 terms of variables defined in those more detailed models. In Table 1, we summarize the
1792 relationship between the NADH redox model and several previously published models of
1793 complex I.

1794

Model	Flux	\tilde{r}_{ox}^+	\tilde{r}_{ox}^-	\tilde{r}_{ox}
Beard et al., 2019	$J_{\text{C1}} = \tilde{r}_{\text{ox}}^+ [\text{NADH}_f] - \tilde{r}_{\text{ox}}^- [\text{NAD}_f^+]$	$\tilde{r}_{\text{ox}}^+ = X_{\text{C1}} e^{\frac{\Delta G_{\text{Cl}}}{RT}}$	$\tilde{r}_{\text{ox}}^- = X_{\text{C1}}$	$\tilde{r}_{\text{ox}} = \left(\tilde{r}_{\text{ox}}^+ + \tilde{r}_{\text{ox}}^- \frac{1 + \beta}{1 + \beta'} \right) - \frac{N}{[\text{NADH}_f]} \tilde{r}_{\text{ox}}^-$
Chang et al., 2011 Jin et al., 2002	$J_{\text{C1}} = \tilde{r}_{\text{ox}} [\text{NADH}_f]$	N/A	N/A	$\tilde{r}_{\text{ox}} = V_{\text{max}} \left(\frac{[\text{N}_T]}{[\text{N}_T] + K_{\text{S,D}}} \right) \left(\frac{[\text{Q}_T]}{[\text{Q}_T] + K_{\text{S,A}}} \right) \times$ $\left(\frac{[\text{Q}]}{[\text{Q}] + [\text{QH}_2] K_{\text{R,A}}} \right) \left(\frac{1}{[\text{NADH}_f] + [\text{NAD}_f^+] K_{\text{R,D}}} \right) \times$ $(1 - e^{-\frac{\Delta G_{\text{Cl}}}{RT}})$
Hill, 1977	$J_{\text{C1}} = J_{\text{max}} (1 - e^{-\frac{\Delta G_{\text{Cl}}}{RT}})$	N/A	N/A	$\tilde{r}_{\text{ox}} = J_{\text{max}} (1 - e^{-\frac{\Delta G_{\text{Cl}}}{RT}}) / [\text{NADH}_f]$
Korzeniewski and Zoladz, 2001	$J_{\text{C1}} = k_{\text{Cl}} \Delta G_{\text{Cl}}$	N/A	N/A	$\tilde{r}_{\text{ox}} = k_{\text{Cl}} \Delta G_{\text{Cl}} / [\text{NADH}_f]$
$\Delta G_{\text{Cl}} = -[\Delta G_{0,\text{Cl}} + 4\Delta G_{\text{H}} - RT \ln \left(\frac{[\text{H}^+]}{10^{-7}} \right) - RT \ln \left(\frac{[\text{Q}]}{[\text{QH}_2]} \right) - RT \ln \left(\frac{[\text{NADH}_f]}{[\text{NAD}_f^+]} \right)]; \Delta \tilde{G}_{\text{Cl}} = \Delta G_{\text{Cl}} - RT \ln \left(\frac{[\text{NADH}_f]}{[\text{NAD}_f^+]} \right); \Delta G_{0,\text{Cl}} = -69.37 \text{ kJ/mol}$ $[\text{N}_T] = [\text{NADH}_f] + [\text{NAD}_f^+], [\text{Q}_T] = [\text{Q}] + [\text{QH}_2]$				

1795

1796 **Table 1 | Connection of the NADH redox model to detailed models of complex I.** ΔG_{H} is the proton motive force.
1797 ΔG_{Cl} is the free energy difference of the reaction at complex I. $\Delta G_{0,\text{Cl}}$ is the standard free energy difference of the
1798 reaction at complex I. $[\text{Q}]$, $[\text{QH}_2]$ and $[\text{Q}_T]$ are the concentrations of the oxidized, reduced and total ubiquinone
1799 concentrations.

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1802 **References**

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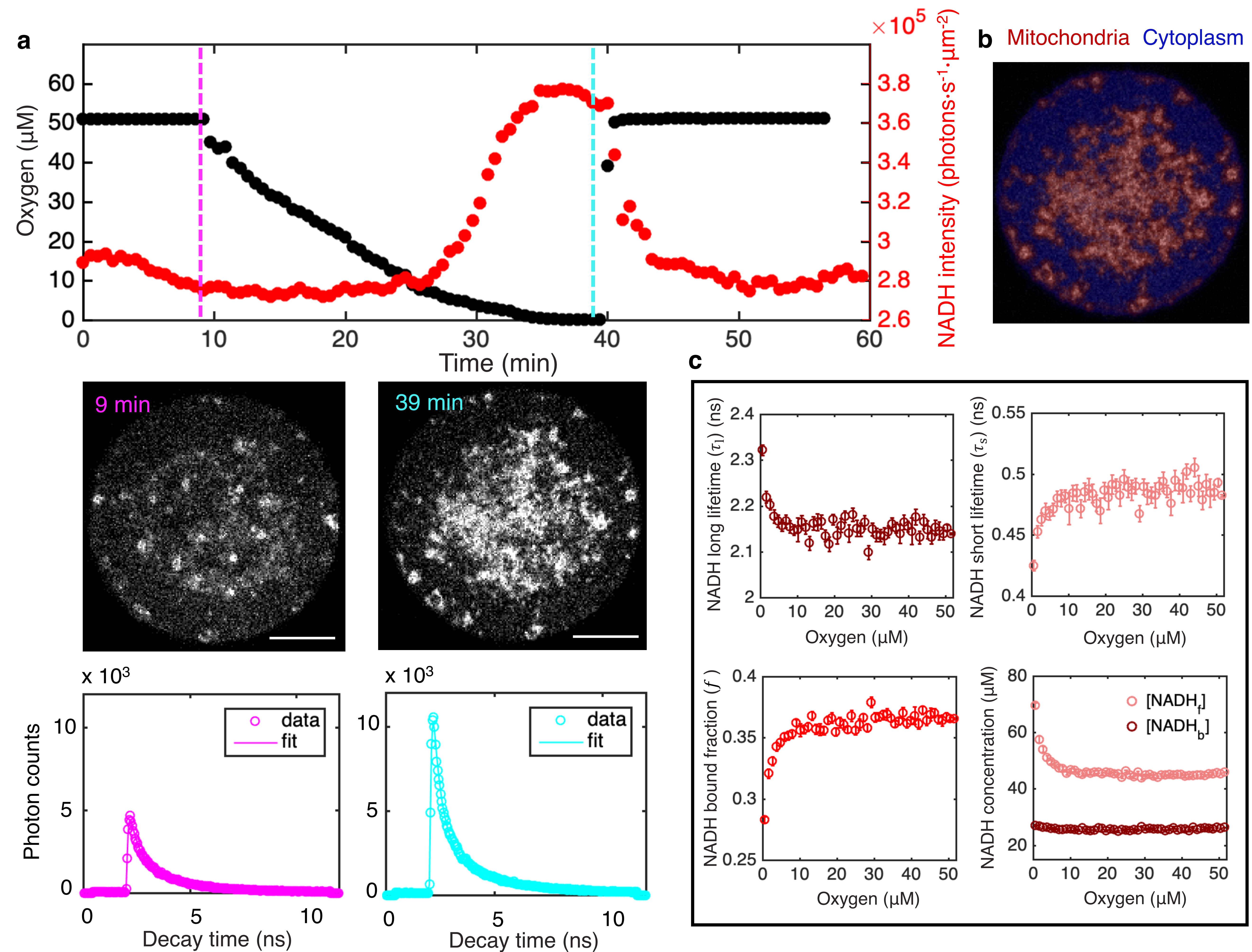
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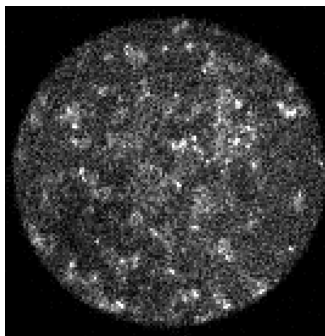
1981 **Acknowledgements**

1982

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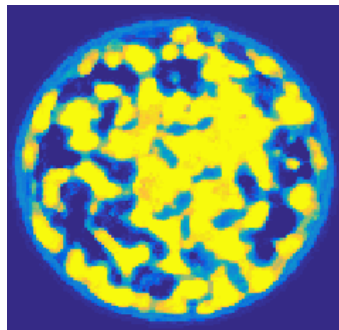
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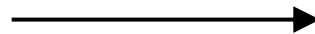
Pixel
classification



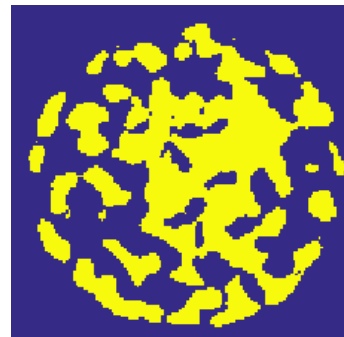
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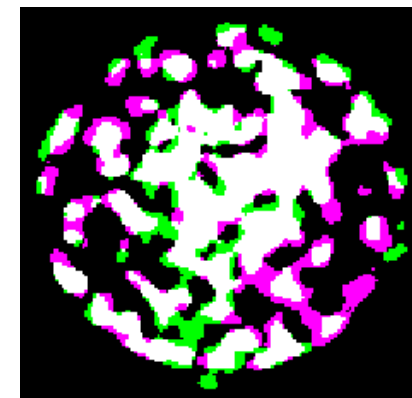
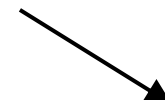
Thresholding
 $P > 0.7$



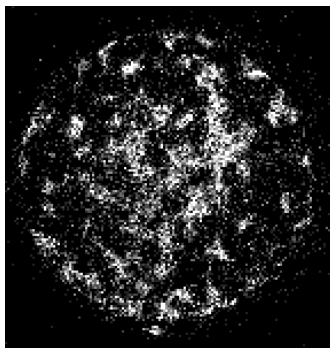
NADH-based segmentation



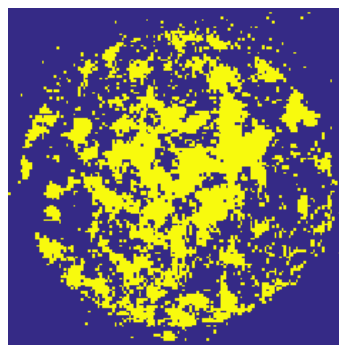
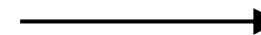
Overlay



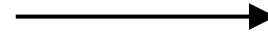
MitoTracker image



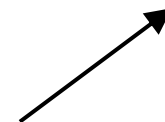
Thresholding
intensity above
60 percentile

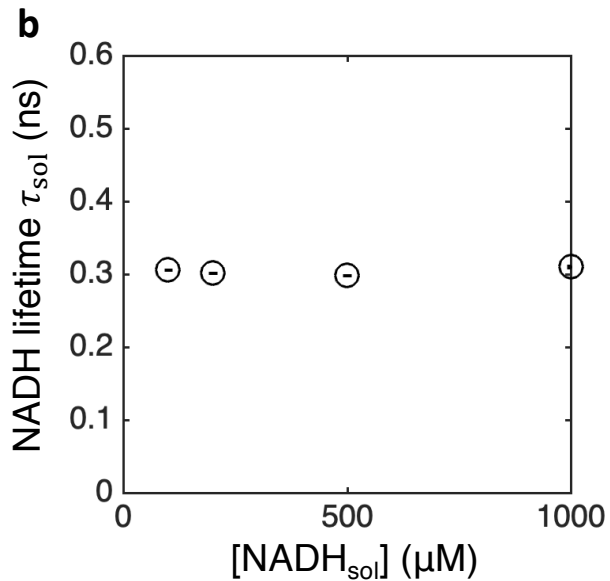
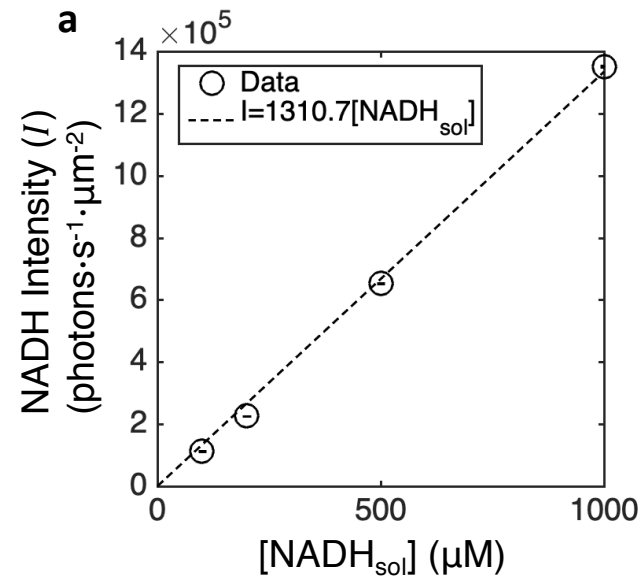


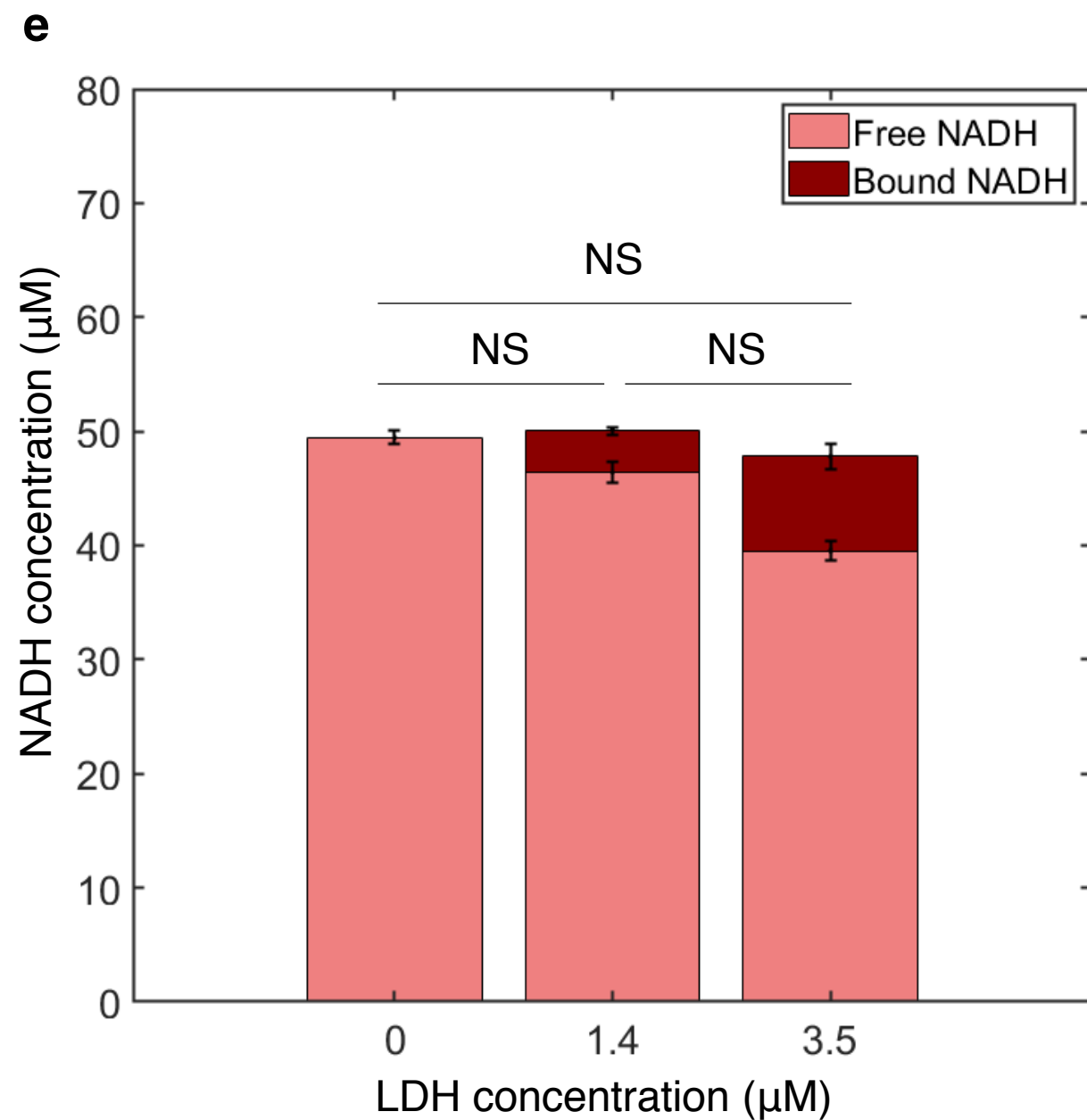
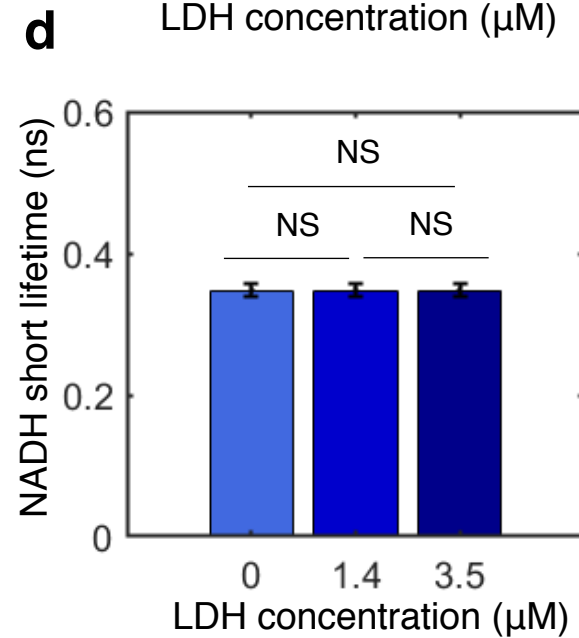
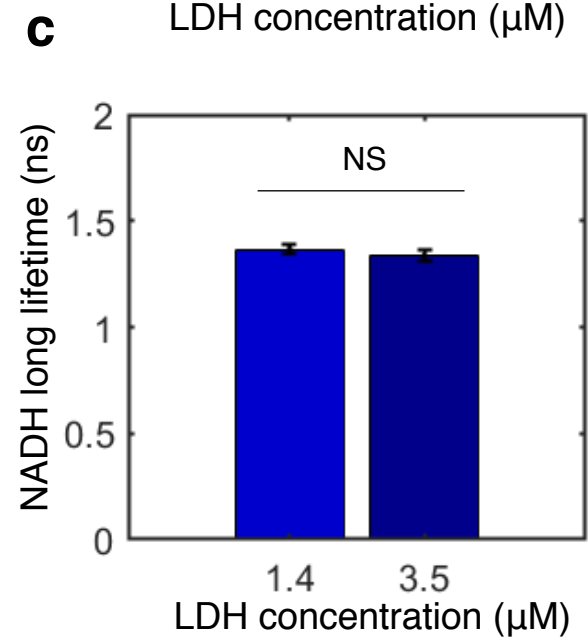
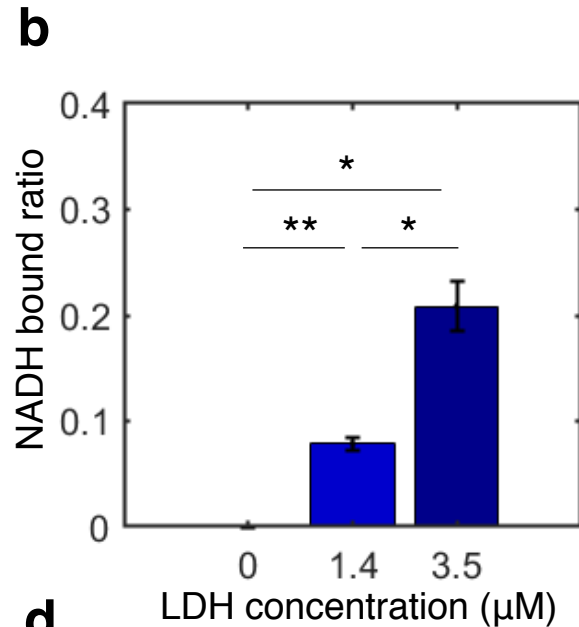
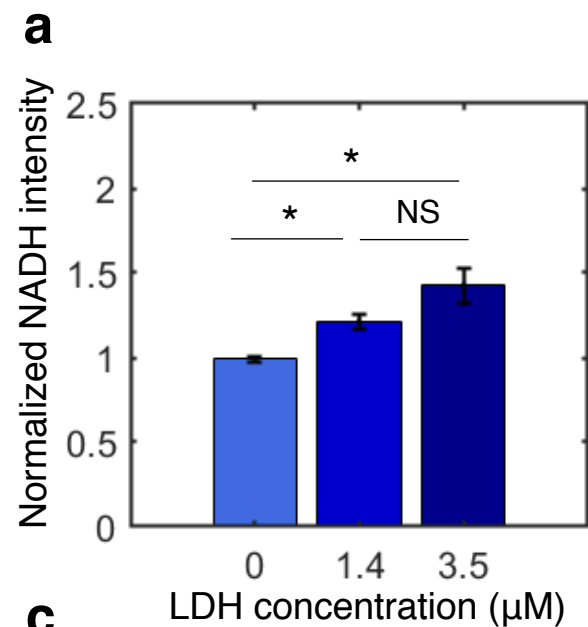
Gaussian blur

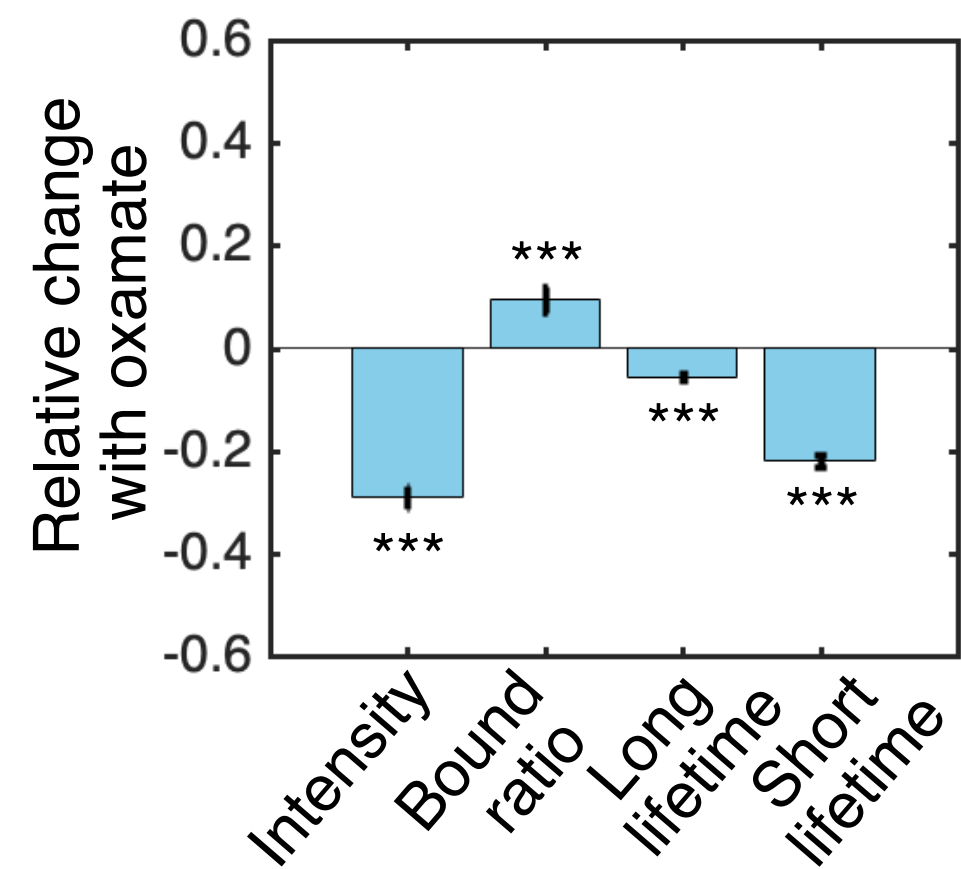
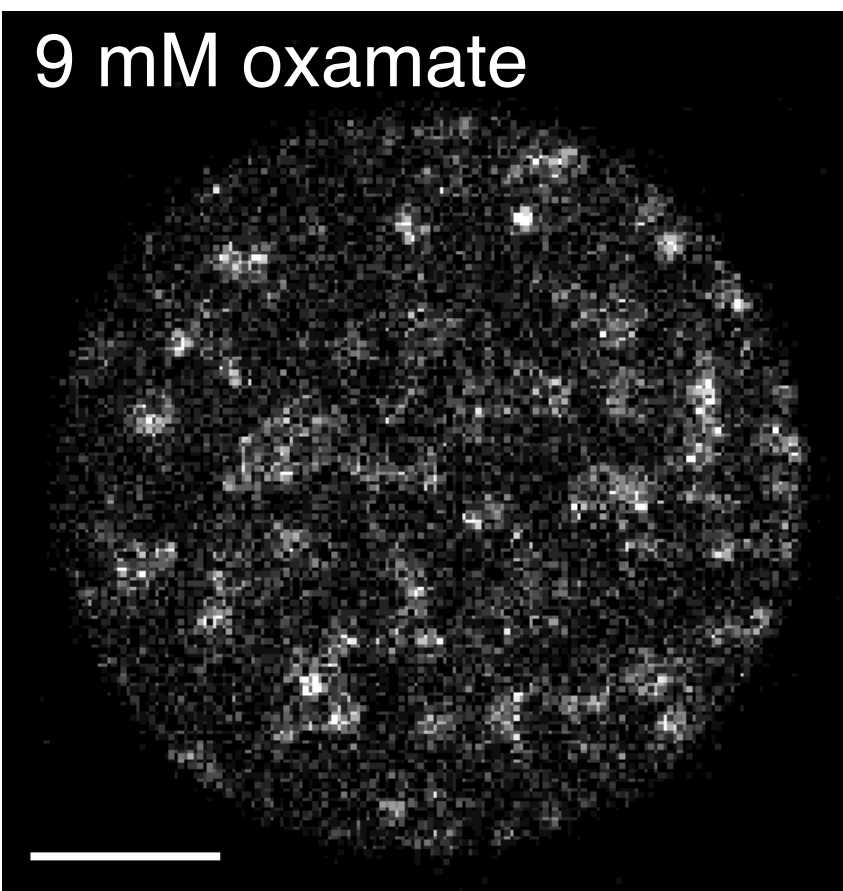
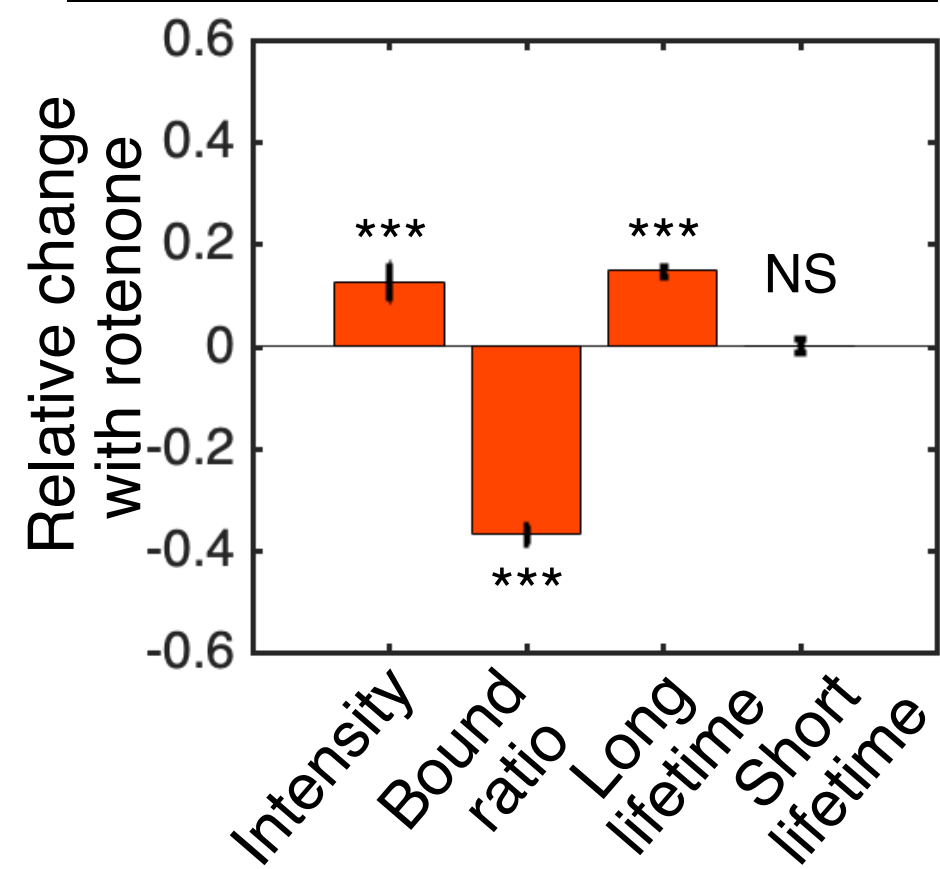
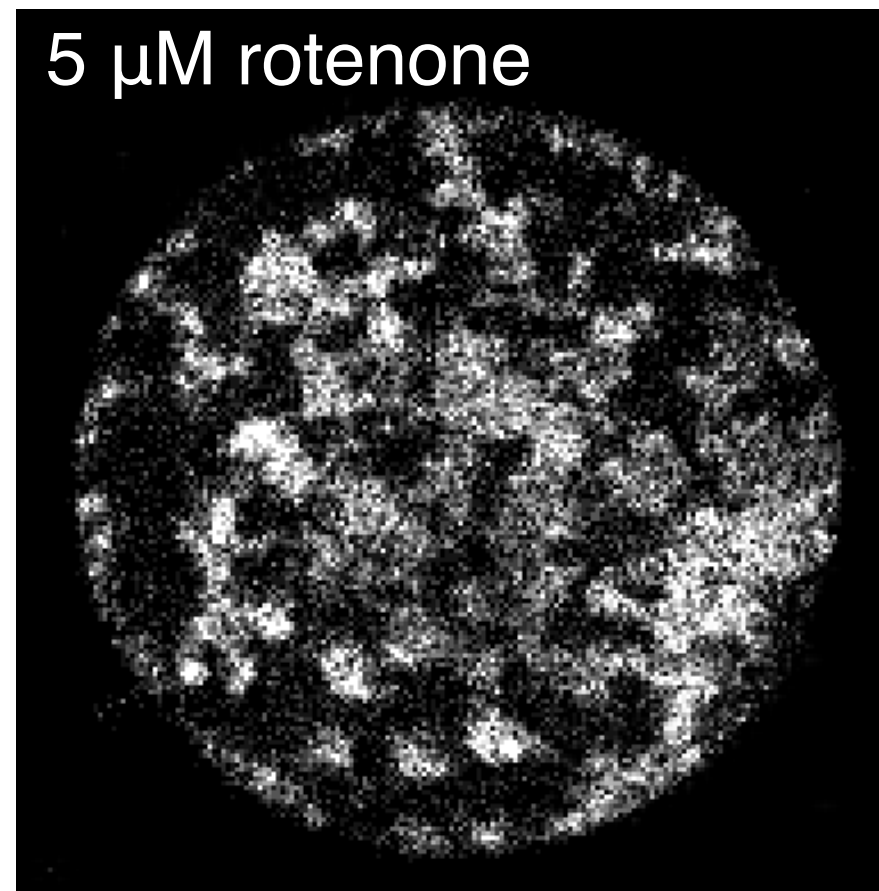
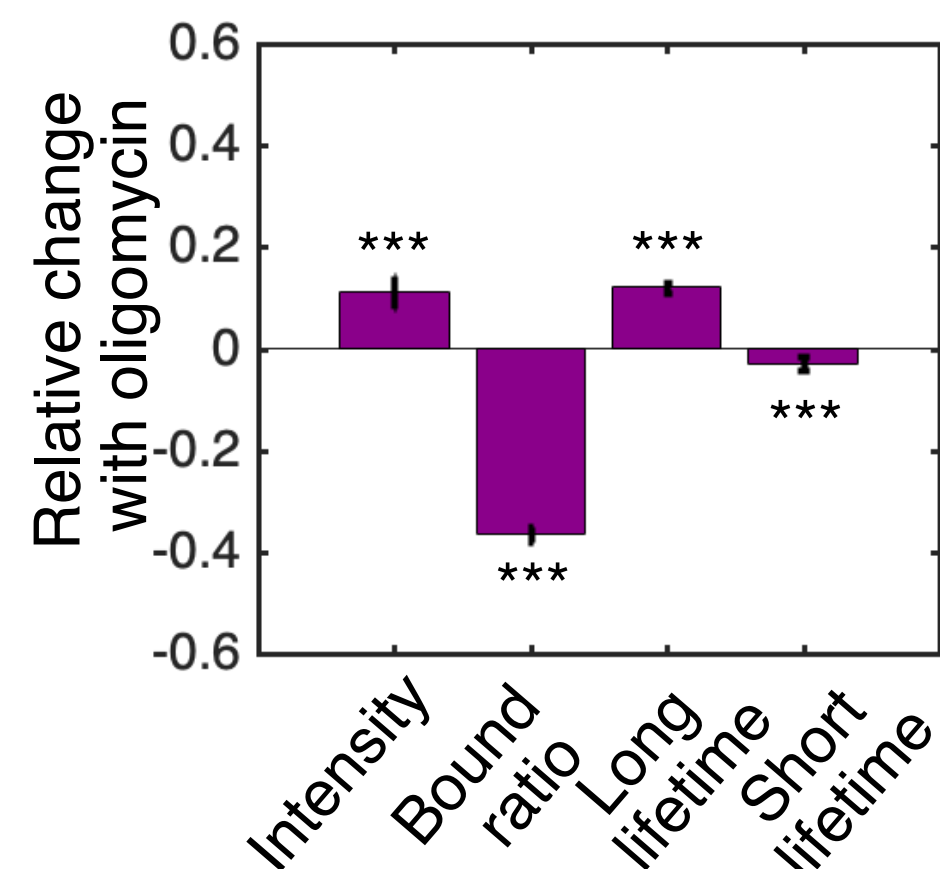
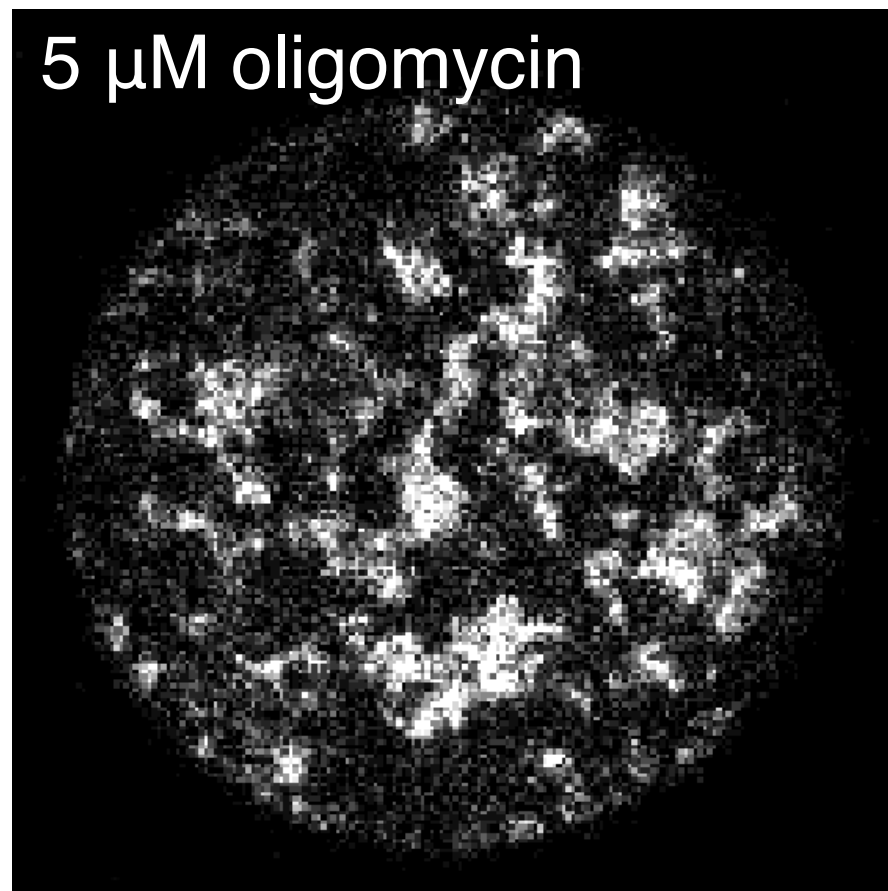
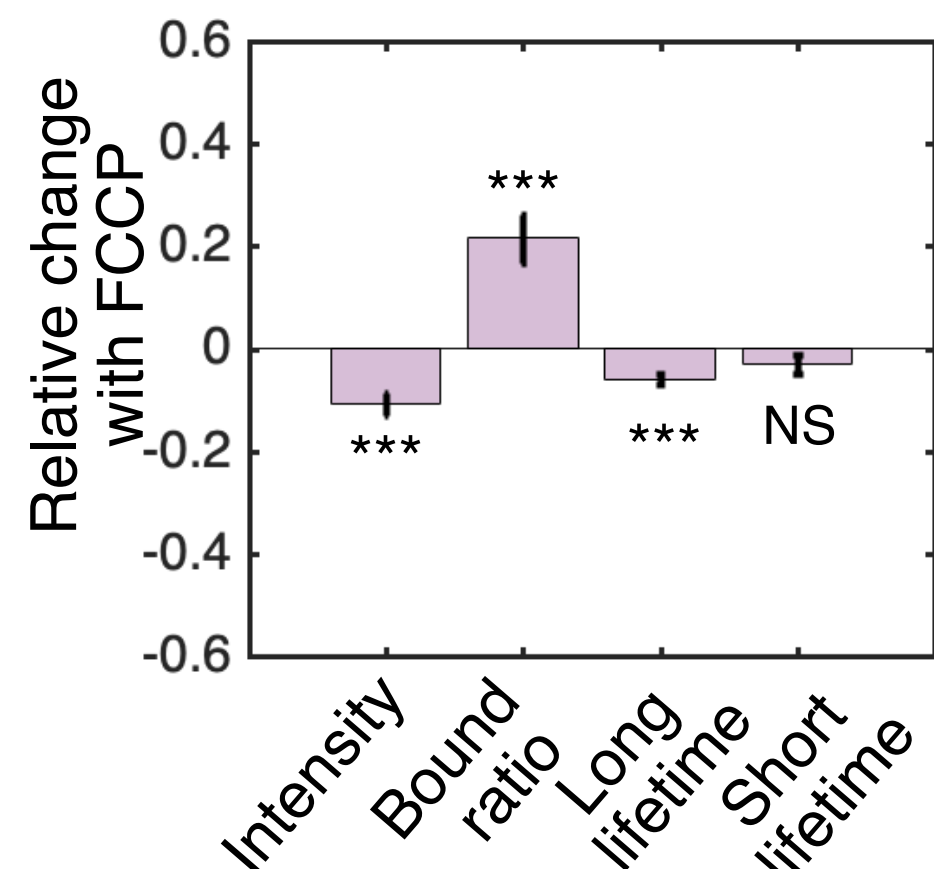
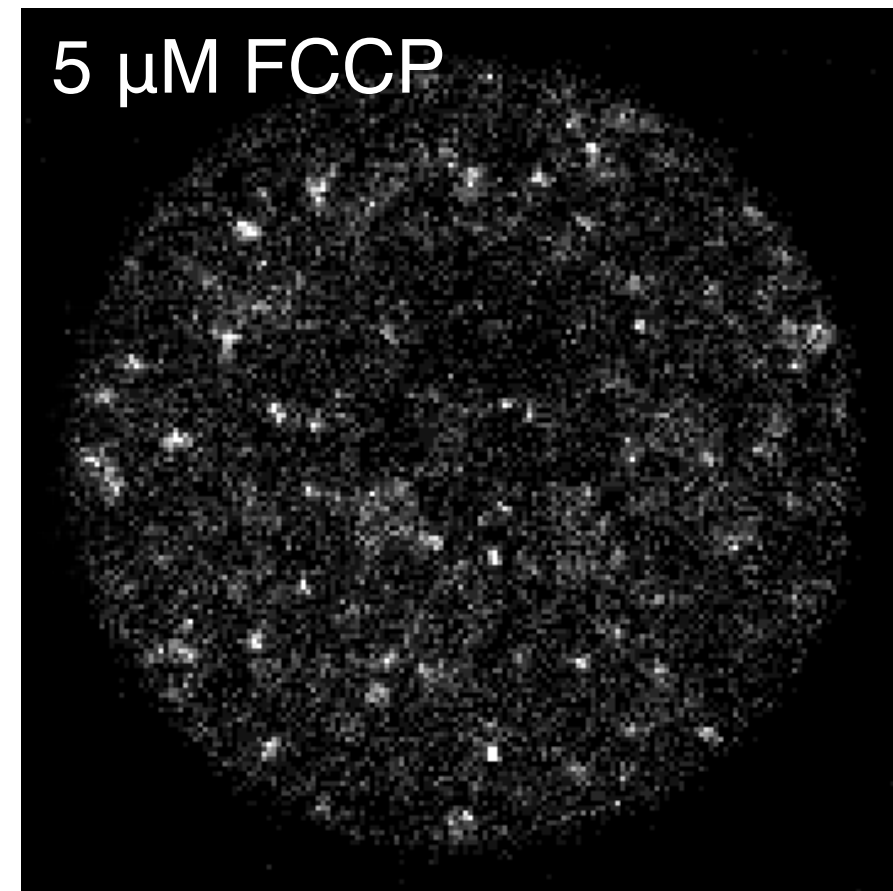
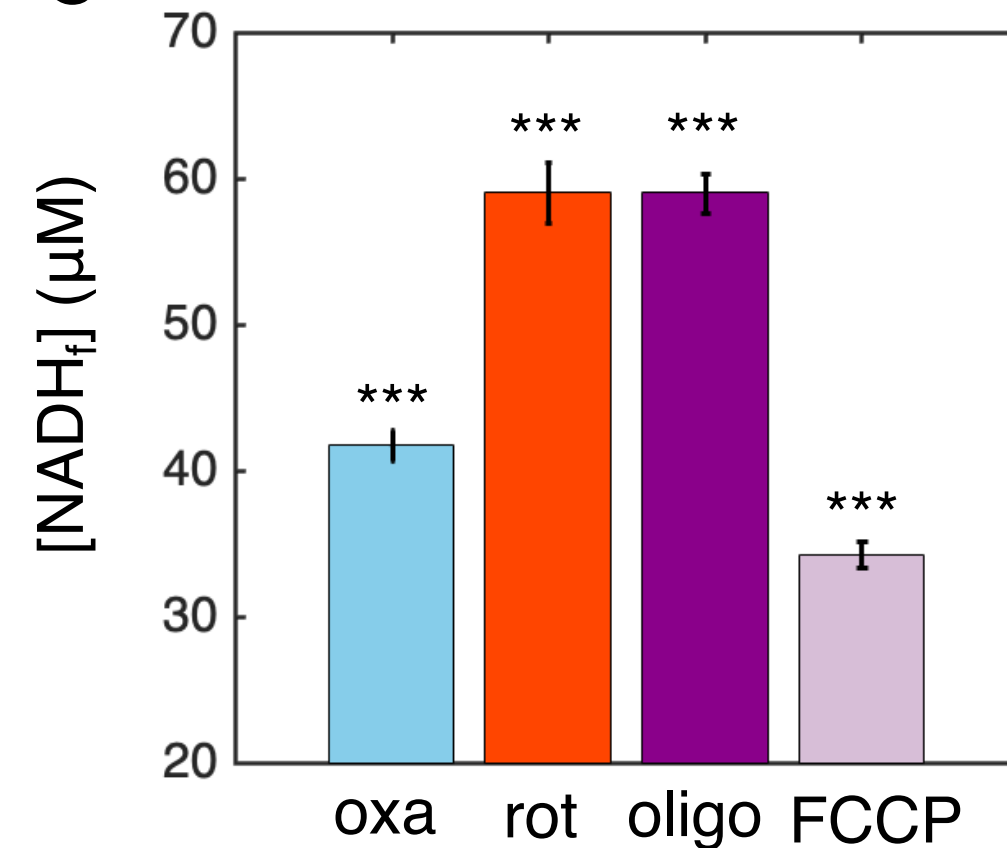
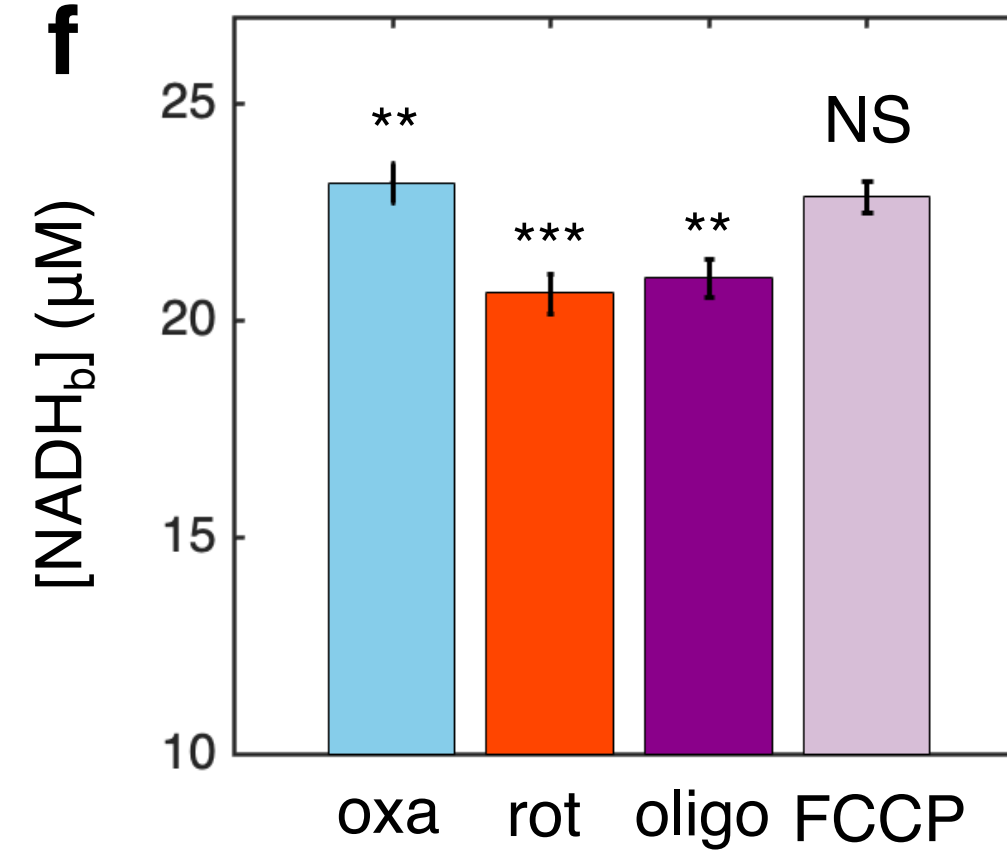


MitoTracker-based segmentation



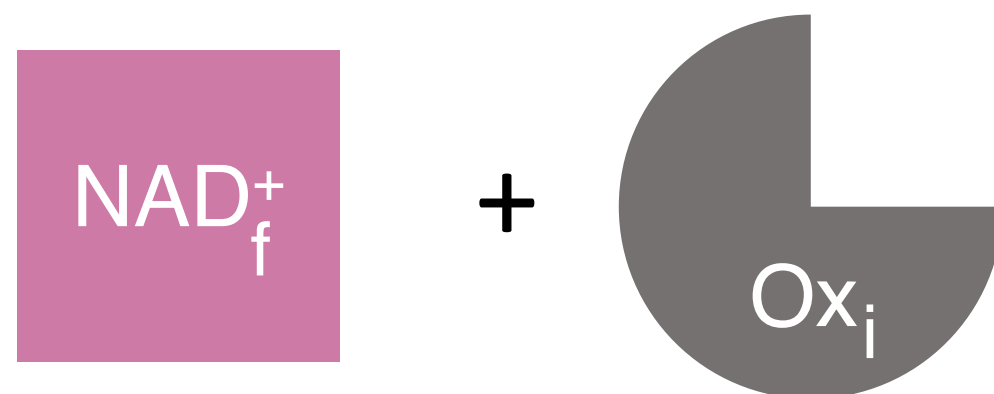
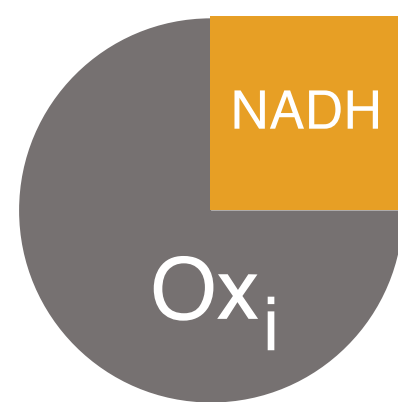




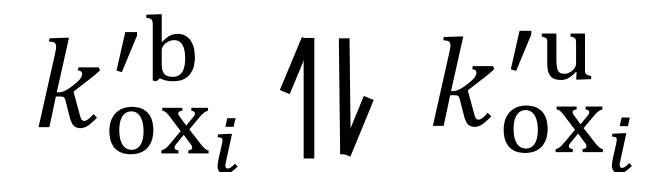
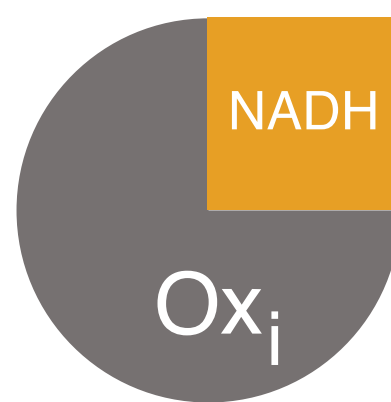
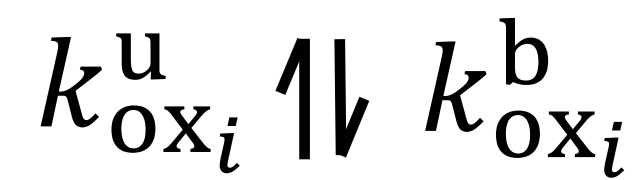
a**b****c****d****e****f**

a Reversible Michaelis-Menten kinetics

Full notation



Reduced notation



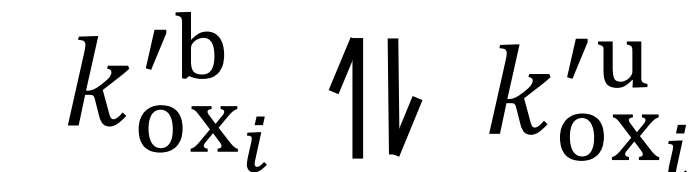
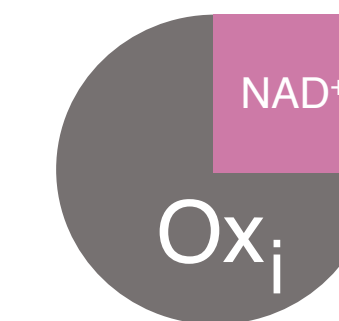
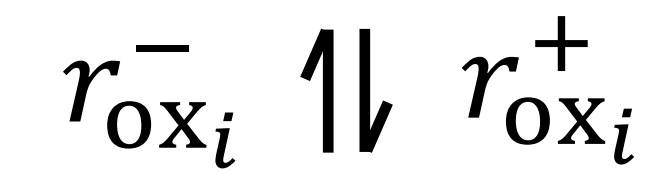
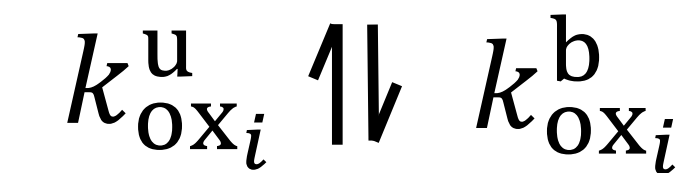
$$k_{\text{Ox}_i}^b = k_{\text{Ox}_i}^b([\text{Ox}_i]) = k_1[\text{Ox}_i]$$

$$k'_{\text{Ox}_i}{}^b = k'_{\text{Ox}_i}{}^b([\text{Ox}_i]) = k_{-2}[\text{Ox}_i]$$

$$k_{\text{Ox}_i}^u = k_{-1}, k'_{\text{Ox}_i}{}^u = k_2$$

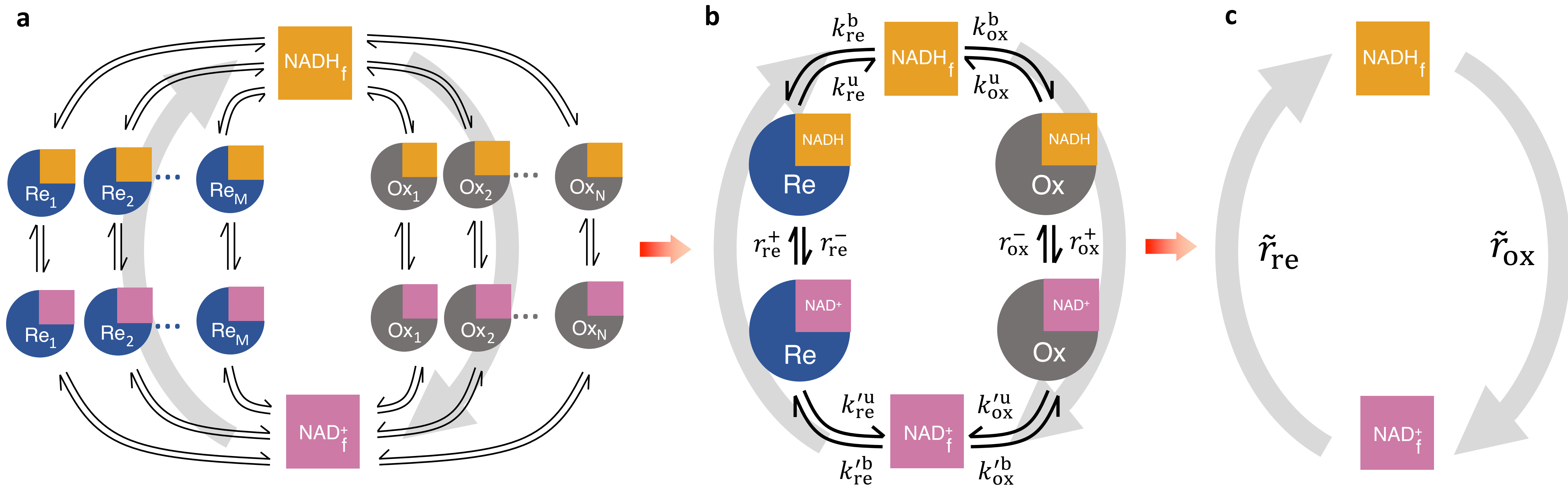
b Generalized enzyme kinetics

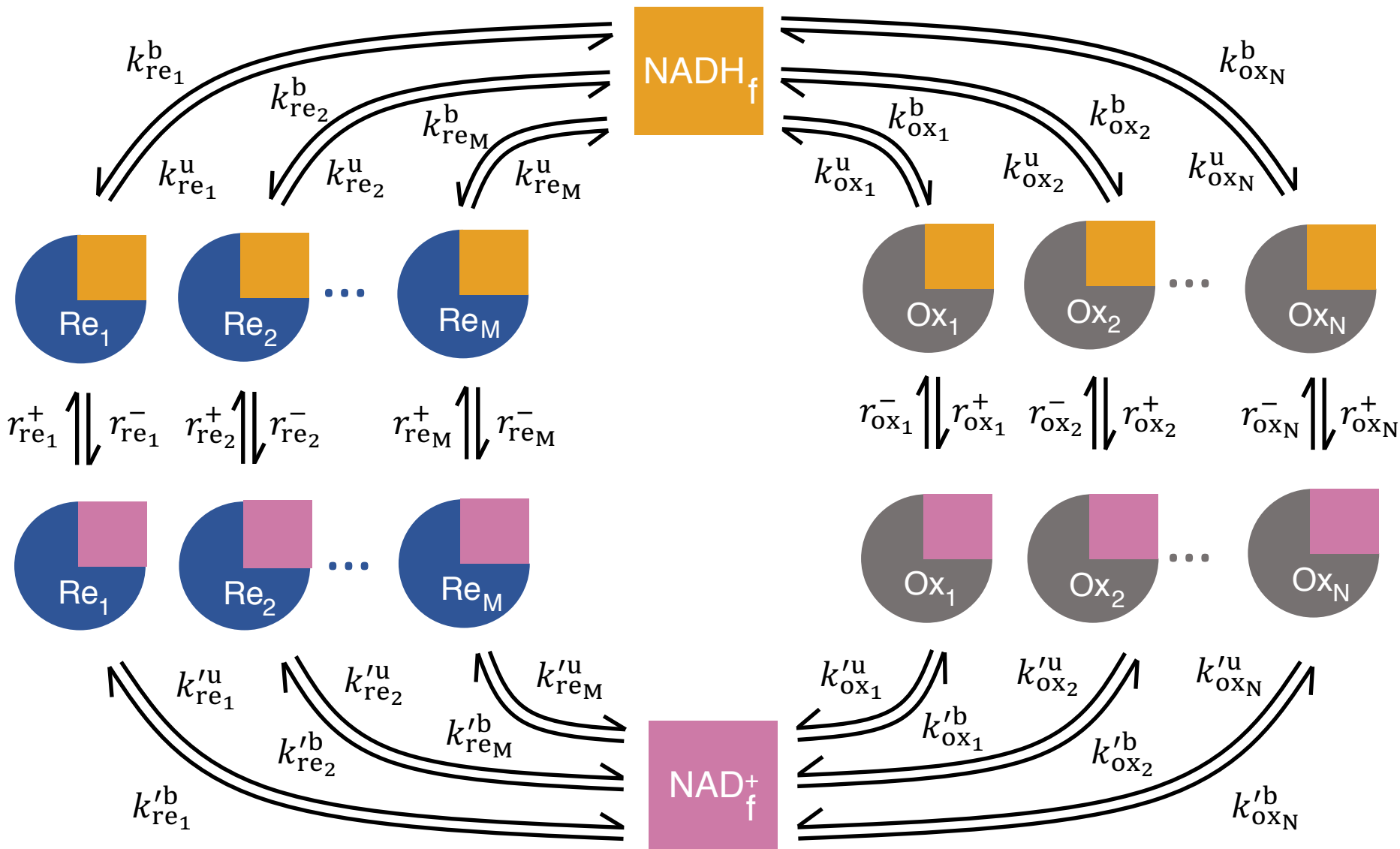
Reduced notation

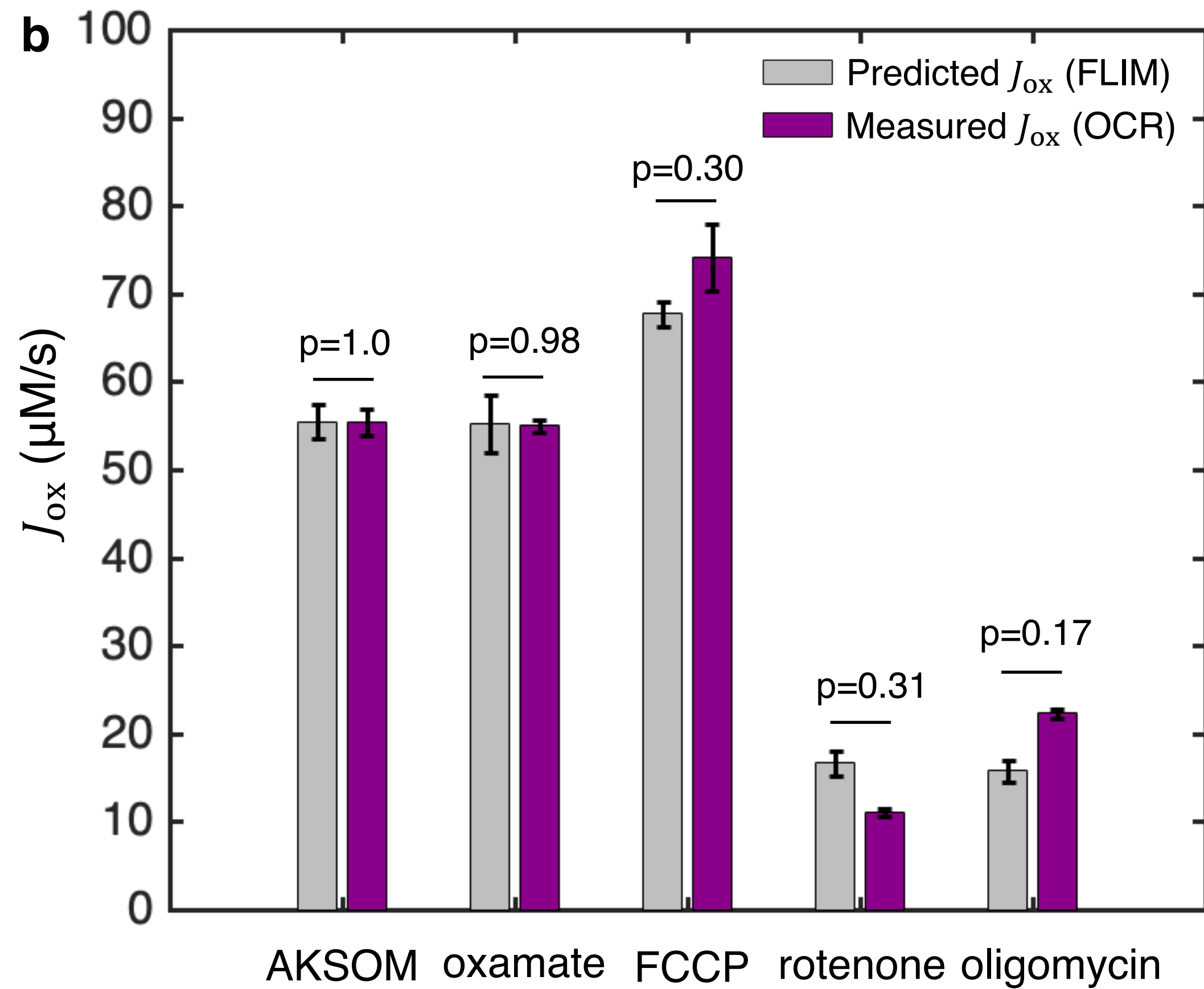
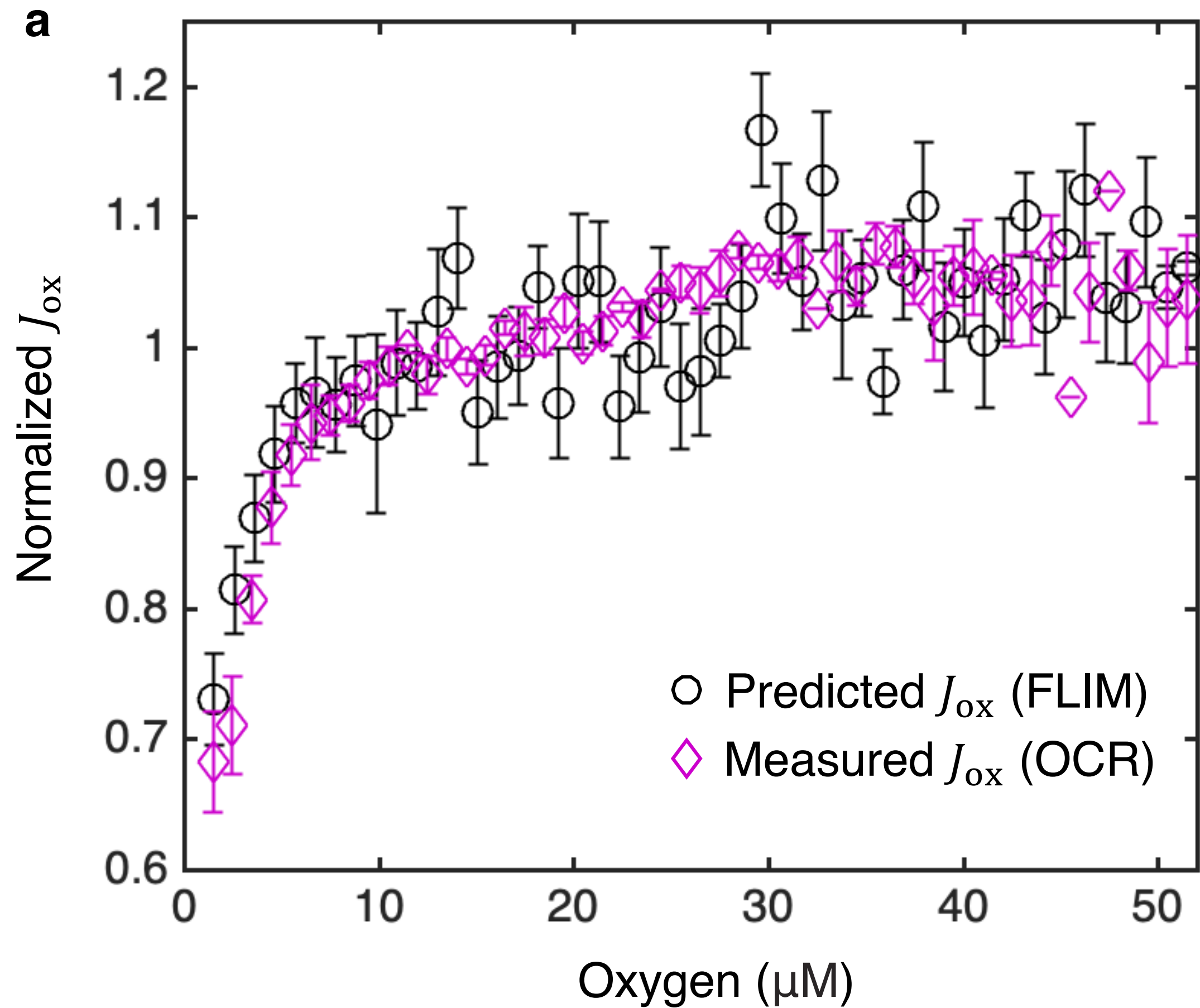


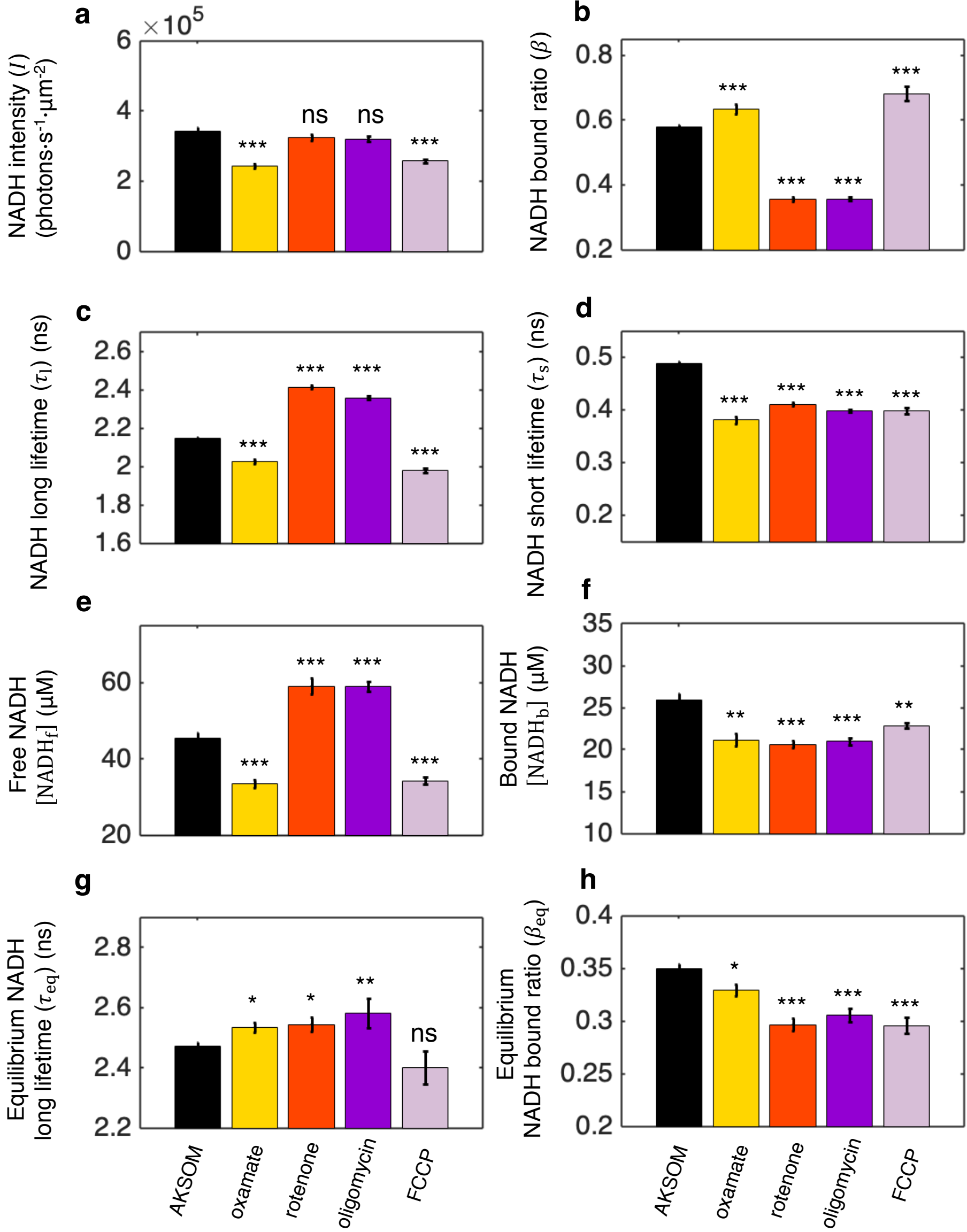
$$k = k([\text{Ox}_i], [\text{NADH}_f], [\text{Metabolites}], \text{pH}, \dots)$$

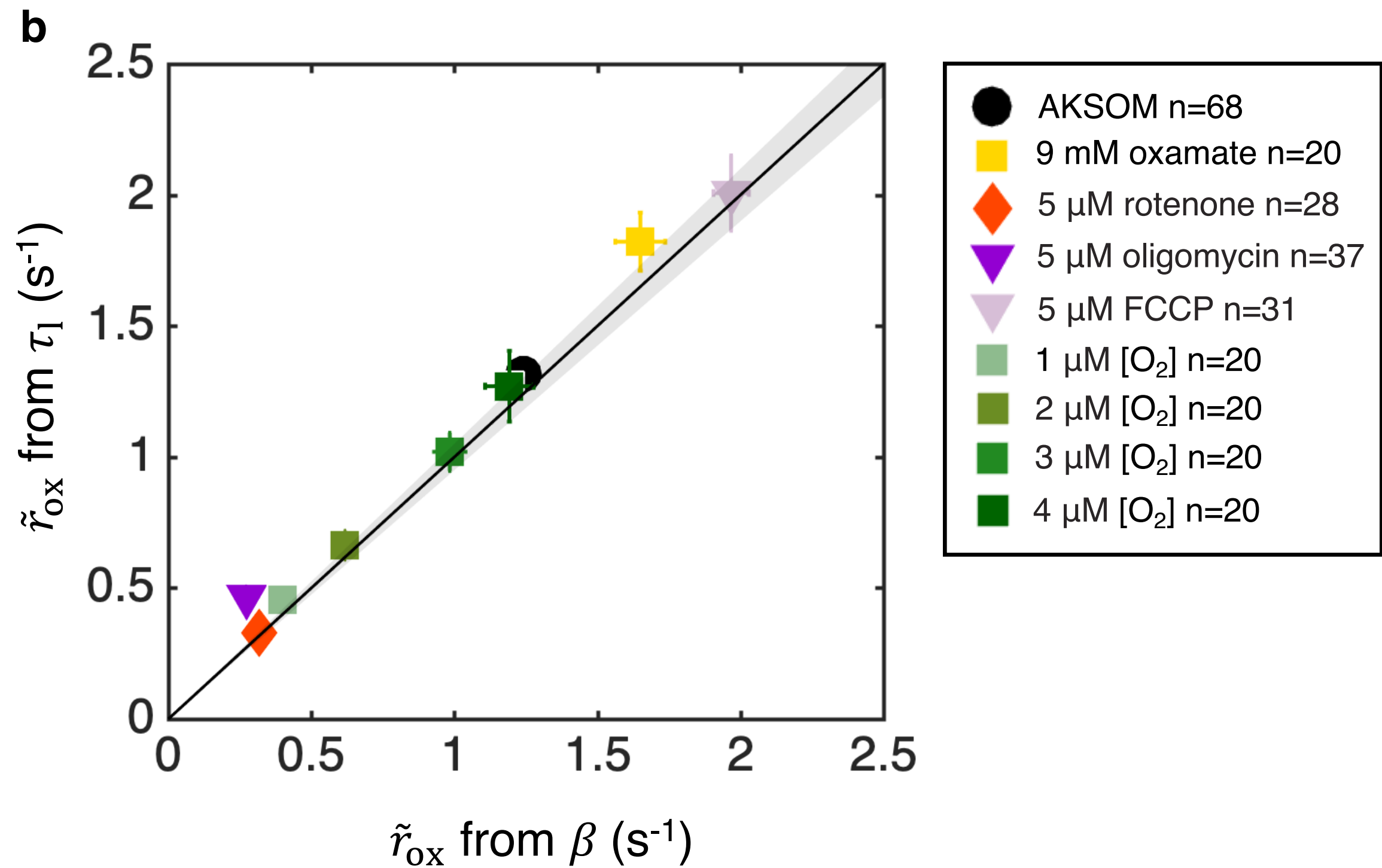
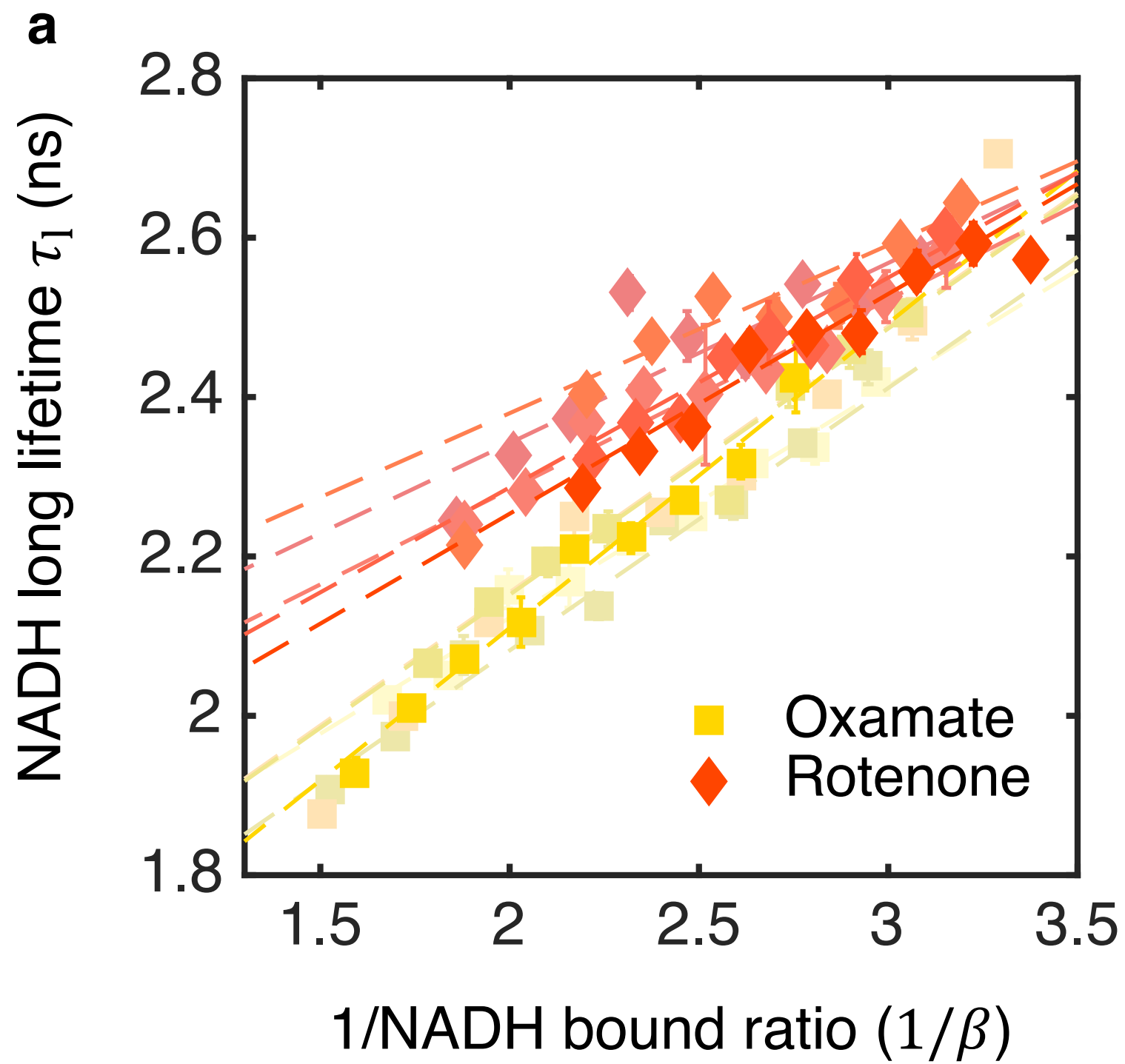
$$r = r([\text{Ox}_i], [\text{NADH}_f], [\text{Metabolites}], \text{pH}, \dots)$$

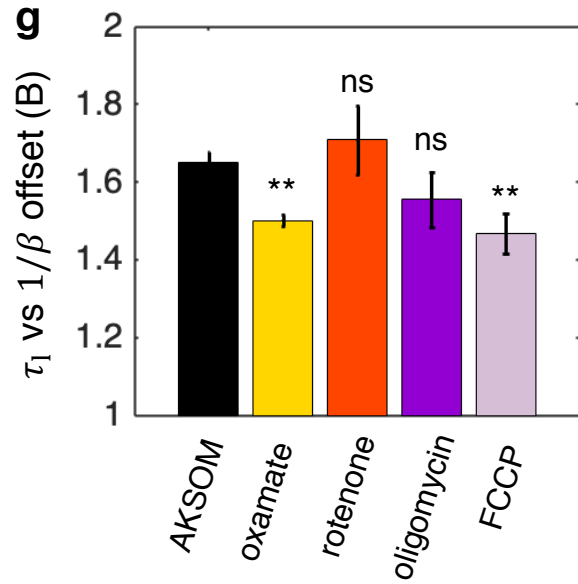
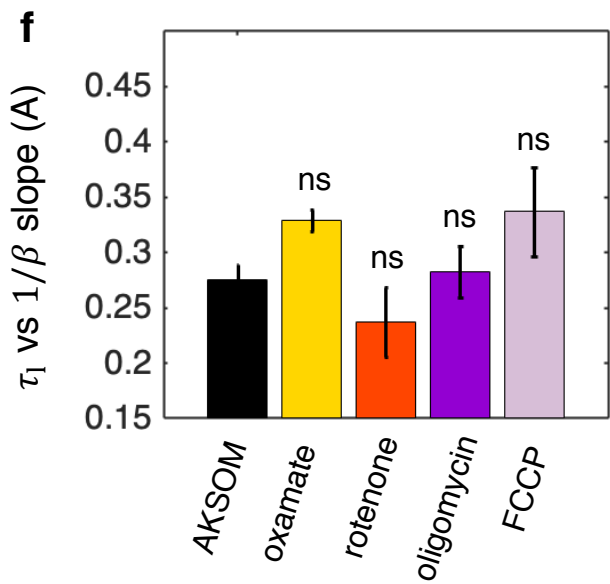
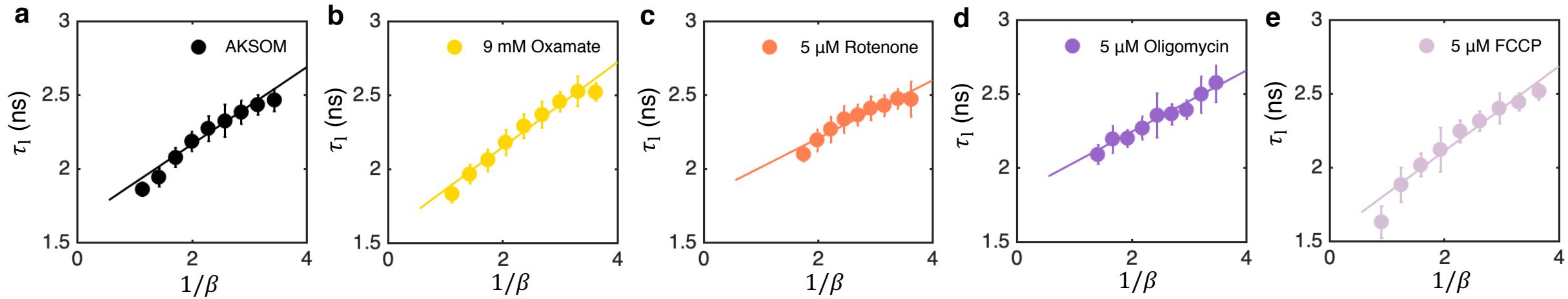


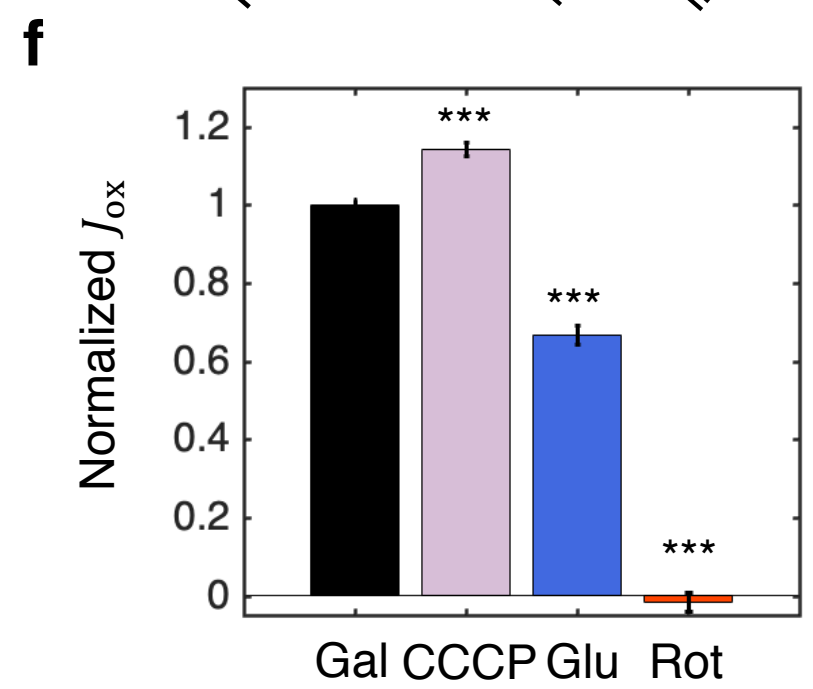
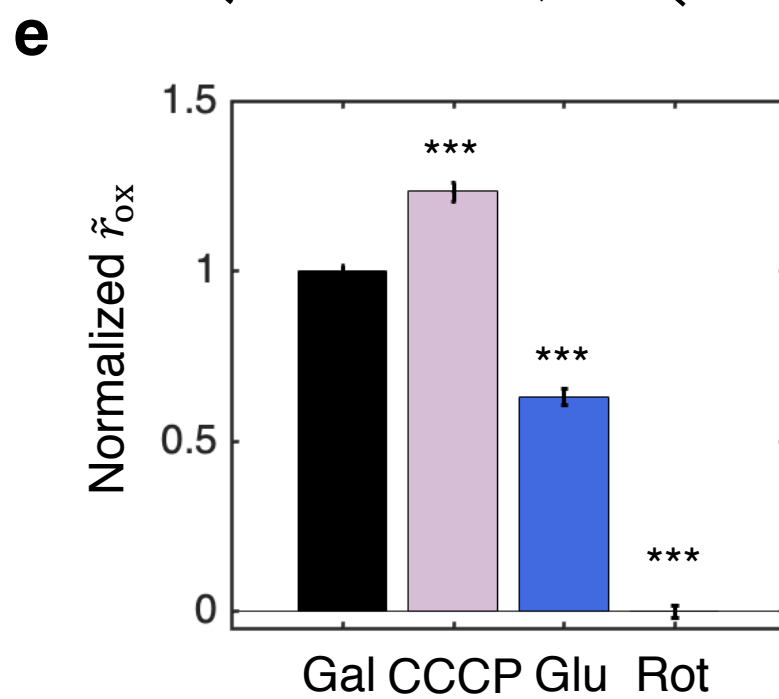
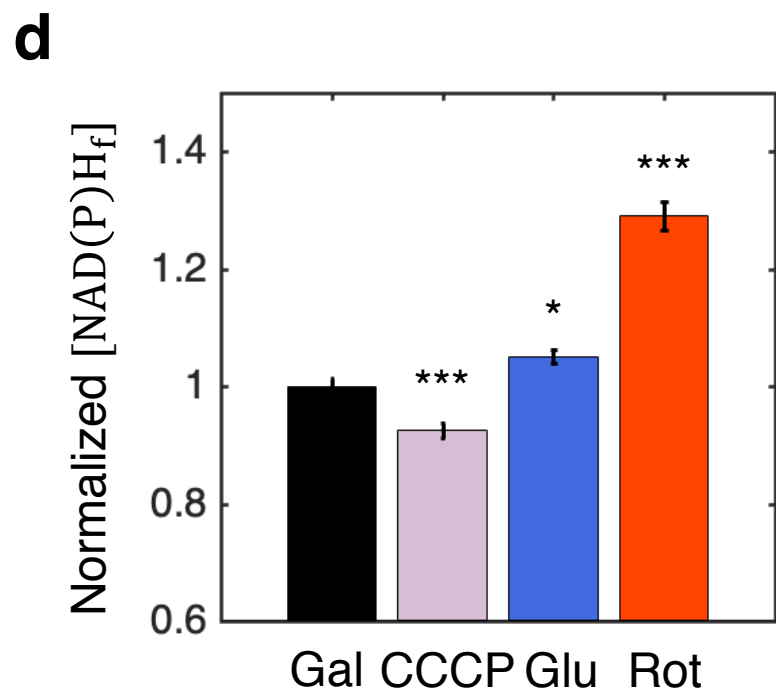
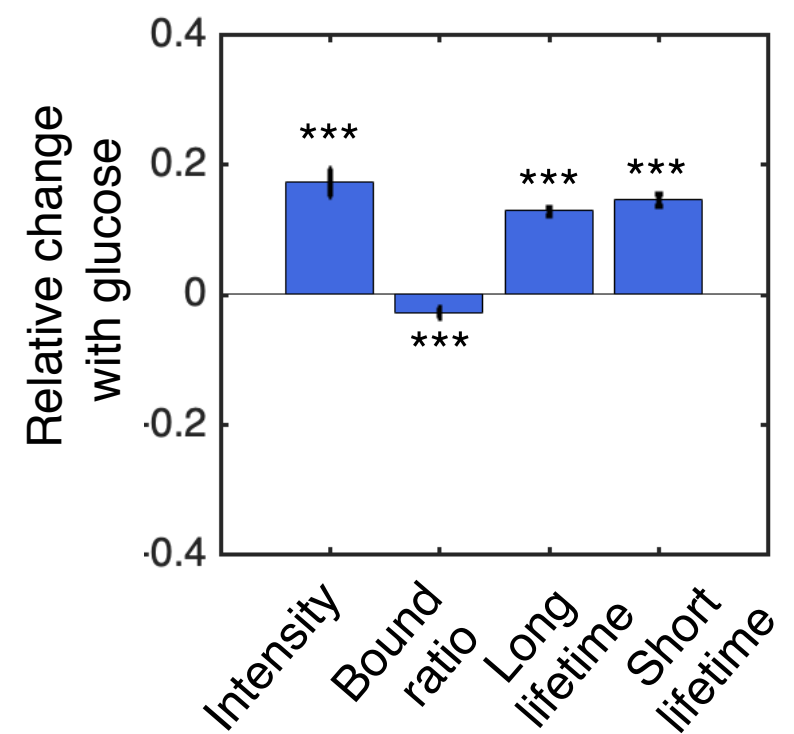
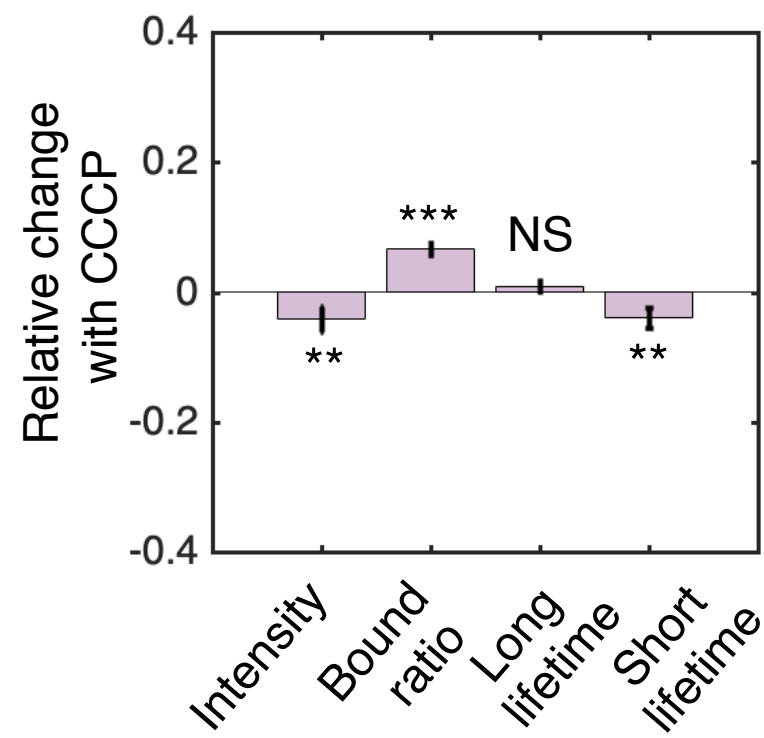
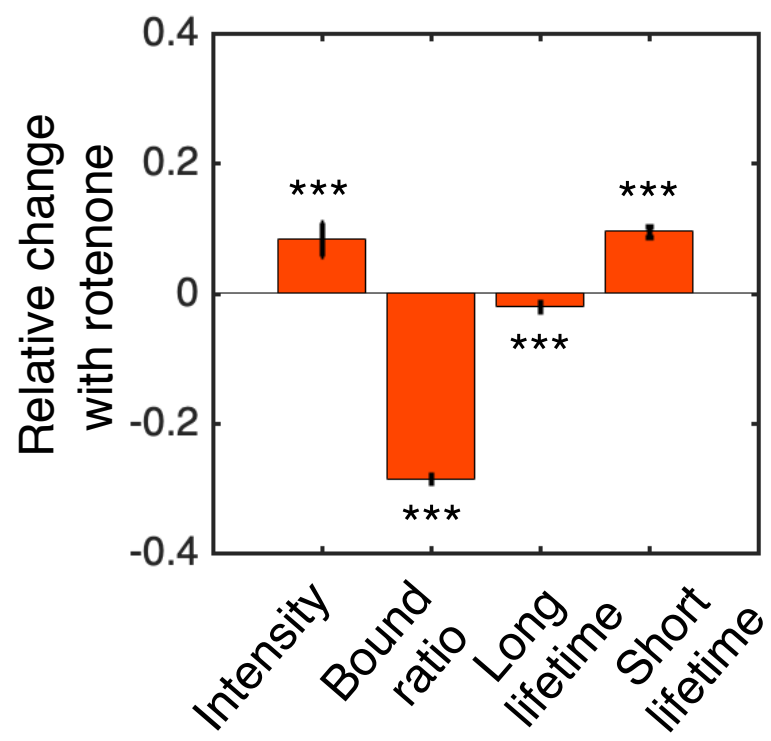
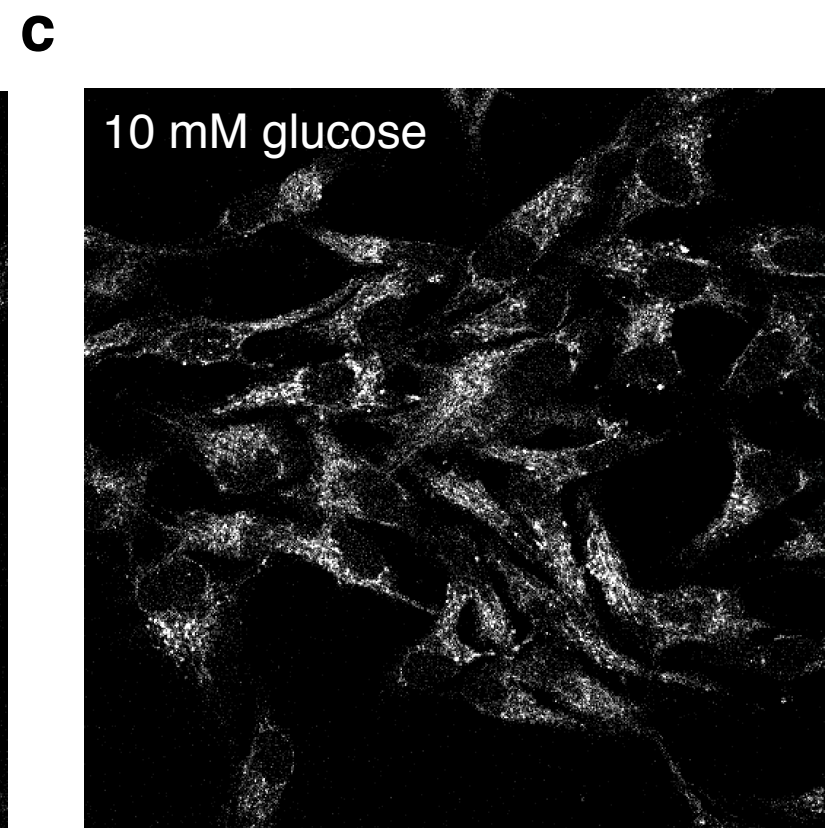
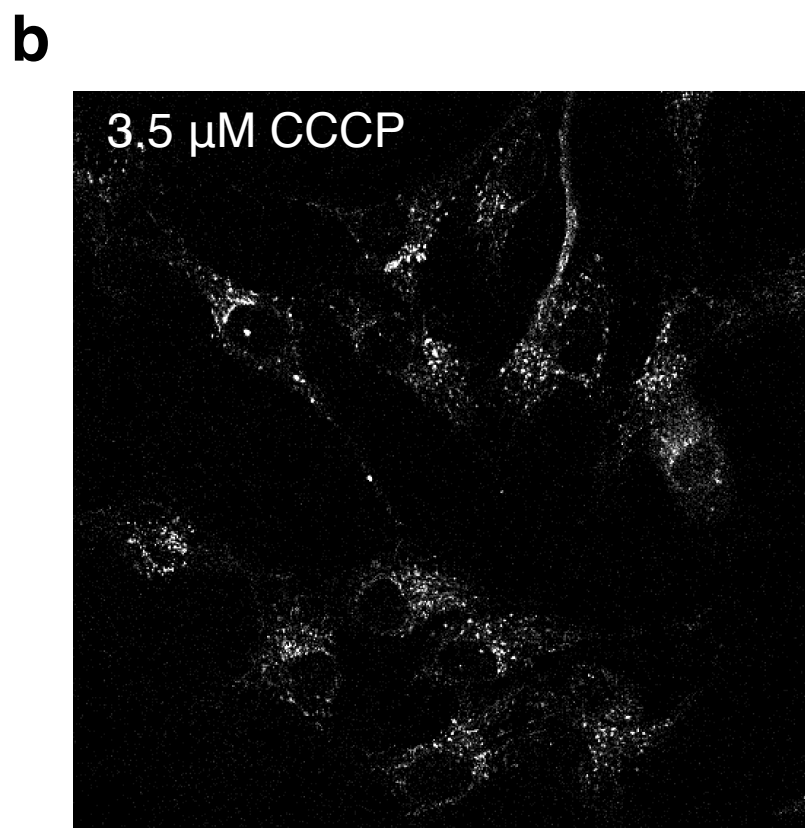
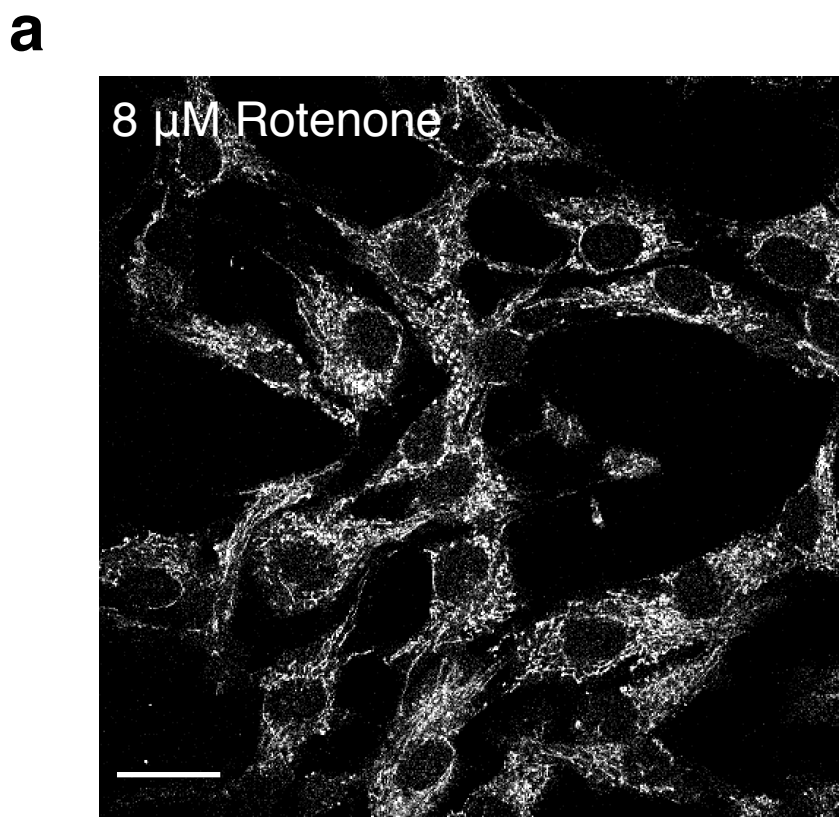


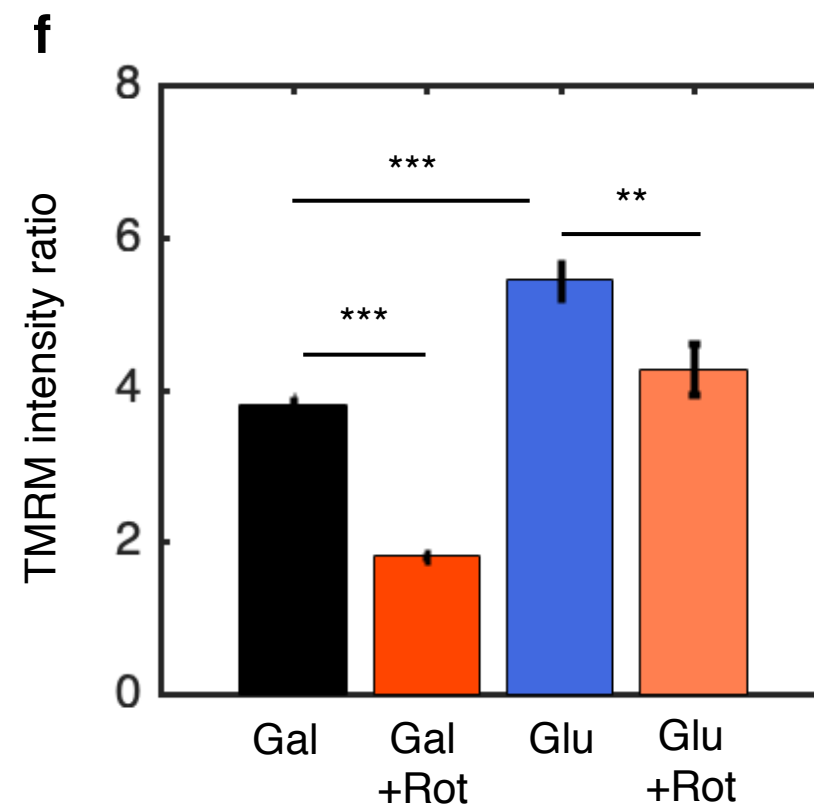
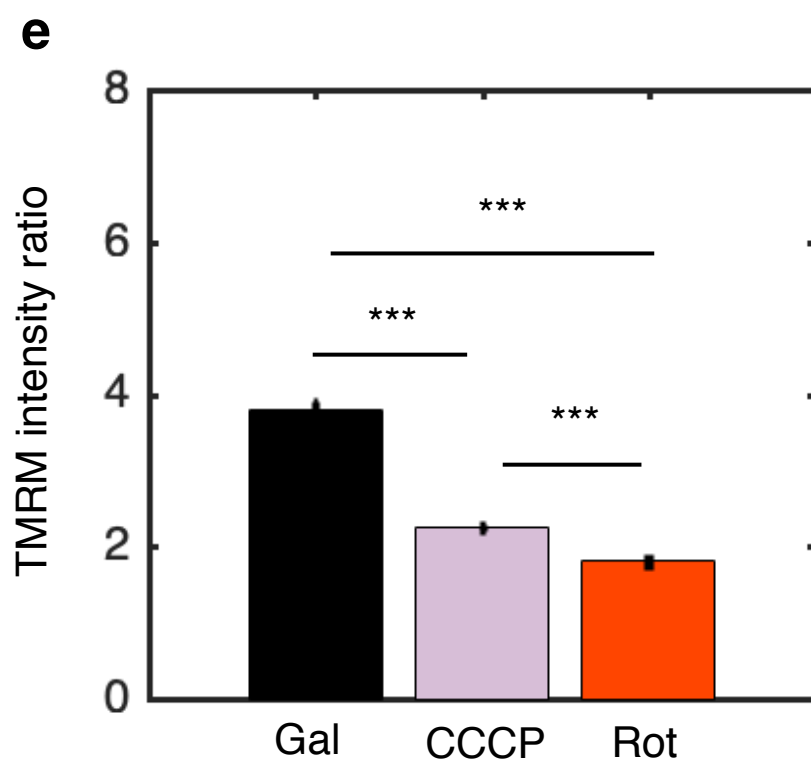
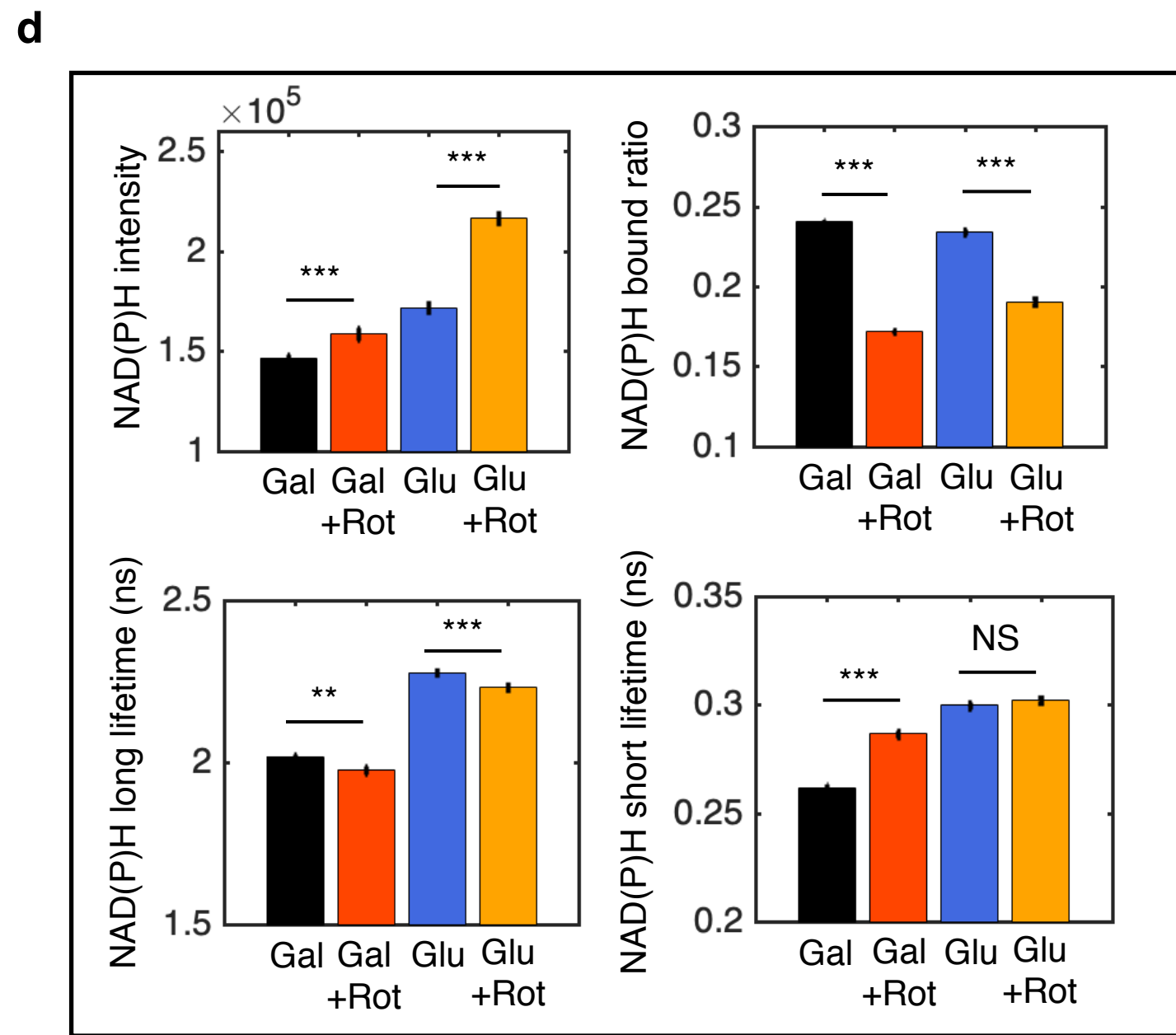
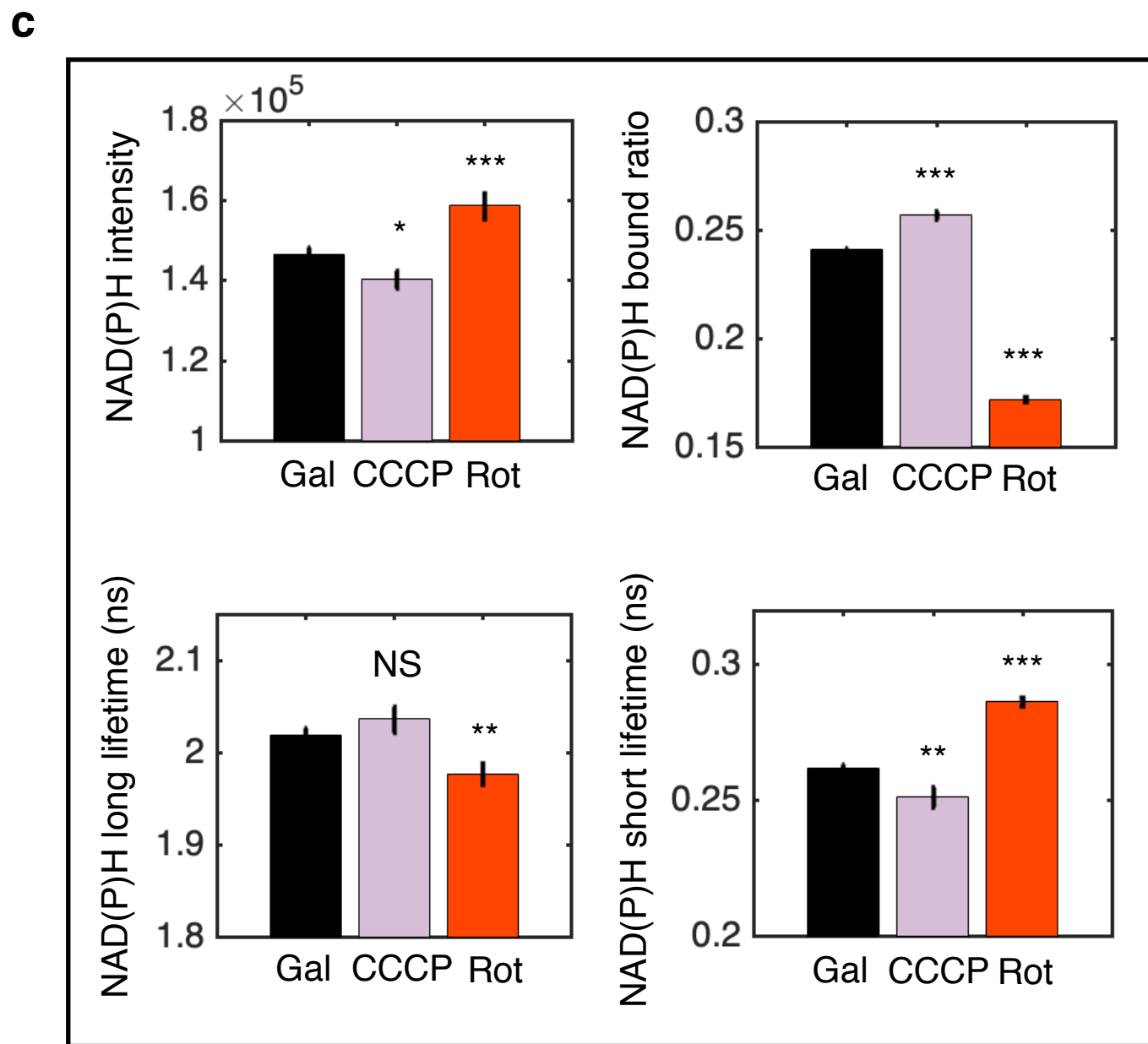
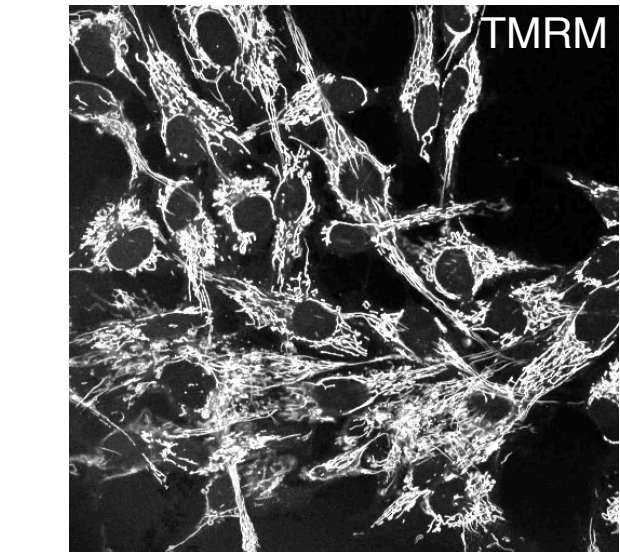
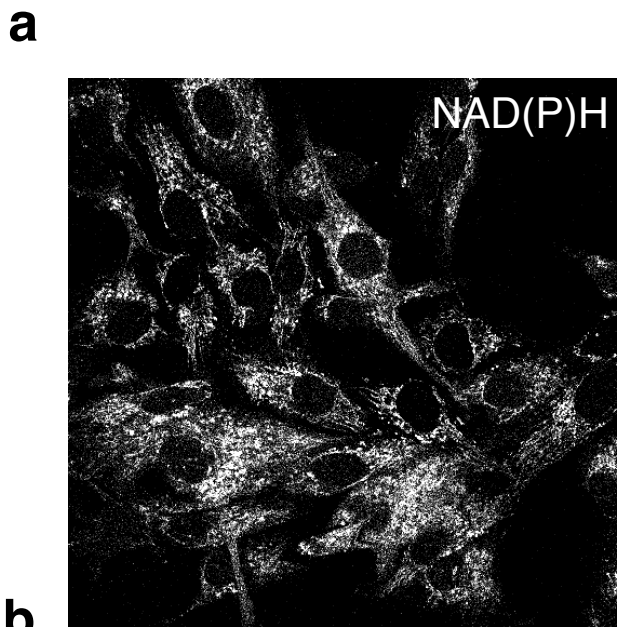










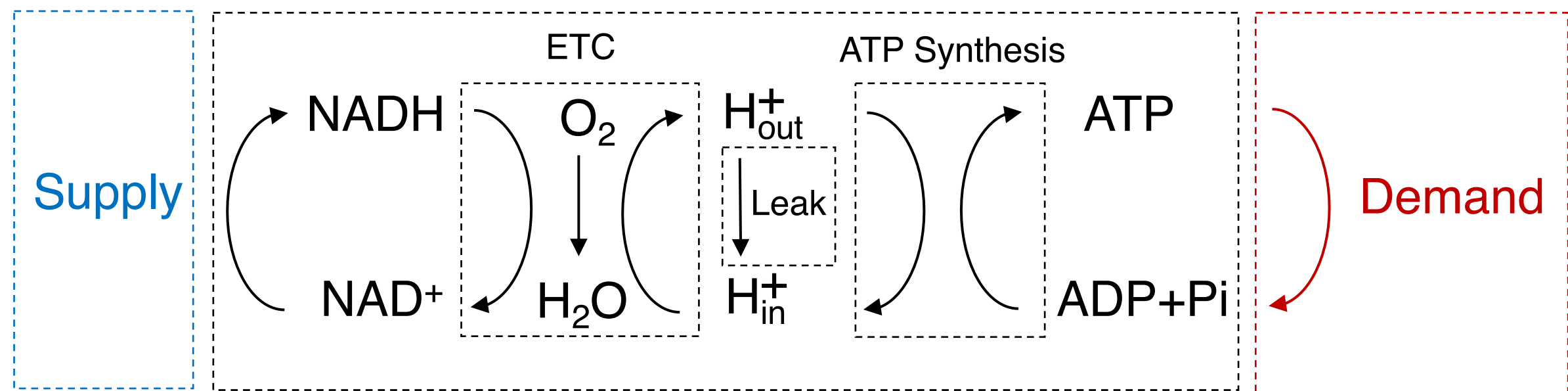


Cytoplasm

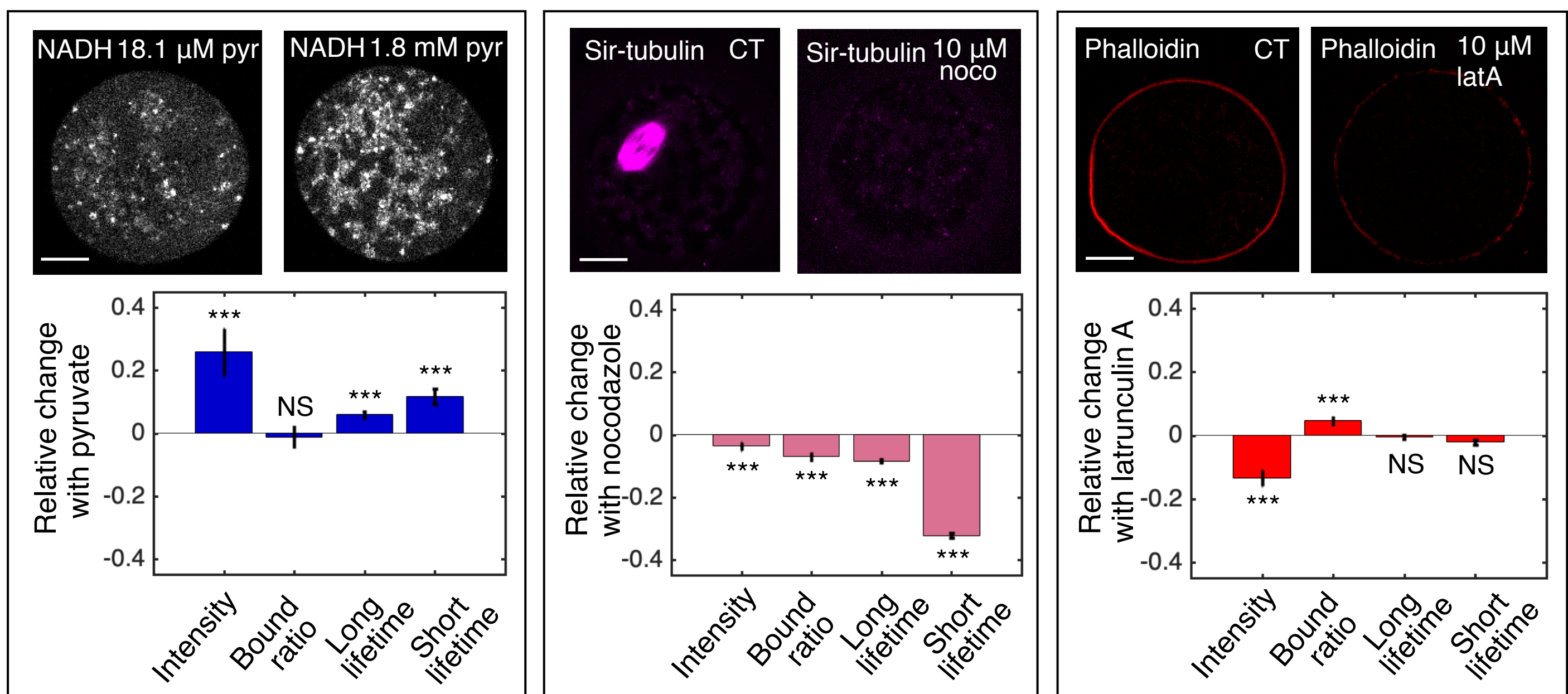
Mitochondria

Cytoplasm

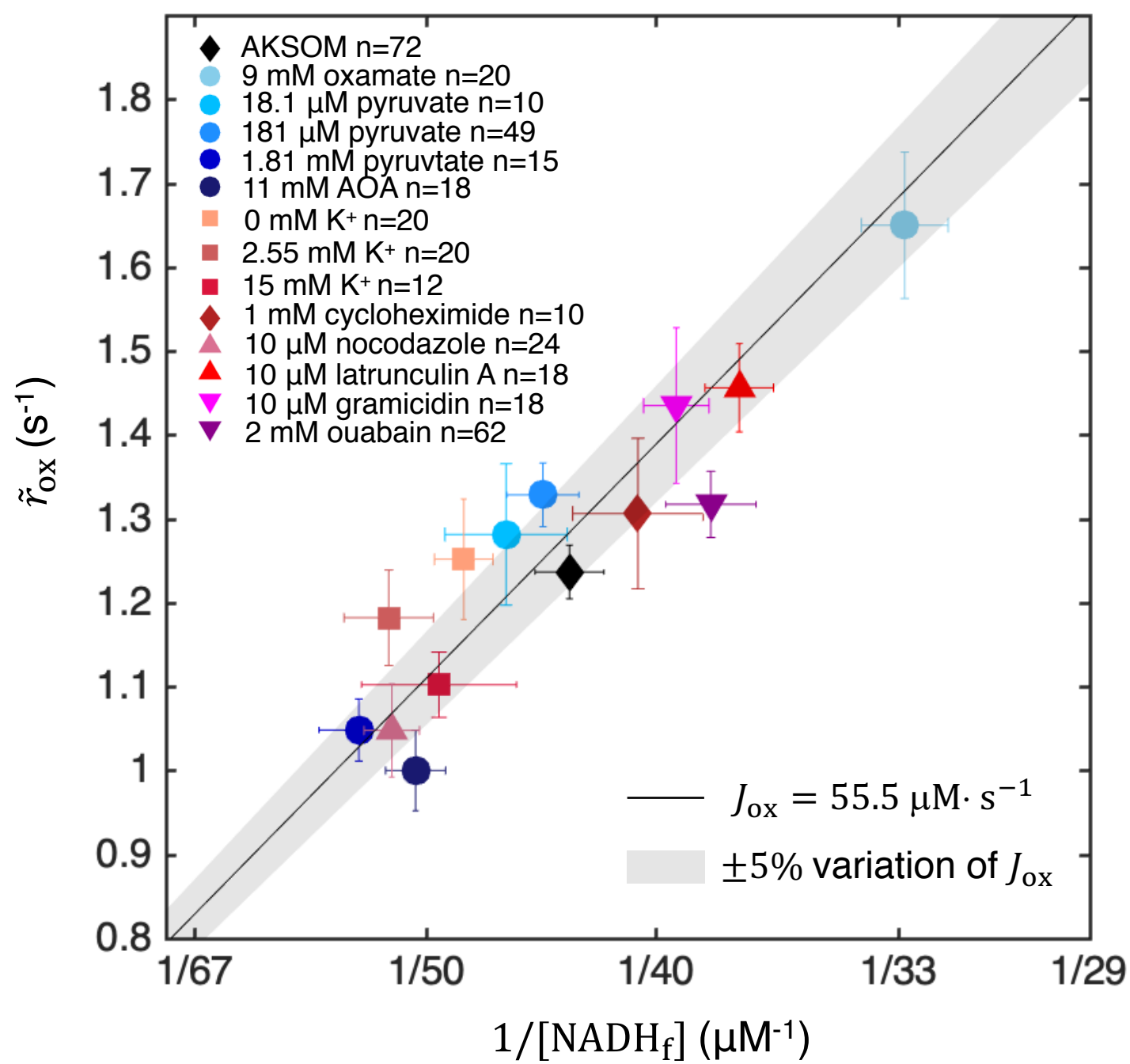
a



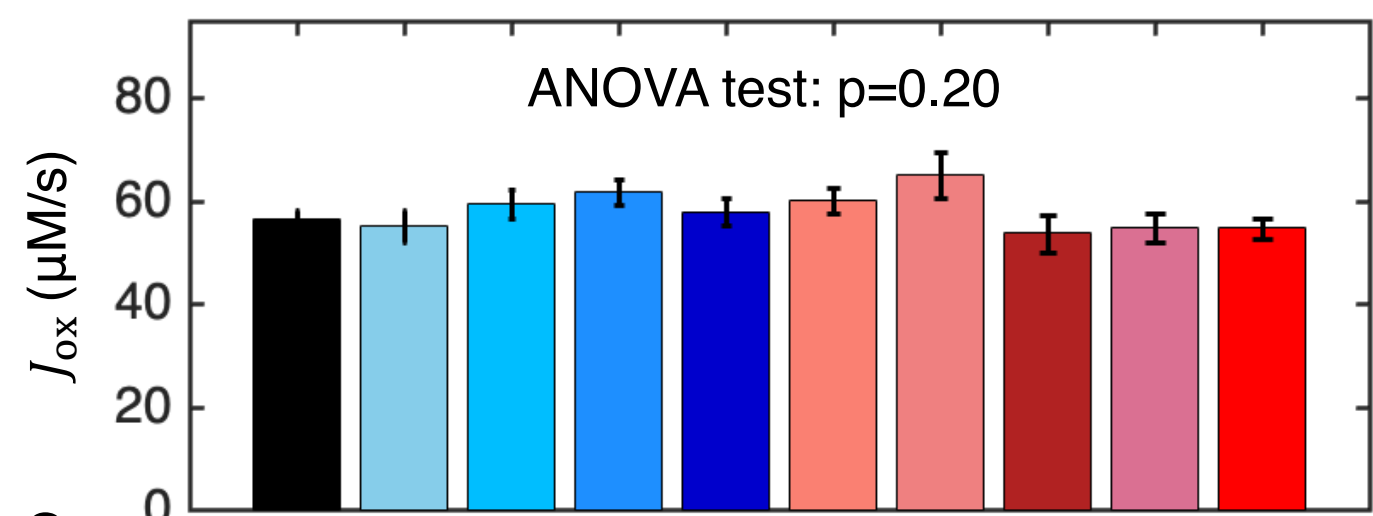
b



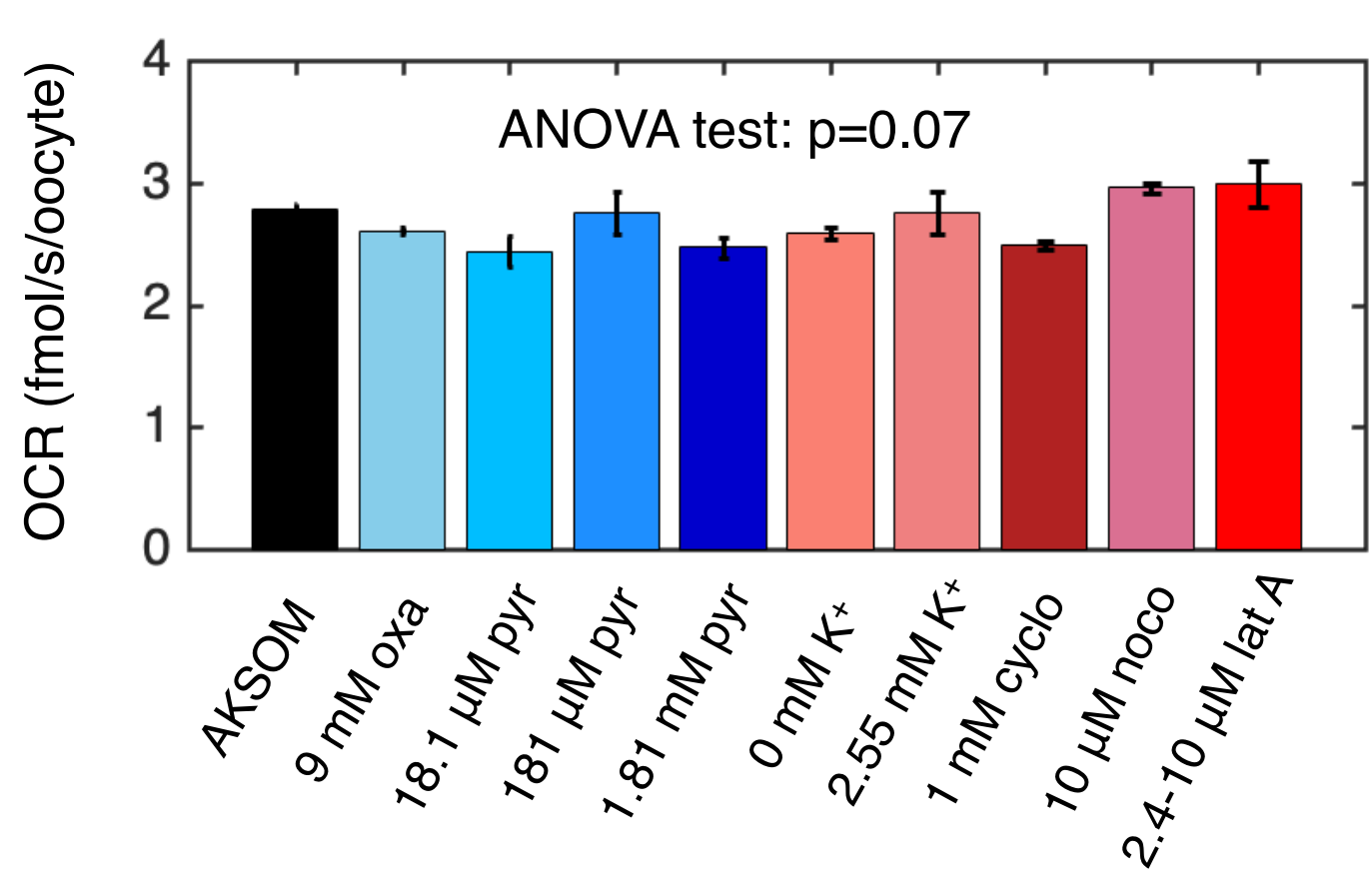
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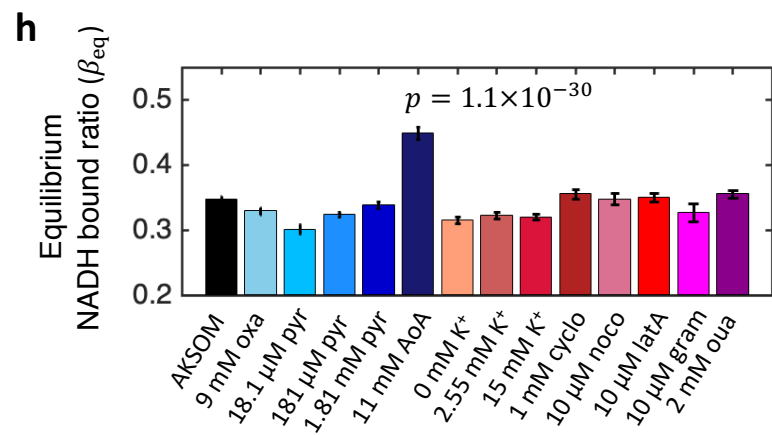
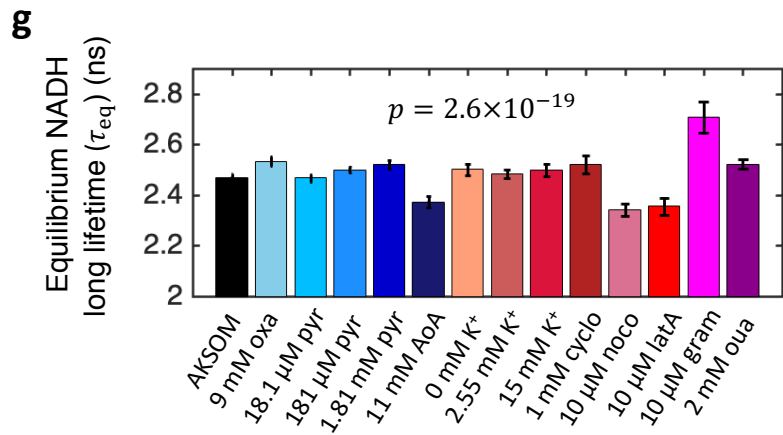
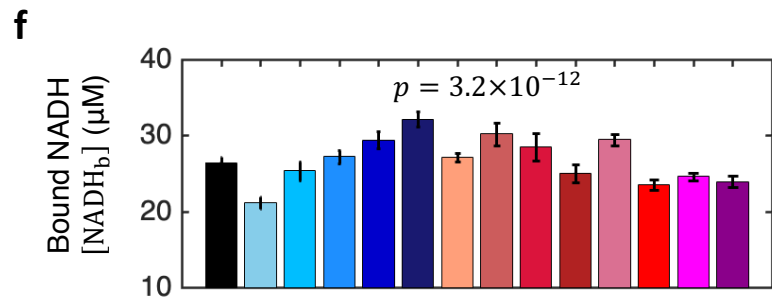
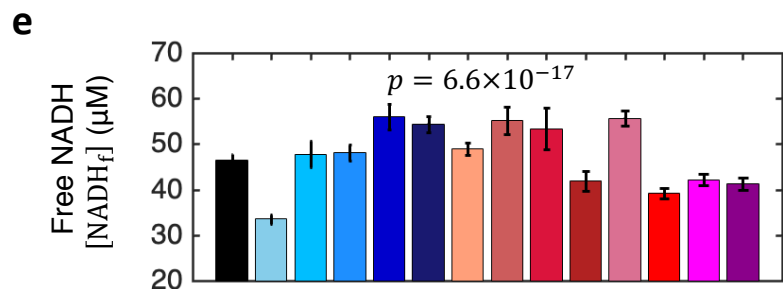
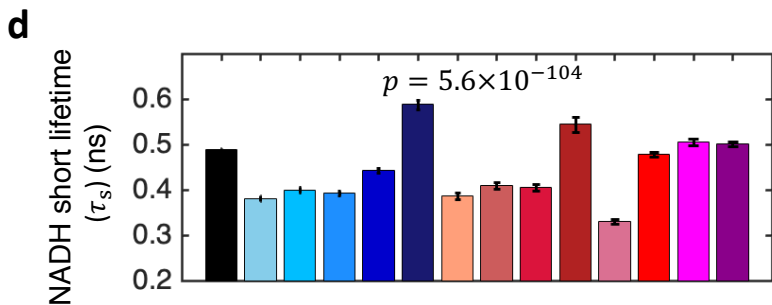
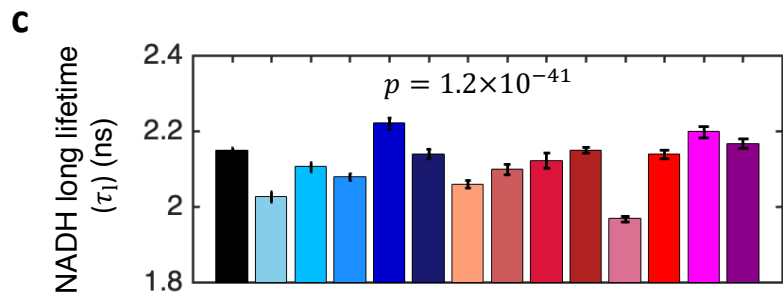
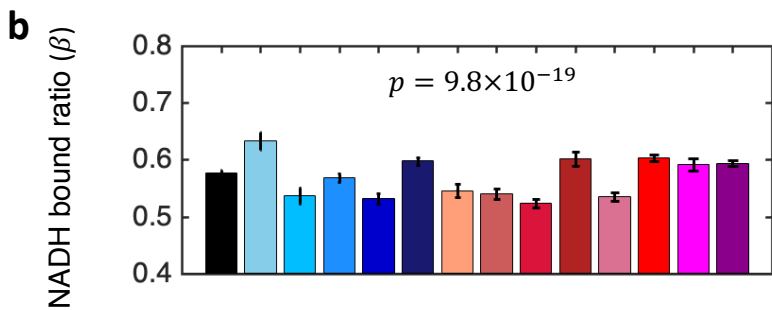
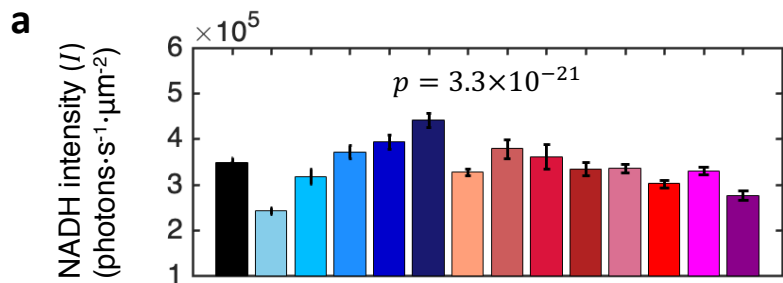


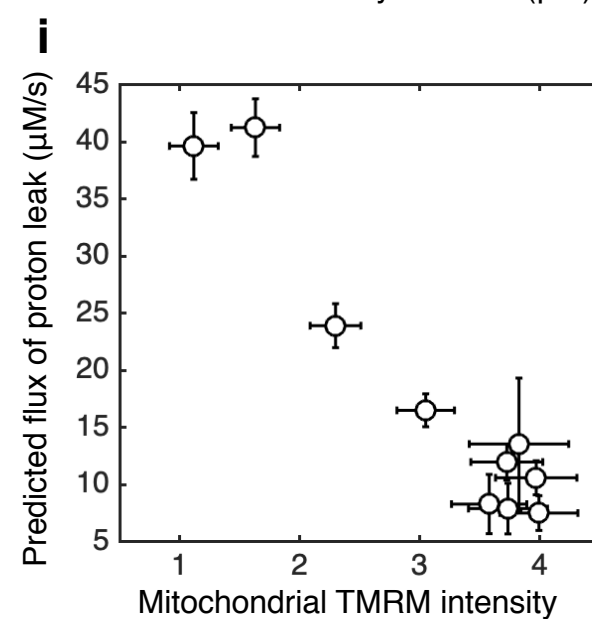
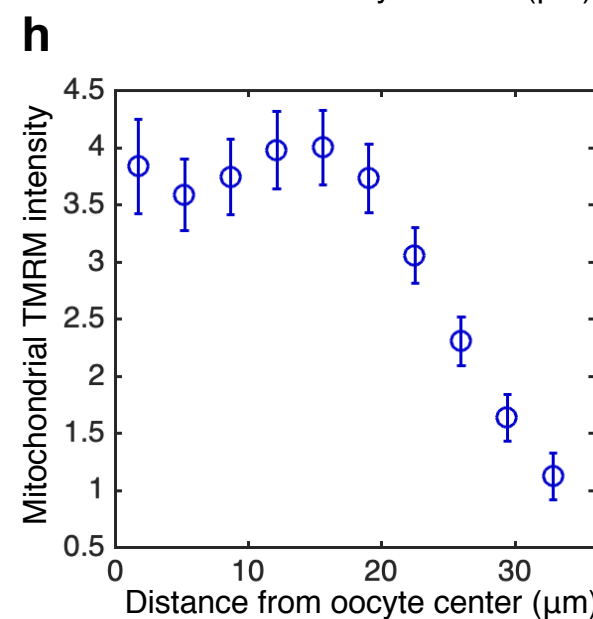
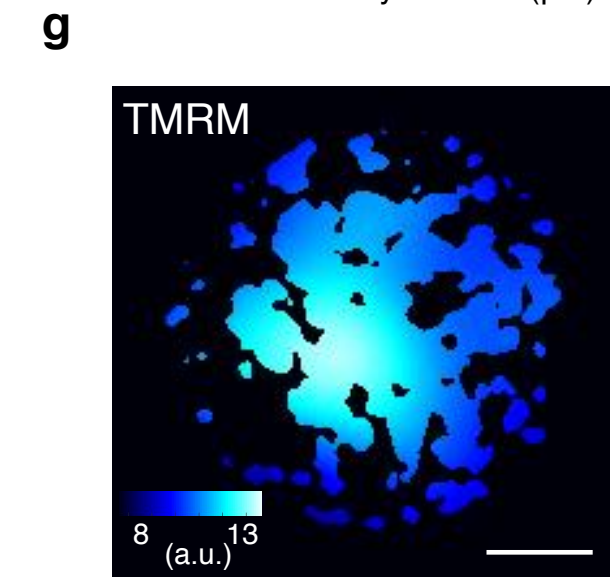
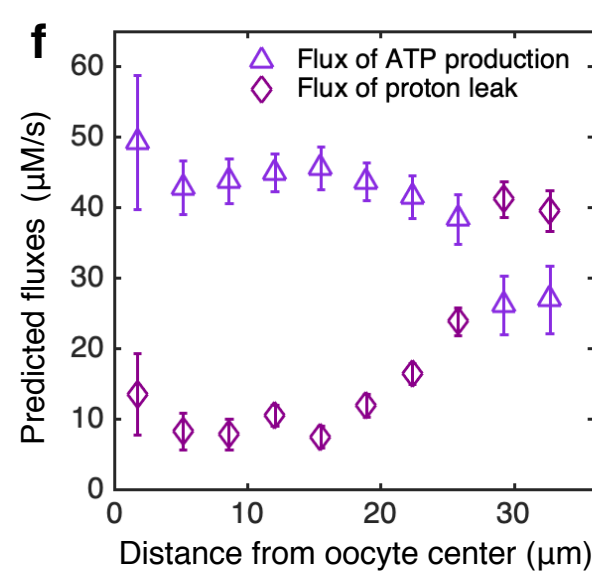
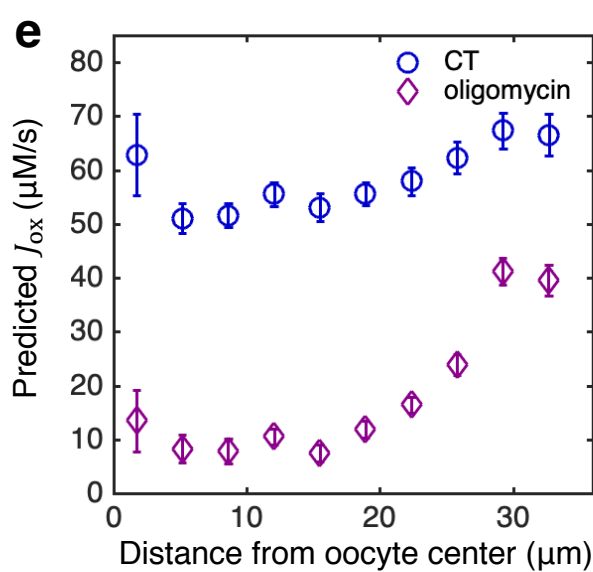
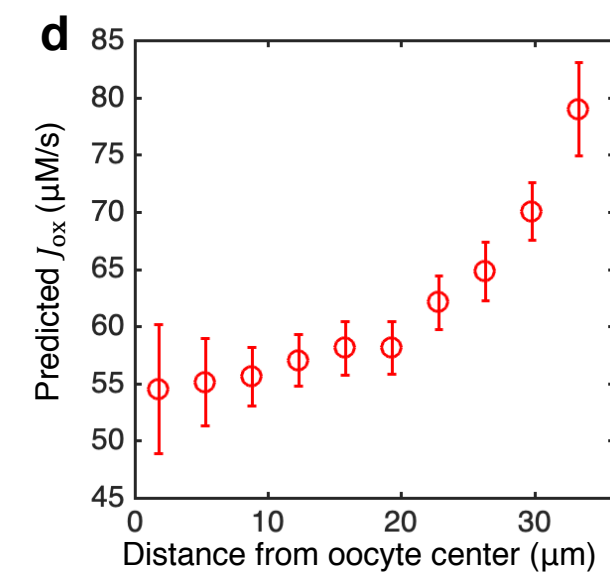
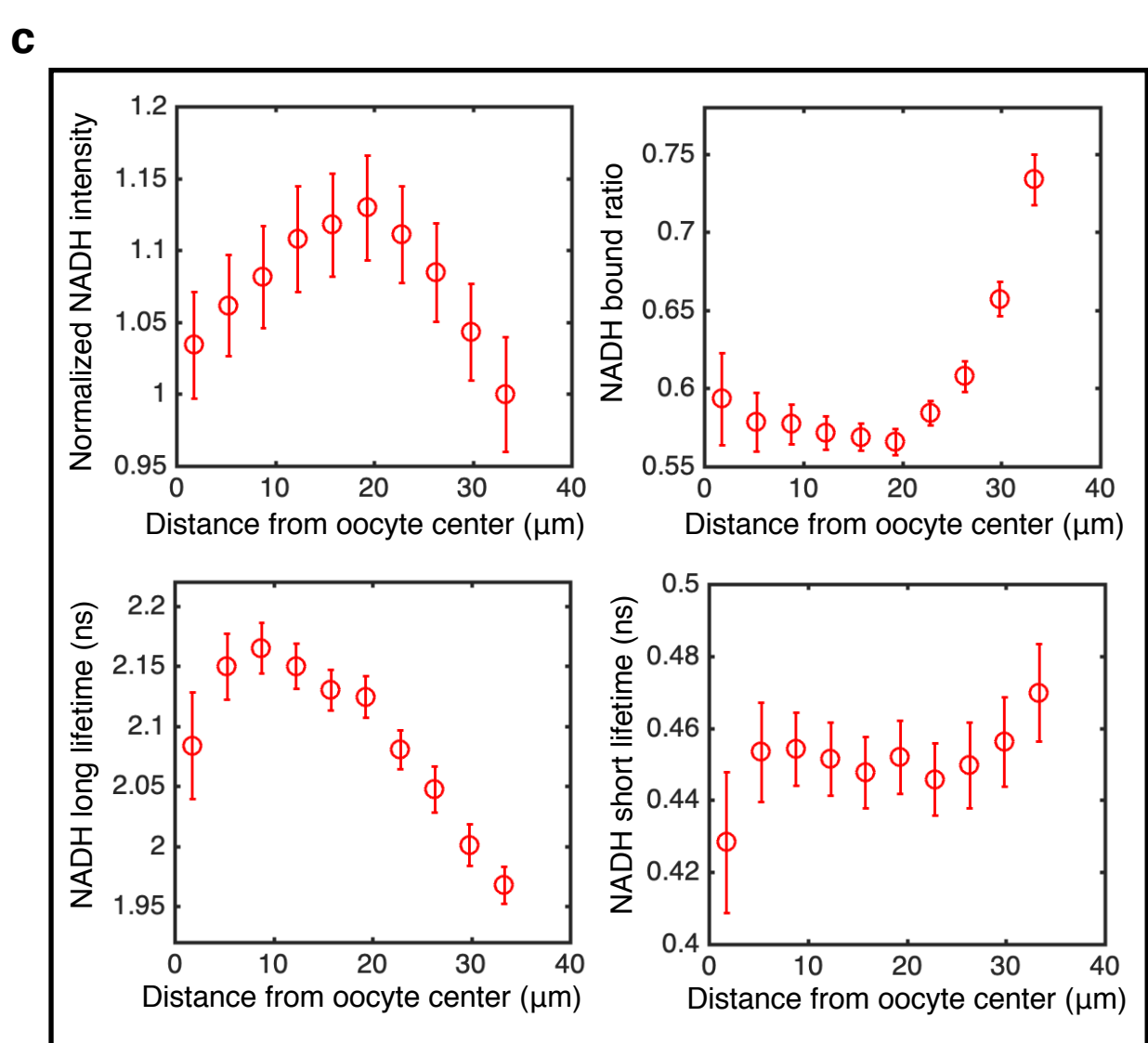
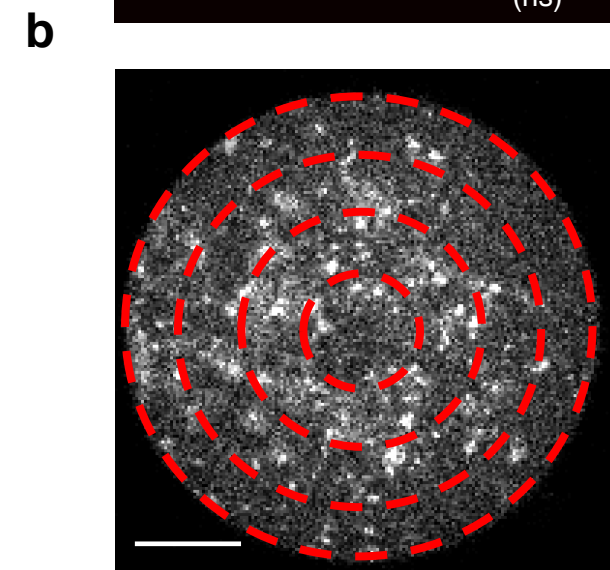
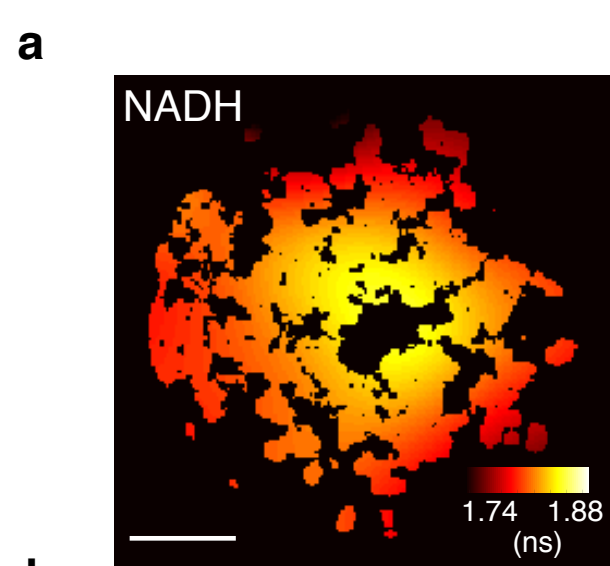
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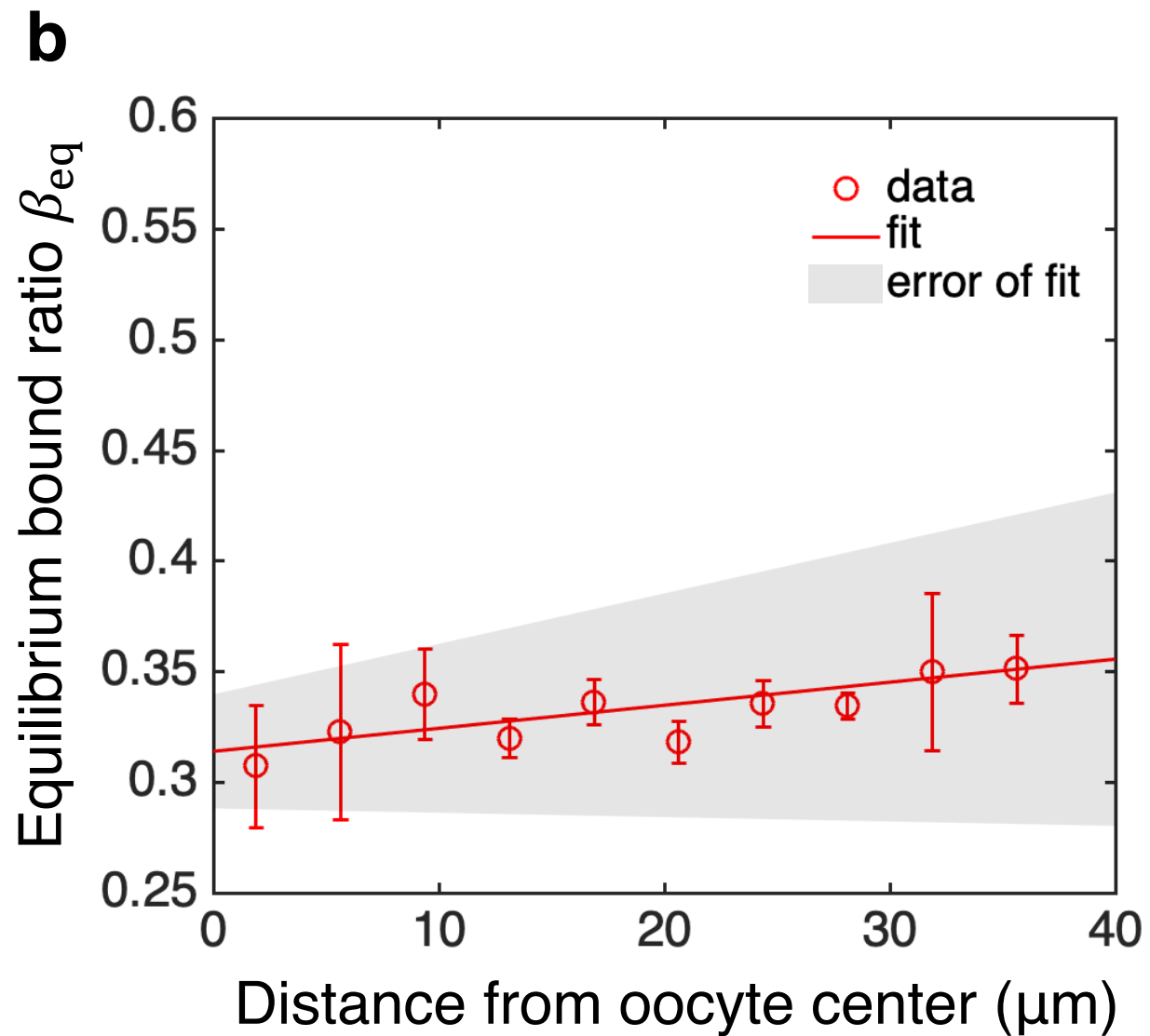
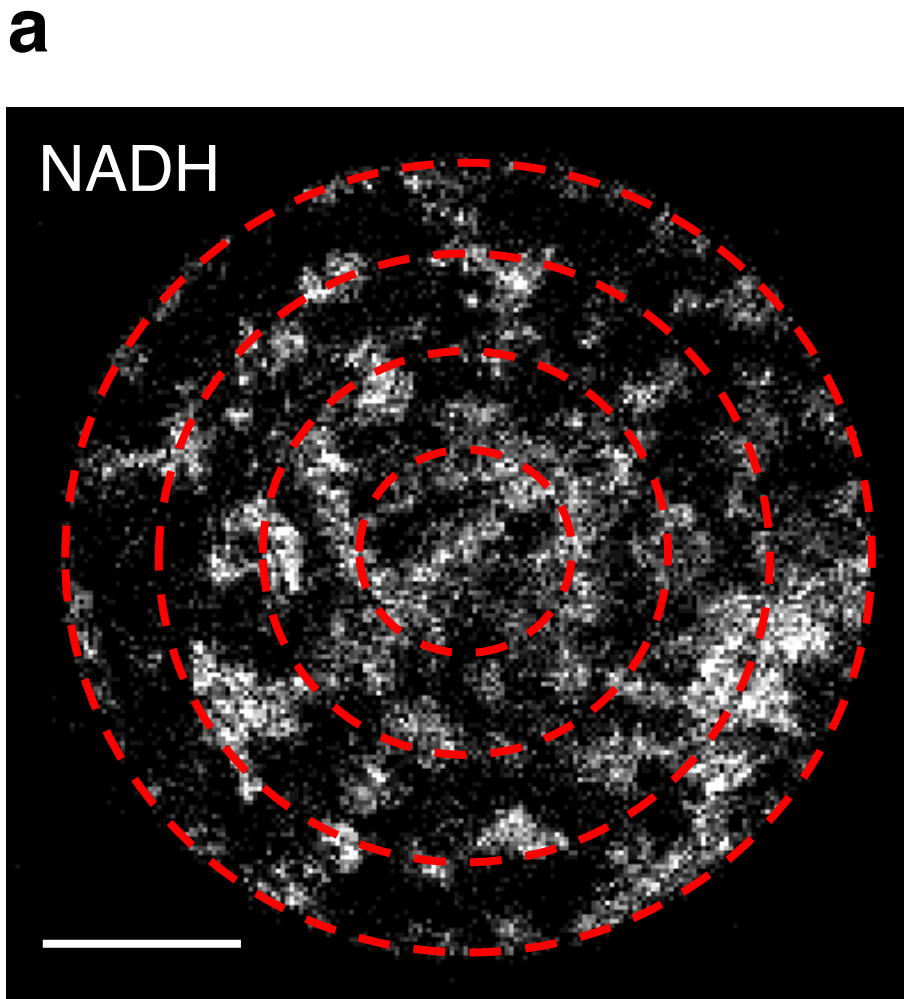


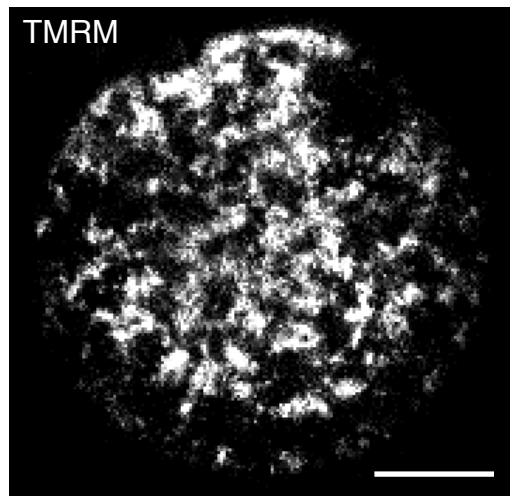
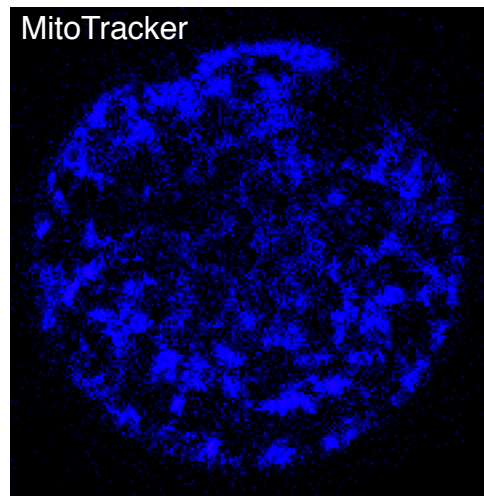
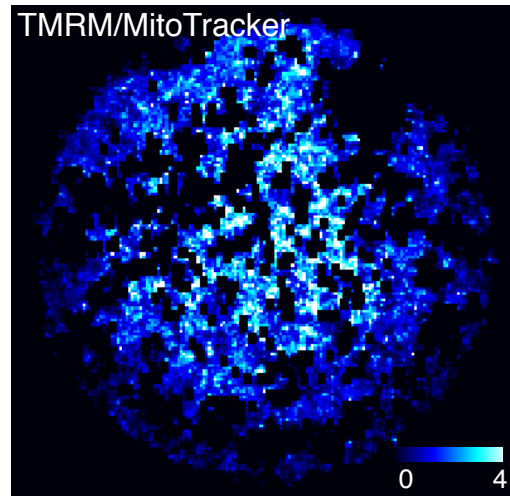
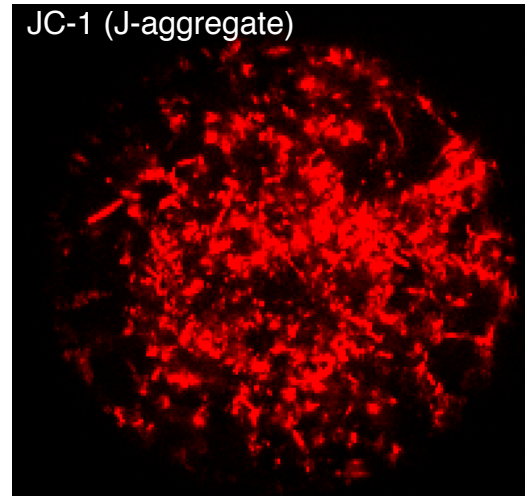
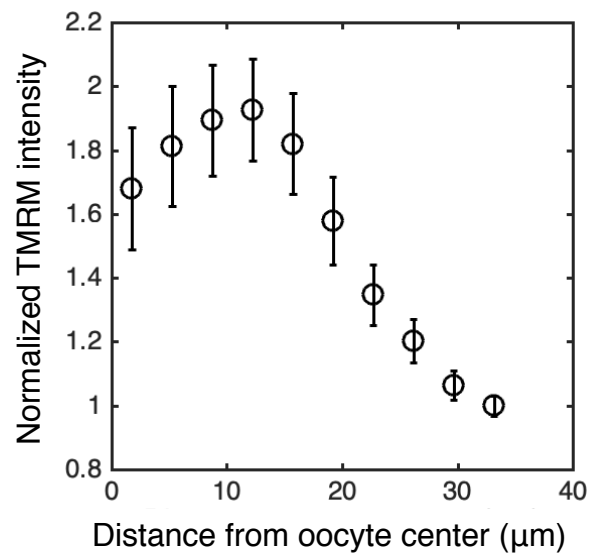
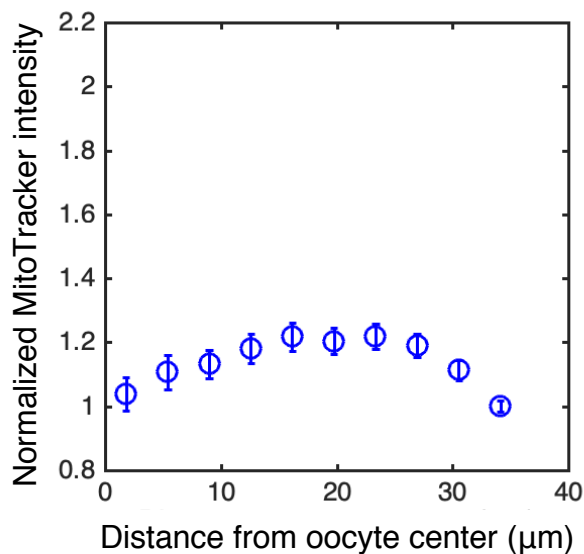
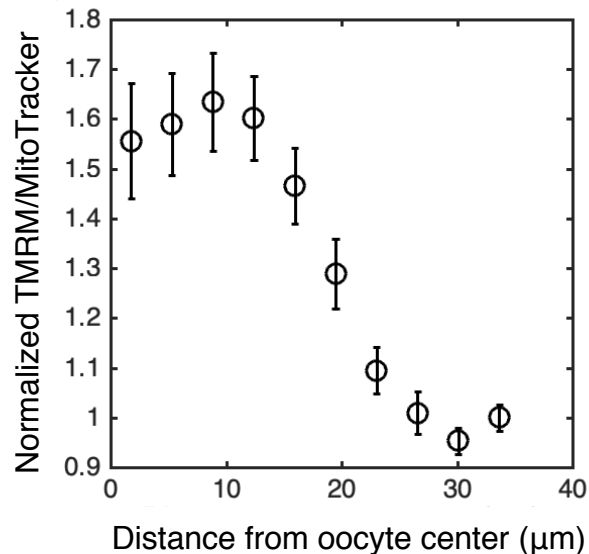
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